Modular Electronics Learning (ModEL) Project

DC Motors

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Chapter 1

Introduction

DC electric motors were the first practical electric motor technology, and dominated early industry until the advent of AC induction motors and AC power distribution systems. Even then, for a while DC motors were still preferred over AC for applications where variable-speed operation was essential, as AC induction motor speed is a function of power frequency.

This module explores the fundamental principles of electromagnetism and electromagnetic induction as they apply to the operation of electric motors. Multiple types of DC motor will be discussed, including the most modern type which is the brushless DC motor.

Important concepts related to DC electric motors include electromagnetism, magnetic attraction/repulsion, magnetic fields, magnetic poles, right-hand rule, Lorentz force, electromagnetic induction, Faraday’s Law of electromagnetic induction, rates of change, Lenz’s Law, brushes, commutators, counter-EMF, Ohm’s Law, Kirchhoff’s Voltage Law, field windings, series versus shunt versus compound motors, transistors, and the Hall Effect.

Here are some good questions to ask of yourself while studying this subject:

- How do magnetic fields and electric currents relate to one another?
- What is electromagnetic induction, and what conditions are necessary for it to occur?
- How does the Right Hand Rule apply to straight-line conductors?
- How does the Right Hand Rule apply to conductive loops?
- What is Lenz’s Law, and how does it apply to electromagnetism?
- How is mechanical torque produced by an electric motor?
- How does the Right Hand Rule apply to the Tutorial’s illustrations showing simple wire and motor structures?
- What practical purpose do brushes and commutator serve in a DC electric motor?
- What replaces the brushes and commutator within a “brushless” DC electric motor?
• How may we force a motor to function as a generator?
• Why does motor current surge when it is first started?
• Why do some motors have permanent magnets while others have field windings?
• What are the characteristics of a series-wound DC motor?
• What are the characteristics of a shunt-wound DC motor?
• What are the characteristics of a compound-wound DC motor?
• What must be done to a DC motor to reverse its direction of rotation?
Chapter 2

Tutorial
2.1 Magnetism and induction

The phenomenon of an electric current creating a magnetic field is called electromagnetism. This effect may be enhanced by forming the current-carrying conductor into a coil shape, which causes each wire turn’s magnetic field to link with the magnetic fields of the other turns in the wire coil, producing a greater net magnetic field:

The terms “north” and “south” refer to the tips of a magnetic compass needle, in honor of which direction they point when allowed to freely orient to the natural magnetic field of the Earth. Like poles repel, while opposite poles attract. While the magnetic field passing through and around the coiled wire is an endless loop just like the circular field surrounding the straight wire, we are able to assign “north” and “south” poles only to the coil because the coil itself has definite ends for the field to enter and exit. A straight wire provides no convenient features to mark the “ends” of the field, and so we cannot place “N” and “S” symbols anywhere along its length.

A coil’s magnetic field may be further enhanced by providing a solid iron path for it to pass through, since iron offers less magnetic “resistance” than empty space or air. This is how powerful electromagnets are made: by wrapping coils of wire around an iron “core” material. The strength of the magnetic field is then easily controlled by varying the intensity of the electric current. Such electromagnets are the basis of solenoid actuators used to exert mechanical force, as well as electric motors used to perform mechanical work.

Note the arrowhead symbols used to denote both current (red) and magnetic field (green) directions. These directions are of course, conventions, but still we need a way to consistently

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1 This means that any bar-shaped magnet will tend to orient itself such that its “north” pole points toward the Arctic and its “south” pole toward the Antarctic. Since opposite magnetic poles attract, this actually means that the natural magnetic pole located on Earth’s north (Arctic) end is actually “magnetic south” and vice-versa. Confusing, no?

2 As we know, the direction of “conventional flow” for electric current is merely what early experimenters assumed was the correct direction of the mysterious “electric fluid” for which they had no reliable means to discern. Later discoveries showed that in fact electric current through metallic conductors is comprised of negatively-charged electrons
2.1. MAGNETISM AND INDUCTION

associate electromagnetic polarity with current direction, and for this purpose we have the right-hand rule. If you curl the fingers of your right hand as though forming a fist, and point your thumb outward (perpendicular to your wrist), your fingers and thumb will serve as a faithful guide to associating conventional-flow current with magnetic north. For a straight current-carrying conductor, your thumb points in the direction of conventional current flow and your curled fingertips point in the direction of magnetic north. For a coiled conductor, your curled fingertips point in the direction of conventional flow while your thumb points in the direction of magnetic north:

![Diagram showing application of the right-hand rule](image)

The challenges of representing vectors existing in three physical dimensions accurately on a two-dimensional page are obvious. A common notation used to represent vector arrows perpendicular to the page is to show arrowheads as circles with center-dots (as though you were looking at a cone-shaped arrowhead headed toward your eyes) and arrow tails as “X” symbols (as though you were looking at the fletchings of an arrow headed away from you). Here is a view of the same circuit using this notation to show the true orientation of the magnetic field lines perpendicular to the page:

![Diagram showing vector notation](image)

It is a good active-reading exercise to take your right hand and try applying it to this illustration, first pointing your thumb in the direction of current for each straight wire section and seeing how the curl of your fingers match the arrow head/tail symbols, then curling your fingers in the clockwise direction of the circuit’s current and verifying that your thumb indeed points into the page with the arrow tails in the center of the wire loop.

which actually flow in the direction opposite to the accepted convention. This matters less than one might suppose. Magnetic fields are even more arbitrary, as there are no particles actually drifting anywhere to constitute a direction, but still it is necessary for the sake of accurate communication to define “north” and “south” polarity of these fields. Incidentally, the definition of “north” for a magnetic field is that of the north-pointing end of a magnetic compass needle, which means that the magnetic pole located near the Earth’s geographic north pole (in the Arctic) is actually “magnetic south” so that the “magnetic north” of a compass’ needle will be attracted in that direction!

3Either an entirely straight wire, or a straight section of wire that is part some other shape.
Magnetic fields react with one another to produce force, and this is useful for converting electrical energy into mechanical work. If we know we can create magnetic fields using electric current, and we also know these fields repel (same poles) and attract (opposite poles), it is fairly simple to build electro-mechanical machinery using electricity to produce mechanical motion (e.g. electric motors).

The foundational principle of electromagnetic force generation is another variation of the right-hand rule where the index finger, middle finger, and thumb point in straight lines all perpendicular to each other, relating the vectors of electric current motion ($Q\vec{v}$), magnetic flux direction ($\vec{B}$), and Lorentz force ($\vec{F}$):

Two parallel current-carrying conductors a mutual force proportional to both their currents. If the currents travel in the same direction, the forces will attract; if the currents flow in opposite directions, the forces repel. The following illustrations show three different pairs of current-carrying conductors viewed from the end (with current either entering into or exiting out of the page, arrow tip and tail markings showing the directions of conventional flow):

Another good active-reading exercise is to map the right-hand rule onto each of these examples, aligning the index finger with the direction of electric current, the middle finger with the magnetic flux vector from the near side of the other conductor, and verifying the proper direction of the Lorentz force vector.

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4 A vector quantity is one with both a magnitude and a direction, as opposed to a scalar quantity which only has magnitude and no specified direction.

5 Instead of using $I$ to represent current, which is a scalar quantity, we express the motion of electric charges more directly in terms of charge quantity ($Q$, in Coulombs) multiplied by vector velocity ($\vec{v}$, in meters per second).
Complementary to electromagnetism is the phenomenon of electromagnetic induction. This occurs when a conductor experiences a perpendicular magnetic field varying in strength over time. This is how generators are constructed: by moving coils of wire past a stationary magnetic field, or vice-versa. The amount of voltage induced across the coil is proportional to the number of turns of wire in that coil and to the magnetic field’s rate-of-change over time. This mathematical relationship is expressed in Faraday’s Law of Electromagnetic Induction:

$$V = N \frac{d\Phi}{dt}$$

Where,
- $V$ = Induced voltage across the coil, in Volts
- $N$ = Number of “turns” or “wraps” in the coil
- $\frac{d\Phi}{dt}$ = Rate-of-change of magnetic flux, in Webers per second

Electromagnetic induction is proportional to the rate at which a magnetic field strengthens or weakens perpendicular to a conductive coil. This means a voltmeter connected to a wire coil will register nothing when a nearby magnet is stationary, but will register voltage every time the magnet moves (either toward the coil or away from it):

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6Magnetic flux is related to magnetic field strength by cross-sectional area, with $B = \frac{\Phi}{A}$. Thus, it is valid to think of magnetic field strength as the degree to which magnetic flux is concentrated into an area. This holds true for the units of measurement used to express each: the unit of the Tesla used for magnetic field strength ($B$) is equivalent to Webers of flux per square meter.
If such a coil is connected to form a complete circuit allowing an electric current to form when the magnet advances or retreats, the coil will produce its own magnetic field of such a polarity as to oppose the inducing field’s change. This is called *Lenz’s Law*, and it stands as a universal feature of induction: **the induced effect always opposes the inducing cause.**

Examine the illustrations below showing a coil of wire facing a permanent magnet. In the left-hand illustration the magnet is stationary and therefore no induction occurs. In the center and right-hand illustrations the magnet moves, causing the coil to experience a varying magnetic field and thereby causing induction. The short-circuit permits current as a result of this induction, and we know any electric current through a coil produces its own magnetic field. Lenz’s Law tells us this *induced* magnetic field must act to counter the motion of the permanent magnet:

[Insert illustrations showing magnetic fields and current directions]

Inserting an electrical resistance into the coil’s circuit diminishes the strength of this reaction, but does not alter its direction. Note how the coil functions as a *source* to the resistor’s *load*:

[Insert illustrations showing current passing through a circuit with and without resistance]

If we break the circuit, no current may pass and therefore no opposing magnetic field can form. However, the coil must still generate a voltage in accordance with Faraday’s Law, and the polarity of that voltage will be the same as it would if there were a resistive load connected:

[Insert illustrations showing voltage generation without current]

In case you were wondering, all these current directions and voltage polarities will reverse if we swap either the permanent magnet’s polarity (i.e. South pole facing the coil) or the direction the coil is wrapped around its core. Reversing both of these parameters is equivalent to a double-negative, resulting in the same current directions and voltage polarities as shown above.
2.2 Permanent-magnet motors

Magnetism, of course, is a direct consequence of moving electrical charge carriers, which is why every current-carrying conductor is surrounded by its own magnetic field. Certain materials\(^7\), however, may be made “permanently” magnetic, requiring no electric current to sustain their own magnetic field. The common bar magnet and horseshoe magnet are examples of this phenomenon.

If a pair of permanent magnets are arranged to form a magnetic flux spanning a gap, and a current-carrying conductor placed within that gap perpendicular to the permanent magnetism, the conductor will experience a lateral force perpendicular to both the current and the magnetic flux vectors. This is the familiar Lorentz force, following the right-hand rule:

\[ \text{N} \quad \text{S} \quad \text{Force} \quad \text{S} \quad \text{N} \]

\(^7\)All ferromagnetic materials such as iron have the ability to retain at least some magnetic flux after the magnetizing stimulus has been removed. Certain so-called rare earth compounds are exceptionally good in this regard.
If we revise this experiment slightly and place a loop of wire within that same gap, the loop experiences a torque (i.e. twisting force) as one wire is forced upward and the other downward:

This makes sense if we view the loop as a pair of wires with each wire experiencing its own force by the perpendicular right-hand rule (left-hand wire forced up and right-hand wire forced down), or alternatively if we consider the loop as a partial coil with the curled-finger version of the right-hand rule informing us of the coil’s magnetic polarity (north down and south up), with north repelling north, south repelling south, and north-south attracting. Either way the loop tries to rotate clockwise as viewed from the perspective of the battery.

As promising as this seems to be as the foundation for the design of an electric motor, there is a problem: the loop will not spin in a full circle, but instead will stop when its magnetic poles align with the permanent magnets, only one-quarter of a turn away from where it is shown above. Furthermore, the wires connecting the loop to the battery would become twisted together if the loop were (somehow) to turn more than 180 degrees. If only we had a way to make and break connection to the battery at just the right positions as the loop rotated, we might have a way to make this loop fully spin.
An ingenious solution to this problem is a sliding-contact assembly called a *commutator*, and a pair of graphite (carbon) *brushes* serving as contact points between the battery’s wires and the commutator segments. The commutator is simply a pair of semi-circular metal pieces terminating the ends of the wire loop and arranged about the centerline of rotation. These pieces rotate along with the loop as one assembly, making and breaking contact with the brushes as it spins:

When energized by a DC electrical source, the loop continuously turns while the commutator and brushes make and break contact as necessary to maintain the same direction of rotation. Reversing the direction of a permanent-magnet (PM) DC motor is as simple as reversing the polarity of the energizing source:

In order to maintain a strong magnetic field through the rotating loop, it is generally wound around an iron core mounted on a bearing-supported shaft called an *armature*. The armature supports the rotating loop while providing a nearly continuous pathway for magnetic flux lines from one permanent magnet to the other. A circular iron structure joining the magnets’ outer poles together similarly enhances the magnetism by providing a complete magnetic path.
The following illustration taken from page 394 of *Hawkins Electrical Guide Number Two* (published in 1914) shows how the wire loop may be wrapped around an iron armature, as well as directions of current (both conventional and electron flow):

For greater effect, we may substitute a multi-turn coil for a single loop. For even greater effect, we may position multiple coils around the armature, with a multitude of commutator bars for the coils’ termination. Additional illustrations (with captions) taken from pages 400 and 401 of the same text show photographs of typical DC motor components:
2.2. PERMANENT-MAGNET MOTORS

Most industrial DC motors have multiple armature coils and commutator segments (also called bars), not just a single “loop” and two segments as shown in the previous model. A photograph of a large (1250 horsepower) DC motor used to propel a passenger ferry ship is shown here, with the field and armature poles clearly seen (appearing much like spokes in a wheel):

A close-up of one brush assembly on this large motor shows both the graphite brush, the brush’s spring-loaded holder, and the myriad of commutator bars the brush makes contact with as the armature rotates. Each armature coil terminates at two of the commutator bars:
2.3 Counter-EMF

As the coils of a DC motor’s armature rotate within the stationary magnetic field of the permanent magnets, they experience an induced voltage as described by Faraday’s Law of Electromagnetic Induction:

\[ V = N \frac{d\Phi}{dt} \]

Where,
- \( V \) = Induced voltage across the coil, in Volts
- \( N \) = Number of “turns” or “wraps” in the coil
- \( \frac{d\Phi}{dt} \) = Rate-of-change of magnetic flux, in Webers per second

Thus, a PM motor also functions as a generator. This is true whether the armature is spun by an external (mechanical) torque or if it is running as a motor. When running as a motor, the induced voltage actually opposes that of the external source – an example of Lenz’s Law in action: the induced effect always opposing the inducing cause.

A helpful problem-solving strategy to simplify complex systems is to model them as collections of simple elements. Here, we will visualize counter-voltage (commonly known as counter-EMF or back-EMF) as an internal DC voltage source series-opposed to the external source powering the motor. For a permanent-magnet DC motor, the magnitude of this counter-EMF is a direct function of shaft speed:

Armature current may be calculated by applying Ohm’s Law and Kirchhoff’s Voltage Law, since armature coil resistance is fairly constant, and the net voltage dropped across that coil’s resistance will be the difference between the external source voltage and the counter-EMF:

\[ I_{\text{arm}} = \frac{V_{\text{external}} - V_{\text{CEMF}}}{R_{\text{arm}}} \]

Counter-EMF explains why for any given applied voltage there is a top speed for a PM motor: at this top speed, the counter-EMF is only slightly less than the external voltage source. If the motor were to somehow spin faster, its counter-EMF would equal the applied voltage and armature current would cease, resulting in zero torque (i.e. zero motor action). Spinning faster yet would result in \( V_{\text{CEMF}} > V_{\text{external}} \) which would result in the motor functioning entirely as a generator and sending

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\(^8\)EMF stands for electromotive force, and it is an older (and not particularly accurate) synonym for voltage.
2.3. COUNTER-EMF

Power to $V_{\text{external}}$ which would act as a load. Therefore, since the amount of source voltage must always be greater than the amount of counter-EMF in order for the machine to function as a motor (load), the source voltage magnitude places an upper limit on a PM motor’s top speed.

Torque (twisting force) is a function of both the stationary magnetic field strength (which is constant for a PM motor) and the rotating armature’s magnetic field strength (which varies with current). Therefore, current determines a PM motor’s torque.

When electrical power is first applied to a stationary PM motor, the result is a high armature current and a corresponding high torque because counter-EMF is zero. As shaft speed increases, counter-EMF increases with it, resulting in less net voltage dropped across the armature coil resistance and less armature current. This initial surge of current during motor start-up is commonly known as inrush current.

Interestingly, this phenomenon of high starting current and relatively low running current is common to all electric motors regardless of design, because it is founded on the universal principle of Lenz’s Law. Every electric motor simultaneously functions as a motor and as a generator, with the generated voltage (counter-EMF) of a running motor less than the applied voltage from the external source. This also means that every motor may be pressed into service as a generator simply by mechanically driving it to a faster speed than it would ordinarily run when powered as a motor, forcing its counter-EMF to exceed the applied voltage. In fact, this is one of the reasons why electric-drive vehicles enjoy high energy efficiency when driven in stop-and-go conditions: the vehicle’s drive motor functions as a generator when decelerating, converting the vehicle’s kinetic energy into electricity to re-charge the on-board battery with potential (chemical) energy. Combustion-based engines have no means to recover the vehicle’s kinetic energy, and so they are only able to decelerate by dissipating that kinetic energy as heat (e.g. friction brakes or engine compression braking).

Permanent-magnet (PM) electric motors are the simplest form of DC motor design, but they have significant limitations. Permanent magnets are expensive and dangerous to handle at large sizes, and so PM motors tend to be small. Additionally, the range of operating speed for a PM motor is limited by the range of supply voltage. In order to build large DC motors more economically, as well as to enjoy wider operating speed range, it becomes necessary to replace the permanent magnets with electromagnet coils called field windings. Multiple options exist for field winding configurations, which we will explore in subsequent sections.
2.4 Series-wound motors

An alternative to using permanent magnets to establish the stationary magnetic field needed for a DC motor, we may use electromagnets formed of wire coils wrapped around iron poles. When such a “field winding” is connected in series with the motor’s armature, we have a series-wound motor:

A wound-field motor does not reverse rotational direction when we reverse the polarity of the DC source, because reversing source polarity reverses the magnetic polarities of both field and armature. If north attracted south with the old polarity, south will still attract north with the new polarity, resulting in the same direction of rotation. In fact, polarity is so irrelevant to the operation of a wound-field motor that we may operate it on AC as well as DC!

The speed and torque characteristics of a series-wound motor differ greatly from that of a PM motor, principally because the strength of the stationary magnetic field varies with armature current for the series-wound motor, whereas it was constant for the PM motor. A “thought experiment” helps us understand the impact of this difference.

Imagine how a series-wound motor reacts when first powered from a stand-still condition. Before the shaft begins to rotate, counter-EMF is zero. This results in maximum voltage drop across the resistances of the field and armature windings, and therefore maximum current. This strong current creates strong magnetic fields for both the field and armature windings, thereby creating a very high torque (twisting force). As shaft speed increases, however, counter-EMF begins to rise. The increasing counter-EMF subtracts from the source voltage to leave less available to drop across the field and armature windings, thereby reducing current and weakening both their magnetic fields. In turn, this weakening of the field winding’s current results in less counter-EMF for any given speed, which in turn results in current remaining fairly constant as speed increases. Rather than counter-EMF building linearly with speed as was the case with the PM motor, a series-wound motor’s counter-EMF is self-limiting. This allows motor speed to increase almost without limit, resulting in exceptionally high top speeds for modest source voltages.

For this reason, series-wound motors are used where a very wide speed range is necessary, and where excessive speed will be constrained by the mechanical load.
2.4. SERIES-WOUND MOTORS

Series-wound motors find popular use in power tools. An early example of this application is found in Royal Lee’s 1946 patent\(^9\), where he shows such a motor at the heart of a hand-held drill:

Noteworthy items shown in this diagram include the armature (11), field windings (10), commutator (34), graphite brushes (35), and springs (36) designed to maintain firm contact between the brushes and commutator bars. Threaded access caps (36') allow for easy replacement of the brushes when they wear out. Graphite is a fairly soft material – much softer than copper – and so these wear faster than the commutator bars. Like a mechanical pencil whose graphite “lead” wears down and must be replaced, so must motor brushes on a regular basis.

2.5 Shunt-wound motors

Another variation on the wound-field concept is the *shunt-wound motor*, so-called because the field winding is wired in parallel (i.e. “shunt”) with the armature. Like the series-wound DC motor, this field winding substitutes for permanent magnets:

Shunt-wound field coils are made of many turns of thin-gauge wire, compared to the relatively thick-gauge wire windings of a series-wound motor. In a series-wound motor the field winding had to be able to handle the full current of the armature, but here the field winding is its own parallel branch and so we must build that winding such that it limits its own current by resistance ($I_{\text{field}} = \frac{V_{\text{source}}}{R_{\text{field}}}$).

Like the series-wound motor, a shunt-wound motor’s direction of rotation does not reverse when the source polarity reverses, and for the exact same reason: reversing the source polarity swaps magnetic polarities for both the field and armature windings. In fact, the only way to reverse the rotation of either a series-wound or shunt-wound motor is to re-wire the connections between armature and field so that one coil’s polarity reverses while the other remains the same.

The speed and torque characteristics of a series-wound motor differ greatly from that of a PM motor and that of a series-wound motor, principally because the strength of the stationary magnetic field varies with applied voltage, whereas it was constant for the PM motor and it varied with armature current for the series-wound motor. If we increase the applied voltage to a shunt-wound motor in an attempt to increase its speed, what will happen is the field winding’s strength increases, which in turn increases the motor’s counter-EMF by the same proportion, thereby providing additional opposition to the newly-increased source voltage value. The end-result is that speed increases only *slightly* with increased source voltage. Altering the operating speed of a shunt-wound motor requires that the excitation of one winding must be varied *independently* of the other.
2.6 Compound-wound motors

A compromise between the wide speed range of the series-wound motor and the nearly-constant speed of the shunt-wound motor is to build a wound-field motor with two field windings: one in series and one in parallel (shunt):

Not surprisingly, each of these field windings resembles the respective windings of the series and shunt motors: the shunt field winding is a long coil of thin wire for high resistance and low current, while the series winding is a short coil of thick wire designed to bear the full current drawn by the armature.
2.7 Brushless DC motors

A major weakness of all DC motors described thus far are the carbon brushes and commutator bars. The need to conduct relatively high amounts of current through sliding graphite-on-copper contact represents a daunting engineering challenge. Decades of brush design refinement, armature winding techniques, and other technical innovations have permitted electric DC motors to become fairly reliable machines, but still the fundamental problem remains. Brushes and commutator bars wear out over time. Sparking is all but inevitable at the point of interface between the brush and commutator. The intrusion of dust or oil or other contaminants inside the motor will very rapidly destroy the delicate contact between brushes and commutator bars. Clearly, if there was some way to eliminate the need for brushes and commutators, it would represent a significant advance in electric motor performance and reliability.

The first motor technology to challenge DC was the *AC induction motor*, which is a topic for another module. AC induction motors rely on the alternating nature of the source voltage and current to create a “rotating magnetic field” for the rotor to follow, and therefore completely eliminate brushes, commutator, and even coil windings on the rotor. This advance, combined with the advent of an electrical device called a *transformer* established AC as the dominant mode of electric power transmission in the world. It was not until many decades later that solid-state (transistor) technology made possible a new type of DC motor that could rival the AC induction motor’s legendary reliability.

Now that we have reliable solid-state switching devices called *transistors* capable of turning on and off at incredibly high speed, we have the means to build a new type of permanent-magnet motor requiring no brushes and no commutator. Instead of letting the permanent magnets be stationary around a wound armature, we may place the permanent magnets on a rotor and use transistors to switch current on and off (and in different directions) through stationary windings located around the rotor. This is called a *brushless DC motor* or *BLDC* motor, and it may be thought of as a permanent-magnet motor turned inside-out: stationary wire coils surrounding a permanently-magnetized rotor.

For many years brushless DC motors were limited to small power levels for the same reasons as regular PM motors. However, with the advent of *rare-earth magnets* it is now possible to construct powerful brushless DC motors in compact sizes. This technology is popular for drive motors in electric vehicles, as well as countless small-motor applications such as computer processor cooling fans.
An early patent on a form of brushless DC motor invented by William Lear and Samuel Auld shows one representation of a two-pole permanent-magnet rotor (item number 44) surrounded by a four-pole stationary armature (pole face item numbers 60, 62, 64, and 66). Item number 68 represents a cross-sectional illustration of the wire coil (winding) wrapped around each pole:

![Diagram of brushless DC motor with labeled parts](image)

Lear and Auld’s patent also showed a diagram of the armature windings with four switching elements numbered 1, 2, 3, and 4 for sequential energization from the DC source (terminals 80 and 84):

![Diagram of armature windings with numbered elements](image)

These numbered elements could, in principle, be any suitable mechanical or electronic switch. Typically they are transistors triggered by Hall-effect sensors magnetically detecting the position of the rotor as it spins. These transistors and rotor position sensors substitute for brushes and commutator bars, closing and opening circuits to energize and de-energize coils at the appropriate times to keep the rotor spinning in the desired direction.

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Chapter 3

Historical References

This chapter is where you will find references to historical texts and technologies related to the module's topic.

Readers may wonder why historical references might be included in any modern lesson on a subject. Why dwell on old ideas and obsolete technologies? One answer to this question is that the initial discoveries and early applications of scientific principles typically present those principles in forms that are unusually easy to grasp. Anyone who first discovers a new principle must necessarily do so from a perspective of ignorance (i.e. if you truly discover something yourself, it means you must have come to that discovery with no prior knowledge of it and no hints from others knowledgeable in it), and in so doing the discoverer lacks any hindsight or advantage that might have otherwise come from a more advanced perspective. Thus, discoverers are forced to think and express themselves in less-advanced terms, and this often makes their explanations more readily accessible to others who, like the discoverer, comes to this idea with no prior knowledge. Furthermore, early discoverers often faced the daunting challenge of explaining their new and complex ideas to a naturally skeptical scientific community, and this pressure incentivized clear and compelling communication. As James Clerk Maxwell eloquently stated in the Preface to his book *A Treatise on Electricity and Magnetism* written in 1873,

> It is of great advantage to the student of any subject to read the original memoirs on that subject, for science is always most completely assimilated when it is in its nascent state... [page xi]

Furthermore, grasping the historical context of technological discoveries is important for understanding how science intersects with culture and civilization, which is ever important because new discoveries and new applications of existing discoveries will always continue to impact our lives. One will often find themselves impressed by the ingenuity of previous generations, and by the high degree of refinement to which now-obsolete technologies were once raised. There is much to learn and much inspiration to be drawn from the technological past, and to the inquisitive mind these historical references are treasures waiting to be (re)-discovered.
3.1 Transformation of industry by electric motors

Technological innovation generally occurs as an answer to practical problems. The phrase *necessity is the mother of invention* certainly explains the rise of many new technologies, as solutions to pressing needs of individuals and/or society as a whole. This is most definitely the case with electric motors. The scientific discoveries of electromagnetism and electromagnetic induction may have remained laboratory curiosities if not for the incentives of industry to employ cheaper and safer methods of transferring mechanical power to do useful work.

The following pair of photographs shows the machinery within a textile mill, in this particular case a silk-weaving factory, powered by mechanical shafts and belt drives turned by a centrally-located steam engine (left), and later powered by electric motors (right). These images were taken from the text *Electric Motors – their action, control and application* published in 1919. The contrast between these two images, in terms of mechanical complexity and employee safety alone, is stark:

![Plate A: Silk-weaving shed with belt drive.](image1)

![Plate B: The same silk-weaving shed with motor drive.](image2)

Perhaps the most obvious improvement in factory conditions resulting from the replacement of mechanical drive systems with electric is that of personnel safety. All those open belts posed significant hazard to anyone working nearby. Anyone unfortunate enough to get an article of clothing or a limb caught up in one of those moving belts faced a grim fate.
3.1. TRANSFORMATION OF INDUSTRY BY ELECTRIC MOTORS

The authors of this text presented a long list of advantages for the use of electric motor drives over mechanical shaft and belt drives, many of which are simply not apparent to anyone innocent of shaft- and belt-driven industrial environments. Given that it is highly unlikely any reader of this text will have that sort of personal experience, it is worthwhile to recount some of the advantages of electric motor drives cited by the authors of Electric Motors – their action, control and application. If nothing else, it gives a glimpse of early industrial work environments and engineering considerations:

- **Energy efficiency** – long mechanical shafts with journal bearings as well as belt drives incur substantial frictional power losses. Even considering the inefficiencies of converting a steam engine’s mechanical power to electric power (via a generator) and then back to mechanical power again (via a motor), electric drive systems still used less fuel to do the same work as mechanical drive systems!

- **Lower building cost** – structures containing belt-driven machinery needed to support the weight of driveshafts from their ceiling beams, necessitating framework capable of bearing this load. Furthermore, as structures tend to settle over time, misalignments of shafts and belts would occur as the building aged. These problems disappear entirely with electric motors.

- **Building placement** – in a mechanical-drive factory, the steam engine needed to be located immediately adjacent to the factory floor where its power would be used. This is not the case with electric drives, as the generator building could be located a considerable distance from the factory floor, with wires connecting the two.

- **Expansion** – on a similar note, factory facilities are much easier to expand with electric motor drive than with mechanical drive, since building placement and distance from the power source are no longer limited.

- **Portable machinery** – small machines such as grinders may be made portable with electric motor drives, but this is impossible with shaft- and belt-drive.

- **Clear overhead space** – the elimination of shafts from the ceiling of factory buildings made lighting much easier. This advantage is plainly visible in the comparative photographs of the silk mill before and after electric motors. It also facilitated the use of overhead cranes for maintenance and/or production work.

- **Hygiene** – one of the advantages of electric motor drives most difficult to perceive by modern readers is improved air quality and general cleanliness on the factory floor. Apparently, shaft bearings constantly dripped lubricant, and belts continually generated fine dust. Not only did this pose breathing hazards to employees, but the pall of dust and oil would contaminate the very product(s) manufactured, especially in a place such as a textile mill where the last thing you want applied to new silk is dust and oil. As an example of improved working conditions, the 1914 text cites a 40% reduction in lost employee time due to sickness at the Government Printing Office in Washington DC following the retrofit of electric motors to printing machinery. Another working condition improvement was noise reduction, as electric motors run much quieter than shafts and belts.

- **Reliability** – electric motors, even those of circa 1914, were generally more reliable than a belt drive. Furthermore, when an electric motor failed it only affected the one machine it operated,
and repairs could be made while the rest of the machinery on the factory floor continued to operate. This was not the case with machines driven from a common shaft, which had to be stopped to replace any belt along the shaft’s length.

- **Speed control** – when multiple machines are powered by a common shaft, they must all run at the same speed, or be individually equipped with transmissions allowing speed adjustment. Electric motors, on the other hand, are relatively easy to control the speed of. An interesting behavioral note made by the authors of the 1914 text is that what is convenient gets used: electric motor speed controls usually take the form of a simple knob or dial that may be turned, while shifting a mechanical transmission requires manipulation of large and cumbersome levers. Human operators were found to make frequent adjustments to electric drive speed controls in order to improve efficiency and/or production, while they would be more reluctant to do the same with clumsy mechanical speed controls. This simple fact translated to improved production with electric drives.

- **Turndown** – this refers to the ability to run only portions of a factory’s machinery after hours, during holidays, or during labor strikes. This would be inefficient in a mechanical-drive system because the (large) common steam engine would have to be run at full speed even if just one machine on the factory floor needed to operate. However, with electric drives it was possible to run a small auxiliary generator just large enough to power the reduced machinery, without having to turn the shafts of all the other machines.

As a result of these advantages, it was found that factories generally increased their production output by 20 to 30 percent following retrofit to electric motor drive.
Chapter 4

Derivations and Technical References

This chapter is where you will find mathematical derivations too detailed to include in the tutorial, and/or tables and other technical reference material.
4.1 Magnetic field quantities

A useful definition of electric field \((E)\) is in terms of the force \((F\), called the Lorentz force\) exerted on an electric charge \((Q)\) influenced by that field:

\[
\vec{F} = Q\vec{v} \times \vec{B}
\]

Where,
- \(\vec{F}\) = Force exerted on the charge (Newtons)
- \(Q\) = Charge quantity (Coulombs\(^1\))
- \(\vec{v}\) = Velocity of moving charge (meters per second)
- \(\vec{B}\) = Magnetic field (Tesla, or Newtons per Ampere-meter)

The small “arrow” symbols above the variables for force and velocity and magnetic field in the equation denote those variables as vector quantities, having both magnitude and direction. Charge is a scalar quantity having only magnitude but no direction, and as a scalar quantity when multiplied by the velocity vector it simply magnifies the magnitude but does not alter the direction. The “cross-product” \((\times)\) is a specific form of vector multiplication, and it results in a product at right angles to the vector directions of both terms. Therefore, the force and velocity and electric field vectors never all point in the same direction.

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\(^1\)One Coulomb of electric charge is equal to \(6.2415 \times 10^{18}\) electrons.
Vector cross-products conveniently relate to the fingers of the right hand, which is where the “right-hand rule” originates:

\[
C = A \times B
\]

When holding the index finger, middle finger, and thumb of your right hand perpendicular to each other, your index finger points in the direction of the velocity vector \((\vec{v})\), your middle finger in the direction of the magnetic field vector \((\vec{B})\), and your thumb in the direction of the force vector \((\vec{F})\). A simple mnemonic I use to remember these relationships of fingers to vectors is that the Index finger points in the direction of current\(^2\) \((I)\), the Middle finger points in the direction of the magnetic field \((B)\), and the Thumb points in the direction of the thrust (i.e. force) acting upon the moving charge.

The Lorentz force’s effect on electrically-charged particles in motion has many applications, from redirecting the paths of charged-particle beams in particle accelerator machines, to bending the trajectory of electron beams in a cathode-ray tube (CRT), to forcing electrons to travel in spiral or circular trajectories inside of magnetron (microwave oscillator) tubes. An illustration of a positively-charged particle curving perpendicular to a magnetic field appears here:

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\(^2\)Some textbooks speak of a “left-hand rule” which is intended to make sense of electric charge motion (current) in terms of electron flow. As we know, electrons are the only real mobile charge carriers within metal conductors, and so technically “electron flow” notation is most physically accurate when describing the motion of electric charges in metallic circuits. However, the right-hand rule is a mathematical definition for vector cross products, the concept of the cross product arising in the late 18th century when electrical science was still in its infancy. Early explorers of electricity used the established mathematical tools of their time and applied it to their work with electric currents and magnetism. At that time, charge carriers in metal wires were assumed to be “positive” and this is how the motion of positively-charged carriers became associated with the first vector of the cross-product. As a result of this assumption which was later proven false, we have two different conventions for denoting the motion of electricity: electron-flow which is physically accurate (for metal wires, at least), and conventional flow which is mathematically accurate. This, perhaps more than any other reason, is why educational programs designed for mathematically rigorous fields (e.g. electrical engineering) exclusively use conventional flow notation rather than electron flow notation to denote the direction of current.
If the moving charge in question is not a single charged particle but rather part an electric current passing through a conductor parallel to the first, both conductors will experience a mutually-attracting force given by the following equation:

\[ \vec{F} = I\vec{l} \times \vec{B} \]

Where,
- \( \vec{F} \) = Force exerted on both conductors (Newtons)
- \( I \) = Current (Amperes)
- \( \vec{l} \) = Length of wire (meters)
- \( \vec{B} \) = Magnetic field (Tesla, or Newtons per Ampere-meter)

The point-charge Lorentz force equation and the two-conductor Lorentz force equation are not that different from one another. Dimensional analysis validates this: the Lorentz force on a moving charge uses that charge quantity (Coulombs) multiplied by the point-charge’s velocity in meters per second to give Coulomb-meters per second for the first term:

\[ Q\vec{v} = \left[ \text{C} \right] \left[ \frac{\text{m}}{\text{s}} \right] = \left[ \frac{\text{C} \cdot \text{m}}{\text{s}} \right] \]

The Lorentz force on a current-carrying conductor uses the current (Amperes, which is Coulombs per second) multiplied by length in meters, for the same composite units of Coulomb-meters per second:

\[ I\vec{l} = \left[ \frac{\text{C}}{\text{s}} \right] \left[ \text{m} \right] = \left[ \frac{\text{C} \cdot \text{m}}{\text{s}} \right] \]

This dimensional equivalence makes conceptual sense as well: an electrically-charged particle moving through empty space is an electric current in its own right, and an electric current flowing through a conductor is just a collection of charged particles moving through space (just not empty space). In either case, the basis for the Lorentz force remains the same: the moving charge(s) create their own magnetic field, which reacts with the magnetic field of the original current-carrying wire to produce forces acting on both.

If the two currents flow in the same direction, their mutual forces attract. If the two currents flow in opposite directions, their mutual forces repel. This is the basis of electric motors: causing
4.1. MAGNETIC FIELD QUANTITIES

mechanical motion by electro-magnetic attraction and repulsion. It also represents an interesting contrast with electric fields:

With electric fields, opposite charges attract and like charges repel.

With magnetic fields, opposite poles attract and like poles repel.

With parallel currents, opposite directions repel and like directions attract\(^3\).

Two parallel current-carrying conductors of length \(l\) and separated by a distance \(d\) will generate a mutual force proportional to both their currents:

\[
F = \frac{l \mu I_1 I_2}{2\pi d}
\]

\(^3\)That is, assuming it’s like charges moving in these directions! If the charges in question are opposite each other, then like directions will repel and opposite directions will attract!
The circular loops surrounding the current-carrying conductors in the previous illustrations represent the magnetic lines of flux \((\Phi_B)\) surrounding each of those conductors. The magnetic field \((B)\) is related to magnetic flux by area \((A)\), the field being a measurement of how densely-packed those flux lines are per unit area:

\[
\vec{B} = \frac{\Phi_B}{A}
\]

Where,
- \(\vec{B}\) = Magnetic field (Tesla, or Webers per square meter)
- \(\Phi_B\) = Magnetic flux (Webers)
- \(A\) = Area over which flux is distributed (square meters)

An older unit of measurement for magnetic fields is the Gauss which is much smaller than a Tesla, with one Tesla equivalent to 10,000 Gauss. To put things into perspective, the Earth’s natural magnetic field has a strength of approximately one-half of one Gauss\(^4\).

Magnetic field strength is an inverse function of distance from any current-carrying wire, and also depends on the magnetic permeability of the space adjacent to the wire:

\[
B = \frac{\mu I}{2\pi d}
\]

Where,
- \(B\) = Magnetic field (Tesla, or Newtons per Ampere-meter)
- \(\mu\) = Magnetic permeability of the surrounding space (Tesla-meters per Ampere, \(4\pi \times 10^{-7}\) for empty space)
- \(I\) = Current (Amperes)
- \(d\) = Distance from conductor (meters)

\(^4\)Using the online Magnetic Field Calculator application provided by NOAA (the National Oceanic and Atmospheric Administration) at https://ngdc.noaa.gov/geomag/calculators/magcalc.shtml#igrfwmm, applying the World Magnetic Model WMM modeling algorithm for years 2019-2024, the total magnetic field strength at my home is 53,584.4 nano-Tesla (53,584.4 nT or 0.535844 Gauss), and presently (May 2020) decaying at a rate of \(-104.1\) nT per year.
4.1. MAGNETIC FIELD QUANTITIES

The relation of magnetic flux to current through a conductor follows a similar equation:

\[ \Phi = \frac{\mu AI}{2\pi d} \]

Where,
- \( \Phi \) = Magnetic flux (Webers)
- \( \mu \) = Magnetic permeability of the surrounding space (Tesla-meters per Ampere, \( 4\pi \times 10^{-7} \) for empty space)
- \( A \) = Area over which flux is distributed (square meters)
- \( I \) = Current (Amperes)
- \( d \) = Distance from conductor (meters)

As this equation makes clear, the amount of magnetic flux surrounding a current-carrying conductor depends not only on the amount of current, but also on the sampled area, the distance from the wire, and also the surrounding material. Most substances (gas, liquid, solid) have permeability values greater than that of empty space, and so this means magnetic flux is usually enhanced by the presence of matter around the current-carrying conductor.

\(^{5}\)Interestingly, superconducting materials forbid magnetic fields inside of their bulk, and so the permeability value of any superconductor must be zero!
Chapter 5

Questions

This learning module, along with all others in the ModEL collection, is designed to be used in an inverted instructional environment where students independently read\(^1\) the tutorials and attempt to answer questions on their own prior to the instructor’s interaction with them. In place of lecture\(^2\), the instructor engages with students in Socratic-style dialogue, probing and challenging their understanding of the subject matter through inquiry.

Answers are not provided for questions within this chapter, and this is by design. Solved problems may be found in the Tutorial and Derivation chapters, instead. The goal here is independence, and this requires students to be challenged in ways where others cannot think for them. Remember that you always have the tools of experimentation and computer simulation (e.g. SPICE) to explore concepts!

The following lists contain ideas for Socratic-style questions and challenges. Upon inspection, one will notice a strong theme of metacognition within these statements: they are designed to foster a regular habit of examining one’s own thoughts as a means toward clearer thinking. As such these sample questions are useful both for instructor-led discussions as well as for self-study.

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\(^1\)Technical reading is an essential academic skill for any technical practitioner to possess for the simple reason that the most comprehensive, accurate, and useful information to be found for developing technical competence is in textual form. Technical careers in general are characterized by the need for continuous learning to remain current with standards and technology, and therefore any technical practitioner who cannot read well is handicapped in their professional development. An excellent resource for educators on improving students’ reading prowess through intentional effort and strategy is the book textit{Reading For Understanding – How Reading Apprenticeship Improves Disciplinary Learning in Secondary and College Classrooms} by Ruth Schoenbach, Cynthia Greenleaf, and Lynn Murphy.

\(^2\)Lecture is popular as a teaching method because it is easy to implement: any reasonably articulate subject matter expert can talk to students, even with little preparation. However, it is also quite problematic. A good lecture always makes complicated concepts seem easier than they are, which is bad for students because it instills a false sense of confidence in their own understanding; reading and re-articulation requires more cognitive effort and serves to verify comprehension. A culture of teaching-by-lecture fosters a debilitating dependence upon direct personal instruction, whereas the challenges of modern life demand independent and critical thought made possible only by gathering information and perspectives from afar. Information presented in a lecture is ephemeral, easily lost to failures of memory and dictation; text is forever, and may be referenced at any time.
CHAPTER 5. QUESTIONS

GENERAL CHALLENGES FOLLOWING TUTORIAL READING

- **Summarize** as much of the text as you can in one paragraph of your own words. A helpful strategy is to explain ideas as you would for an intelligent child: as simple as you can without compromising too much accuracy.

- **Simplify** a particular section of the text, for example a paragraph or even a single sentence, so as to capture the same fundamental idea in fewer words.

- Where did the text **make the most sense** to you? What was it about the text’s presentation that made it clear?

- Identify where it might be easy for someone to **misunderstand the text**, and explain why you think it could be confusing.

- Identify any **new concept(s)** presented in the text, and explain in your own words.

- Identify any **familiar concept(s)** such as physical laws or principles applied or referenced in the text.

- Devise a **proof of concept** experiment demonstrating an important principle, physical law, or technical innovation represented in the text.

- Devise an experiment to **disprove** a plausible misconception.

- Did the text reveal any **misconceptions** you might have harbored? If so, describe the misconception(s) and the reason(s) why you now know them to be incorrect.

- Describe any useful **problem-solving strategies** applied in the text.

- **Devise a question** of your own to challenge a reader’s comprehension of the text.
General follow-up challenges for assigned problems

• Identify where any fundamental laws or principles apply to the solution of this problem, especially before applying any mathematical techniques.

• Devise a thought experiment to explore the characteristics of the problem scenario, applying known laws and principles to mentally model its behavior.

• Describe in detail your own strategy for solving this problem. How did you identify and organized the given information? Did you sketch any diagrams to help frame the problem?

• Is there more than one way to solve this problem? Which method seems best to you?

• Show the work you did in solving this problem, even if the solution is incomplete or incorrect.

• What would you say was the most challenging part of this problem, and why was it so?

• Was any important information missing from the problem which you had to research or recall?

• Was there any extraneous information presented within this problem? If so, what was it and why did it not matter?

• Examine someone else’s solution to identify where they applied fundamental laws or principles.

• Simplify the problem from its given form and show how to solve this simpler version of it. Examples include eliminating certain variables or conditions, altering values to simpler (usually whole) numbers, applying a limiting case (i.e. altering a variable to some extreme or ultimate value).

• For quantitative problems, identify the real-world meaning of all intermediate calculations: their units of measurement, where they fit into the scenario at hand. Annotate any diagrams or illustrations with these calculated values.

• For quantitative problems, try approaching it qualitatively instead, thinking in terms of “increase” and “decrease” rather than definite values.

• For qualitative problems, try approaching it quantitatively instead, proposing simple numerical values for the variables.

• Were there any assumptions you made while solving this problem? Would your solution change if one of those assumptions were altered?

• Identify where it would be easy for someone to go astray in attempting to solve this problem.

• Formulate your own problem based on what you learned solving this one.

General follow-up challenges for experiments or projects

• In what way(s) was this experiment or project easy to complete?

• Identify some of the challenges you faced in completing this experiment or project.
• Show how thorough documentation assisted in the completion of this experiment or project.
• Which fundamental laws or principles are key to this system’s function?
• Identify any way(s) in which one might obtain false or otherwise misleading measurements from test equipment in this system.
• What will happen if \( \text{component X} \) fails (open/shorted/etc.)?
• What would have to occur to make this system unsafe?
5.1 Conceptual reasoning

These questions are designed to stimulate your analytic and synthetic thinking. In a Socratic discussion with your instructor, the goal is for these questions to prompt an extended dialogue where assumptions are revealed, conclusions are tested, and understanding is sharpened. Your instructor may also pose additional questions based on those assigned, in order to further probe and refine your conceptual understanding.

Questions that follow are presented to challenge and probe your understanding of various concepts presented in the tutorial. These questions are intended to serve as a guide for the Socratic dialogue between yourself and the instructor. Your instructor’s task is to ensure you have a sound grasp of these concepts, and the questions contained in this document are merely a means to this end. Your instructor may, at his or her discretion, alter or substitute questions for the benefit of tailoring the discussion to each student’s needs. The only absolute requirement is that each student is challenged and assessed at a level equal to or greater than that represented by the documented questions.

It is far more important that you convey your reasoning than it is to simply convey a correct answer. For this reason, you should refrain from researching other information sources to answer questions. What matters here is that you are doing the thinking. If the answer is incorrect, your instructor will work with you to correct it through proper reasoning. A correct answer without an adequate explanation of how you derived that answer is unacceptable, as it does not aid the learning or assessment process.

You will note a conspicuous lack of answers given for these conceptual questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. The best way by far is to debate the answers with fellow students and also with the instructor during the Socratic dialogue sessions intended to be used with these learning modules. Reasoning through challenging questions with other people is an excellent tool for developing strong reasoning skills.

Another means of checking your conceptual answers, where applicable, is to use circuit simulation software to explore the effects of changes made to circuits. For example, if one of these conceptual questions challenges you to predict the effects of altering some component parameter in a circuit, you may check the validity of your work by simulating that same parameter change within software and seeing if the results agree.

3Analytical thinking involves the “disassembly” of an idea into its constituent parts, analogous to dissection. Synthetic thinking involves the “assembly” of a new idea comprised of multiple concepts, analogous to construction. Both activities are high-level cognitive skills, extremely important for effective problem-solving, necessitating frequent challenge and regular practice to fully develop.
5.1.1 Reading outline and reflections

“Reading maketh a full man; conference a ready man; and writing an exact man” – Francis Bacon

Francis Bacon’s advice is a blueprint for effective education: reading provides the learner with knowledge, writing focuses the learner’s thoughts, and critical dialogue equips the learner to confidently communicate and apply their learning. Independent acquisition and application of knowledge is a powerful skill, well worth the effort to cultivate. To this end, students should read these educational resources closely, write their own outline and reflections on the reading, and discuss in detail their findings with classmates and instructor(s). You should be able to do all of the following after reading any instructional text:

√ Briefly OUTLINE THE TEXT, as though you were writing a detailed Table of Contents. Feel free to rearrange the order if it makes more sense that way. Prepare to articulate these points in detail and to answer questions from your classmates and instructor. Outlining is a good self-test of thorough reading because you cannot outline what you have not read or do not comprehend.

√ Demonstrate ACTIVE READING STRATEGIES, including verbalizing your impressions as you read, simplifying long passages to convey the same ideas using fewer words, annotating text and illustrations with your own interpretations, working through mathematical examples shown in the text, cross-referencing passages with relevant illustrations and/or other passages, identifying problem-solving strategies applied by the author, etc. Technical reading is a special case of problem-solving, and so these strategies work precisely because they help solve any problem: paying attention to your own thoughts (metacognition), eliminating unnecessary complexities, identifying what makes sense, paying close attention to details, drawing connections between separated facts, and noting the successful strategies of others.

√ Identify IMPORTANT THEMES, especially GENERAL LAWS and PRINCIPLES, expounded in the text and express them in the simplest of terms as though you were teaching an intelligent child. This emphasizes connections between related topics and develops your ability to communicate complex ideas to anyone.

√ Form YOUR OWN QUESTIONS based on the reading, and then pose them to your instructor and classmates for their consideration. Anticipate both correct and incorrect answers, the incorrect answer(s) assuming one or more plausible misconceptions. This helps you view the subject from different perspectives to grasp it more fully.

√ Devise EXPERIMENTS to test claims presented in the reading, or to disprove misconceptions. Predict possible outcomes of these experiments, and evaluate their meanings: what result(s) would confirm, and what would constitute disproof? Running mental simulations and evaluating results is essential to scientific and diagnostic reasoning.

√ Specifically identify any points you found CONFUSING. The reason for doing this is to help diagnose misconceptions and overcome barriers to learning.
5.1. CONCEPTUAL REASONING

5.1.2 Foundational concepts

Correct analysis and diagnosis of electric circuits begins with a proper understanding of some basic concepts. The following is a list of some important concepts referenced in this module’s full tutorial. Define each of them in your own words, and be prepared to illustrate each of these concepts with a description of a practical example and/or a live demonstration.

- Energy
- Simplification as a problem-solving strategy
- Thought experiments as a problem-solving strategy
- Electrical source
- Electrical load
- Ohm’s Law
- Lenz’s Law
- Kirchhoff’s Voltage Law
- Inrush current
- Magnetic field
- Right-hand rule
- Ferromagnetism
CHAPTER 5. QUESTIONS

Electromagnetism

Electromagnetic induction

Counter-EMF

Transistor

Hall effect

Lorentz force

Direct Current (DC)

Alternating Current (AC)

Commutation

Brush

Properties of series circuits

Properties of parallel circuits
5.1.3 Dynamic braking experiment

A student is experimenting with a small PM motor one day, and discovers if they short-circuit the motor’s terminals with a piece of wire the shaft suddenly becomes very difficult to turn. Explain why this phenomenon — called *dynamic braking* — happens.

**Challenges**

- What will happen if we connect a resistor across the motor terminals rather than a direct short?
- If we couple the motor shaft to some source of mechanical energy (e.g. engine, person turning a hand crank, wind turbine, etc.), where does energy go as the motor “brakes” the prime mover’s effort?

5.1.4 Coil spring solenoid

Suppose we bent a copper wire into the shape of a coil spring. Will this coil tend to expand, collapse, or experience no inter-loop forces at all if a large amount of current passes through it?

**Challenges**

- What will happen if current reverses direction?
5.1.5 Shunt motor speed control

Compare these two methods of controlling motor speed:

Are they equivalent? Does the motor’s speed respond similarly to increases in resistance for both cases? Which might be the most practical speed-control method?

Challenges

- A more modern method of DC motor speed control relies on transistor switching elements to rapidly interrupt current to a winding, rather than inserting series resistance with a winding. The “duty cycle” of this pulsing (i.e. on-time versus total on+off time for each pulse cycle) determines the percentage of excitation for that winding. Why do you suppose this is the preferred method of speed control for a motor, rather than a variable resistance?
5.2 Quantitative reasoning

These questions are designed to stimulate your computational thinking. In a Socratic discussion with your instructor, the goal is for these questions to reveal your mathematical approach(es) to problem-solving so that good technique and sound reasoning may be reinforced. Your instructor may also pose additional questions based on those assigned, in order to observe your problem-solving firsthand.

Mental arithmetic and estimations are strongly encouraged for all calculations, because without these abilities you will be unable to readily detect errors caused by calculator misuse (e.g. keystroke errors).

You will note a conspicuous lack of answers given for these quantitative questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. My advice is to use circuit simulation software such as SPICE to check the correctness of quantitative answers. Refer to those learning modules within this collection focusing on SPICE to see worked examples which you may use directly as practice problems for your own study, and/or as templates you may modify to run your own analyses and generate your own practice problems.

Completely worked example problems found in the Tutorial may also serve as “test cases” for gaining proficiency in the use of circuit simulation software, and then once that proficiency is gained you will never need to rely on an answer key!\footnote{In other words, set up the circuit simulation software to analyze the same circuit examples found in the Tutorial. If the simulated results match the answers shown in the Tutorial, it confirms the simulation has properly run. If the simulated results disagree with the Tutorial’s answers, something has been set up incorrectly in the simulation software. Using every Tutorial as practice in this way will quickly develop proficiency in the use of circuit simulation software.}

\footnote{This approach is perfectly in keeping with the instructional philosophy of these learning modules: teaching students to be self-sufficient thinkers. Answer keys can be useful, but it is even more useful to your long-term success to have a set of tools on hand for checking your own work, because once you have left school and are on your own, there will no longer be “answer keys” available for the problems you will have to solve.}
5.2.1 Miscellaneous physical constants

Note: constants shown in **bold** type are *exact*, not approximations. Values inside of parentheses show one standard deviation (σ) of uncertainty in the final digits: for example, Avogadro’s number given as 6.02214179(30) \( \times 10^{23} \) means the center value (6.02214179\( \times 10^{23} \)) plus or minus 0.00000030 \( \times 10^{23} \).

Avogadro’s number \( (N_A) = 6.02214179(30) \times 10^{23} \) per mole (mol\(^{-1}\))

Boltzmann’s constant \( (k) = 1.3806504(24) \times 10^{-23} \) Joules per Kelvin (J/K)

Electronic charge \( (e) = 1.602176487(40) \times 10^{-19} \) Coulomb (C)

Faraday constant \( (F) = 9.64853399(24) \times 10^4 \) Coulombs per mole (C/mol)

Magnetic permeability of free space \( (\mu_0) = 1.25663706212(19) \times 10^{-6} \) Henrys per meter (H/m)

Electric permittivity of free space \( (\varepsilon_0) = 8.8541878128(13) \times 10^{-12} \) Farads per meter (F/m)

Characteristic impedance of free space \( (Z_0) = 376.730313668(57) \) Ohms (Ω)

Gravitational constant \( (G) = 6.67428(67) \times 10^{-11} \) cubic meters per kilogram-seconds squared (m\(^3\)/kg-s\(^2\))

Molar gas constant \( (R) = 8.314472(15) \) Joules per mole-Kelvin (J/mol-K) = 0.08205746(14) liters-atmospheres per mole-Kelvin

Planck constant \( (h) = 6.62606896(33) \times 10^{-34} \) joule-seconds (J-s)

Stefan-Boltzmann constant \( (\sigma) = 5.670400(40) \times 10^{-8} \) Watts per square meter-Kelvin\(^4\) (W/m\(^2\)-K\(^4\))

Speed of light in a vacuum \( (c) = 299792458 \text{ meters per second} \) (m/s) = 186282.4 miles per second (mi/s)

Note: All constants taken from NIST data “Fundamental Physical Constants – Extensive Listing”, from [http://physics.nist.gov/consta](http://physics.nist.gov/consta), National Institute of Standards and Technology (NIST), 2006; with the exception of the permeability of free space which was taken from NIST’s 2018 CODATA recommended values database.
5.2. QUANTITATIVE REASONING

5.2.2 Introduction to spreadsheets

A powerful computational tool you are encouraged to use in your work is a spreadsheet. Available on most personal computers (e.g. Microsoft Excel), spreadsheet software performs numerical calculations based on number values and formulae entered into cells of a grid. This grid is typically arranged as lettered columns and numbered rows, with each cell of the grid identified by its column/row coordinates (e.g. cell B3, cell A8). Each cell may contain a string of text, a number value, or a mathematical formula. The spreadsheet automatically updates the results of all mathematical formulae whenever the entered number values are changed. This means it is possible to set up a spreadsheet to perform a series of calculations on entered data, and those calculations will be re-done by the computer any time the data points are edited in any way.

For example, the following spreadsheet calculates average speed based on entered values of distance traveled and time elapsed:

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Distance traveled</td>
<td>46.9</td>
<td>Kilometers</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>Time elapsed</td>
<td>1.18</td>
<td>Hours</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>Average speed</td>
<td>= B1 / B2</td>
<td>km/h</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Text labels contained in cells A1 through A3 and cells C1 through C3 exist solely for readability and are not involved in any calculations. Cell B1 contains a sample distance value while cell B2 contains a sample time value. The formula for computing speed is contained in cell B3. Note how this formula begins with an “equals” symbol (=), references the values for distance and speed by lettered column and numbered row coordinates (B1 and B2), and uses a forward slash symbol for division (/). The coordinates B1 and B2 function as variables\(^6\) would in an algebraic formula.

When this spreadsheet is executed, the numerical value 39.74576 will appear in cell B3 rather than the formula = B1 / B2, because 39.74576 is the computed speed value given 46.9 kilometers traveled over a period of 1.18 hours. If a different numerical value for distance is entered into cell B1 or a different value for time is entered into cell B2, cell B3’s value will automatically update. All you need to do is set up the given values and any formulae into the spreadsheet, and the computer will do all the calculations for you.

Cell B3 may be referenced by other formulae in the spreadsheet if desired, since it is a variable just like the given values contained in B1 and B2. This means it is possible to set up an entire chain of calculations, one dependent on the result of another, in order to arrive at a final value. The arrangement of the given data and formulae need not follow any pattern on the grid, which means you may place them anywhere.

---

\(^6\)Spreadsheets may also provide means to attach text labels to cells for use as variable names (Microsoft Excel simply calls these labels “names”), but for simple spreadsheets such as those shown here it’s usually easier just to use the standard coordinate naming for each cell.
CHAPTER 5. QUESTIONS

Common arithmetic operations available for your use in a spreadsheet include the following:

- Addition (+)
- Subtraction (-)
- Multiplication (*)
- Division (/)
- Powers (^)
- Square roots (sqrt())
- Logarithms (ln(), log10())

Parentheses may be used to ensure proper order of operations within a complex formula. Consider this example of a spreadsheet implementing the quadratic formula, used to solve for roots of a polynomial expression in the form of $ax^2 + bx + c$:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th>B</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$x_{-1}$</td>
<td>$(-B4 + \text{sqrt}((B4^2) - (4<em>B3</em>B5))) / (2*B3)$</td>
</tr>
<tr>
<td>2</td>
<td>$x_{+2}$</td>
<td>$(-B4 - \text{sqrt}((B4^2) - (4<em>B3</em>B5))) / (2*B3)$</td>
</tr>
<tr>
<td>3</td>
<td>a =</td>
<td>9</td>
</tr>
<tr>
<td>4</td>
<td>b =</td>
<td>5</td>
</tr>
<tr>
<td>5</td>
<td>c =</td>
<td>-2</td>
</tr>
</tbody>
</table>

This example is configured to compute roots of the polynomial $9x^2 + 5x - 2$ because the values of 9, 5, and -2 have been inserted into cells B3, B4, and B5, respectively. Once this spreadsheet has been built, though, it may be used to calculate the roots of any second-degree polynomial expression simply by entering the new a, b, and c coefficients into cells B3 through B5. The numerical values appearing in cells B1 and B2 will be automatically updated by the computer immediately following any changes made to the coefficients.

---

7 Modern spreadsheet software offers a bewildering array of mathematical functions you may use in your computations. I recommend you consult the documentation for your particular spreadsheet for information on operations other than those listed here.

8 Spreadsheet programs, like text-based programming languages, are designed to follow standard order of operations by default. However, my personal preference is to use parentheses even where strictly unnecessary just to make it clear to any other person viewing the formula what the intended order of operations is.

9 Reviewing some algebra here, a root is a value for $x$ that yields an overall value of zero for the polynomial. For this polynomial ($9x^2 + 5x - 2$) the two roots happen to be $x = 0.269381$ and $x = -0.82494$, with these values displayed in cells B1 and B2, respectively upon execution of the spreadsheet.
Alternatively, one could break up the long quadratic formula into smaller pieces like this:

\[ y = \sqrt{b^2 - 4ac} \]
\[ z = 2a \]
\[ x = \frac{-b \pm y}{z} \]

Note how the square-root term \((y)\) is calculated in cell \(C1\), and the denominator term \((z)\) in cell \(C2\). This makes the two final formulae (in cells \(B1\) and \(B2\)) simpler to interpret. The positioning of all these cells on the grid is completely arbitrary\(^{10}\) – all that matters is that they properly reference each other in the formulæ.

Spreadsheets are particularly useful for situations where the same set of calculations representing a circuit or other system must be repeated for different initial conditions. The power of a spreadsheet is that it automates what would otherwise be a tedious set of calculations. One specific application of this is to simulate the effects of various components within a circuit failing with abnormal values (e.g., a shorted resistor simulated by making its value nearly zero; an open resistor simulated by making its value extremely large). Another application is analyzing the behavior of a circuit design given new components that are out of specification, and/or aging components experiencing drift over time.

\(^{10}\)My personal preference is to locate all the “given” data in the upper-left cells of the spreadsheet grid (each data point flanked by a sensible name in the cell to the left and units of measurement in the cell to the right as illustrated in the first distance/time spreadsheet example), sometimes coloring them in order to clearly distinguish which cells contain entered data versus which cells contain computed results from formulæ. I like to place all formulæ in cells below the given data, and try to arrange them in logical order so that anyone examining my spreadsheet will be able to figure out \textit{how} I constructed a solution. This is a general principle I believe all computer programmers should follow: \textit{document and arrange your code to make it easy for other people to learn from it.}
5.2.3 Calculating inrush current and counter-EMF

Suppose a permanent-magnet DC motor has a measured internal resistance of 2.8 Ω, including the resistance of its armature winding, brushes and brush contact with the armature, etc. When initially connected to a source it will draw a sudden “inrush” current that decreases as motor speed increases. Calculate the magnitude of this inrush current, assuming the source voltage is 18 Volts.

Next, determine the amount of counter-EMF generated by this motor as it spins at 5700 RPM (revolutions per minute) while drawing 230 milliAmperes from that same 18 Volt DC source.

Challenges

- Calculate the speed at which this motor will draw zero current.
5.3 Diagnostic reasoning

These questions are designed to stimulate your deductive and inductive thinking, where you must apply general principles to specific scenarios (deductive) and also derive conclusions about the failed circuit from specific details (inductive). In a Socratic discussion with your instructor, the goal is for these questions to reinforce your recall and use of general circuit principles and also challenge your ability to integrate multiple symptoms into a sensible explanation of what’s wrong in a circuit. Your instructor may also pose additional questions based on those assigned, in order to further challenge and sharpen your diagnostic abilities.

As always, your goal is to fully explain your analysis of each problem. Simply obtaining a correct answer is not good enough – you must also demonstrate sound reasoning in order to successfully complete the assignment. Your instructor’s responsibility is to probe and challenge your understanding of the relevant principles and analytical processes in order to ensure you have a strong foundation upon which to build further understanding.

You will note a conspicuous lack of answers given for these diagnostic questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. The best way by far is to debate the answers with fellow students and also with the instructor during the Socratic dialogue sessions intended to be used with these learning modules. Reasoning through challenging questions with other people is an excellent tool for developing strong reasoning skills.

Another means of checking your diagnostic answers, where applicable, is to use circuit simulation software to explore the effects of faults placed in circuits. For example, if one of these diagnostic questions requires that you predict the effect of an open or a short in a circuit, you may check the validity of your work by simulating that same fault (substituting a very high resistance in place of that component for an open, and substituting a very low resistance for a short) within software and seeing if the results agree.
5.3.1 Failed-open field winding

Compare and contrast the effects of the field winding failing open for each of these three DC motor types:

- Series-wound
- Shunt-wound
- Compound-wound

Explain why in each case.

Challenges

- If you could attach a speed switch to the motor’s shaft that actuates with excessive speed, how would you connect that switch’s contacts to the motor to serve as a safety device for the motor?

- If you could attach a speed switch to the motor’s shaft that actuates with insufficient speed, how would you connect that switch’s contacts to the motor to serve as a safety device for the motor?
Appendix A

Problem-Solving Strategies

The ability to solve complex problems is arguably one of the most valuable skills one can possess, and this skill is particularly important in any science-based discipline.

- **Study principles, not procedures.** Don’t be satisfied with merely knowing how to compute solutions – learn *why* those solutions work.

- **Identify** what it is you need to solve, identify all relevant data, identify all units of measurement, identify any general principles or formulae linking the given information to the solution, and then identify any “missing pieces” to a solution. **Annotate** all diagrams with this data.

- **Sketch a diagram** to help visualize the problem. When building a real system, always devise a plan for that system and analyze its function *before* constructing it.

- **Follow the units of measurement and meaning of every calculation.** If you are ever performing mathematical calculations as part of a problem-solving procedure, and you find yourself unable to apply each and every intermediate result to some aspect of the problem, it means you don’t understand what you are doing. Properly done, every mathematical result should have practical meaning for the problem, and not just be an abstract number. You should be able to identify the proper units of measurement for each and every calculated result, and show where that result fits into the problem.

- **Perform “thought experiments”** to explore the effects of different conditions for theoretical problems. When troubleshooting real systems, perform *diagnostic tests* rather than visually inspecting for faults, the best diagnostic test being the one giving you the most information about the nature and/or location of the fault with the fewest steps.

- **Simplify the problem** until the solution becomes obvious, and then use that obvious case as a model to follow in solving the more complex version of the problem.

- **Check for exceptions** to see if your solution is incorrect or incomplete. A good solution will work for *all* known conditions and criteria. A good example of this is the process of testing scientific hypotheses: the task of a scientist is not to find support for a new idea, but rather to *challenge* that new idea to see if it holds up under a battery of tests. The philosophical
principle of *reductio ad absurdum* (i.e. disproving a general idea by finding a specific case where it fails) is useful here.

- **Work “backward”** from a hypothetical solution to a new set of given conditions.
- **Add quantities** to problems that are qualitative in nature, because sometimes a little math helps illuminate the scenario.
- **Sketch graphs** illustrating how variables relate to each other. These may be quantitative (i.e. with realistic number values) or qualitative (i.e. simply showing increases and decreases).
- **Treat quantitative problems as qualitative** in order to discern the relative magnitudes and/or directions of change of the relevant variables. For example, try determining what happens if a certain variable were to increase or decrease before attempting to precisely calculate quantities: how will each of the dependent variables respond, by increasing, decreasing, or remaining the same as before?
- **Consider limiting cases.** This works especially well for qualitative problems where you need to determine which direction a variable will change. Take the given condition and magnify that condition to an extreme degree as a way of simplifying the direction of the system’s response.
- **Check your work.** This means regularly testing your conclusions to see if they make sense. This does *not* mean repeating the same steps originally used to obtain the conclusion(s), but rather to use some other means to check validity. Simply repeating procedures often leads to *repeating the same errors* if any were made, which is why alternative paths are better.
Appendix B

Instructional philosophy

“The unexamined circuit is not worth energizing” – Socrates (if he had taught electricity)

These learning modules, although useful for self-study, were designed to be used in a formal learning environment where a subject-matter expert challenges students to digest the content and exercise their critical thinking abilities in the answering of questions and in the construction and testing of working circuits.

The following principles inform the instructional and assessment philosophies embodied in these learning modules:

• The first goal of education is to enhance clear and independent thought, in order that every student reach their fullest potential in a highly complex and inter-dependent world. Robust reasoning is always more important than particulars of any subject matter, because its application is universal.

• Literacy is fundamental to independent learning and thought because text continues to be the most efficient way to communicate complex ideas over space and time. Those who cannot read with ease are limited in their ability to acquire knowledge and perspective.

• Articulate communication is fundamental to work that is complex and interdisciplinary.

• Faulty assumptions and poor reasoning are best corrected through challenge, not presentation. The rhetorical technique of reductio ad absurdum (disproving an assertion by exposing an absurdity) works well to discipline student’s minds, not only to correct the problem at hand but also to learn how to detect and correct future errors.

• Important principles should be repeatedly explored and widely applied throughout a course of study, not only to reinforce their importance and help ensure their mastery, but also to showcase the interconnectedness and utility of knowledge.
These learning modules were expressly designed to be used in an “inverted” teaching environment where students first read the introductory and tutorial chapters on their own, then individually attempt to answer the questions and construct working circuits according to the experiment and project guidelines. The instructor never lectures, but instead meets regularly with each individual student to review their progress, answer questions, identify misconceptions, and challenge the student to new depths of understanding through further questioning. Regular meetings between instructor and student should resemble a Socratic dialogue, where questions serve as scalpels to dissect topics and expose assumptions. The student passes each module only after consistently demonstrating their ability to logically analyze and correctly apply all major concepts in each question or project/experiment. The instructor must be vigilant in probing each student’s understanding to ensure they are truly reasoning and not just memorizing. This is why “Challenge” points appear throughout, as prompts for students to think deeper about topics and as starting points for instructor queries. Sometimes these challenge points require additional knowledge that hasn’t been covered in the series to answer in full. This is okay, as the major purpose of the Challenges is to stimulate analysis and synthesis on the part of each student.

The instructor must possess enough mastery of the subject matter and awareness of students' reasoning to generate their own follow-up questions to practically any student response. Even completely correct answers given by the student should be challenged by the instructor for the purpose of having students practice articulating their thoughts and defending their reasoning. Conceptual errors committed by the student should be exposed and corrected not by direct instruction, but rather by reducing the errors to an absurdity through well-chosen questions and thought experiments posed by the instructor. Becoming proficient at this style of instruction requires time and dedication, but the positive effects on critical thinking for both student and instructor are spectacular.

An inspection of these learning modules reveals certain unique characteristics. One of these is a bias toward thorough explanations in the tutorial chapters. Without a live instructor to explain concepts and applications to students, the text itself must fulfill this role. This philosophy results in lengthier explanations than what you might typically find in a textbook, each step of the reasoning process fully explained, including footnotes addressing common questions and concerns students raise while learning these concepts. Each tutorial seeks to not only explain each major concept in sufficient detail, but also to explain the logic of each concept and how each may be developed.

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1In a traditional teaching environment, students first encounter new information via lecture from an expert, and then independently apply that information via homework. In an “inverted” course of study, students first encounter new information via homework, and then independently apply that information under the scrutiny of an expert. The expert’s role in lecture is to simply explain, but the expert’s role in an inverted session is to challenge, critique, and if necessary explain where gaps in understanding still exist.

2Socrates is a figure in ancient Greek philosophy famous for his unflinching style of questioning. Although he authored no texts, he appears as a character in Plato’s many writings. The essence of Socratic philosophy is to leave no question unexamined and no point of view unchallenged. While purists may argue a topic such as electric circuits is too narrow for a true Socratic-style dialogue, I would argue that the essential thought processes involved with scientific reasoning on any topic are not far removed from the Socratic ideal, and that students of electricity and electronics would do very well to challenge assumptions, pose thought experiments, identify fallacies, and otherwise employ the arsenal of critical thinking skills modeled by Socrates.

3This rhetorical technique is known by the Latin phrase reductio ad absurdum. The concept is to expose errors by counter-example, since only one solid counter-example is necessary to disprove a universal claim. As an example of this, consider the common misconception among beginning students of electricity that voltage cannot exist without current. One way to apply reductio ad absurdum to this statement is to ask how much current passes through a fully-charged battery connected to nothing (i.e. a clear example of voltage existing without current).
from “first principles”. Again, this reflects the goal of developing clear and independent thought in students’ minds, by showing how clear and logical thought was used to forge each concept. Students benefit from witnessing a model of clear thinking in action, and these tutorials strive to be just that.

Another characteristic of these learning modules is a lack of step-by-step instructions in the Project and Experiment chapters. Unlike many modern workbooks and laboratory guides where step-by-step instructions are prescribed for each experiment, these modules take the approach that students must learn to closely read the tutorials and apply their own reasoning to identify the appropriate experimental steps. Sometimes these steps are plainly declared in the text, just not as a set of enumerated points. At other times certain steps are implied, an example being assumed competence in test equipment use where the student should not need to be told again how to use their multimeter because that was thoroughly explained in previous lessons. In some circumstances no steps are given at all, leaving the entire procedure up to the student.

This lack of prescription is not a flaw, but rather a feature. Close reading and clear thinking are foundational principles of this learning series, and in keeping with this philosophy all activities are designed to require those behaviors. Some students may find the lack of prescription frustrating, because it demands more from them than what their previous educational experiences required. This frustration should be interpreted as an unfamiliarity with autonomous thinking, a problem which must be corrected if the student is ever to become a self-directed learner and effective problem-solver. Ultimately, the need for students to read closely and think clearly is more important both in the near-term and far-term than any specific facet of the subject matter at hand. If a student takes longer than expected to complete a module because they are forced to outline, digest, and reason on their own, so be it. The future gains enjoyed by developing this mental discipline will be well worth the additional effort and delay.

Another feature of these learning modules is that they do not treat topics in isolation. Rather, important concepts are introduced early in the series, and appear repeatedly as stepping-stones toward other concepts in subsequent modules. This helps to avoid the “compartmentalization” of knowledge, demonstrating the inter-connectedness of concepts and simultaneously reinforcing them. Each module is fairly complete in itself, reserving the beginning of its tutorial to a review of foundational concepts.

This methodology of assigning text-based modules to students for digestion and then using Socratic dialogue to assess progress and hone students’ thinking was developed over a period of several years by the author with his Electronics and Instrumentation students at the two-year college level. While decidedly unconventional and sometimes even unsettling for students accustomed to a more passive lecture environment, this instructional philosophy has proven its ability to convey conceptual mastery, foster careful analysis, and enhance employability so much better than lecture that the author refuses to ever teach by lecture again.

Problems which often go undiagnosed in a lecture environment are laid bare in this “inverted” format where students must articulate and logically defend their reasoning. This, too, may be unsettling for students accustomed to lecture sessions where the instructor cannot tell for sure who comprehends and who does not, and this vulnerability necessitates sensitivity on the part of the “inverted” session instructor in order that students never feel discouraged by having their errors exposed. Everyone makes mistakes from time to time, and learning is a lifelong process! Part of the instructor’s job is to build a culture of learning among the students where errors are not seen as shameful, but rather as opportunities for progress.
To this end, instructors managing courses based on these modules should adhere to the following principles:

- Student questions are always welcome and demand thorough, honest answers. The only type of question an instructor should refuse to answer is one the student should be able to easily answer on their own. Remember, the fundamental goal of education is for each student to learn to think clearly and independently. This requires hard work on the part of the student, which no instructor should ever circumvent. Anything done to bypass the student’s responsibility to do that hard work ultimately limits that student’s potential and thereby does real harm.

- It is not only permissible, but encouraged, to answer a student’s question by asking questions in return, these follow-up questions designed to guide the student to reach a correct answer through their own reasoning.

- All student answers demand to be challenged by the instructor and/or by other students. This includes both correct and incorrect answers – the goal is to practice the articulation and defense of one’s own reasoning.

- No reading assignment is deemed complete unless and until the student demonstrates their ability to accurately summarize the major points in their own terms. Recitation of the original text is unacceptable. This is why every module contains an “Outline and reflections” question as well as a “Foundational concepts” question in the Conceptual reasoning section, to prompt reflective reading.

- No assigned question is deemed answered unless and until the student demonstrates their ability to consistently and correctly apply the concepts to variations of that question. This is why module questions typically contain multiple “Challenges” suggesting different applications of the concept(s) as well as variations on the same theme(s). Instructors are encouraged to devise as many of their own “Challenges” as they are able, in order to have a multitude of ways ready to probe students’ understanding.

- No assigned experiment or project is deemed complete unless and until the student demonstrates the task in action. If this cannot be done “live” before the instructor, video-recordings showing the demonstration are acceptable. All relevant safety precautions must be followed, all test equipment must be used correctly, and the student must be able to properly explain all results. The student must also successfully answer all Challenges presented by the instructor for that experiment or project.
Students learning from these modules would do well to abide by the following principles:

- No text should be considered fully and adequately read unless and until you can express every idea in your own words, using your own examples.

- You should always articulate your thoughts as you read the text, noting points of agreement, confusion, and epiphanies. Feel free to print the text on paper and then write your notes in the margins. Alternatively, keep a journal for your own reflections as you read. This is truly a helpful tool when digesting complicated concepts.

- Never take the easy path of highlighting or underlining important text. Instead, summarize and/or comment on the text using your own words. This actively engages your mind, allowing you to more clearly perceive points of confusion or misunderstanding on your own.

- A very helpful strategy when learning new concepts is to place yourself in the role of a teacher, if only as a mental exercise. Either explain what you have recently learned to someone else, or at least imagine yourself explaining what you have learned to someone else. The simple act of having to articulate new knowledge and skill forces you to take on a different perspective, and will help reveal weaknesses in your understanding.

- Perform each and every mathematical calculation and thought experiment shown in the text on your own, referring back to the text to see that your results agree. This may seem trivial and unnecessary, but it is critically important to ensuring you actually understand what is presented, especially when the concepts at hand are complicated and easy to misunderstand. Apply this same strategy to become proficient in the use of circuit simulation software, checking to see if your simulated results agree with the results shown in the text.

- Above all, recognize that learning is hard work, and that a certain level of frustration is unavoidable. There are times when you will struggle to grasp some of these concepts, and that struggle is a natural thing. Take heart that it will yield with persistent and varied effort, and never give up!

Students interested in using these modules for self-study will also find them beneficial, although the onus of responsibility for thoroughly reading and answering questions will of course lie with that individual alone. If a qualified instructor is not available to challenge students, a workable alternative is for students to form study groups where they challenge one another.

To high standards of education,

Tony R. Kuphaldt

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4 As the old saying goes, “Insanity is trying the same thing over and over again, expecting different results.” If you find yourself stumped by something in the text, you should attempt a different approach. Alter the thought experiment, change the mathematical parameters, do whatever you can to see the problem in a slightly different light, and then the solution will often present itself more readily.

5 Avoid the temptation to simply share answers with study partners, as this is really counter-productive to learning. Always bear in mind that the answer to any question is far less important in the long run than the method(s) used to obtain that answer. The goal of education is to empower one’s life through the improvement of clear and independent thought, literacy, expression, and various practical skills.
Appendix C

Tools used

I am indebted to the developers of many open-source software applications in the creation of these learning modules. The following is a list of these applications with some commentary on each.

You will notice a theme common to many of these applications: a bias toward code. Although I am by no means an expert programmer in any computer language, I understand and appreciate the flexibility offered by code-based applications where the user (you) enters commands into a plain ASCII text file, which the software then reads and processes to create the final output. Code-based computer applications are by their very nature extensible, while WYSIWYG (What You See Is What You Get) applications are generally limited to whatever user interface the developer makes for you.

The GNU/Linux computer operating system

There is so much to be said about Linus Torvalds’ Linux and Richard Stallman’s GNU project. First, to credit just these two individuals is to fail to do justice to the mob of passionate volunteers who contributed to make this amazing software a reality. I first learned of Linux back in 1996, and have been using this operating system on my personal computers almost exclusively since then. It is free, it is completely configurable, and it permits the continued use of highly efficient Unix applications and scripting languages (e.g. shell scripts, Makefiles, sed, awk) developed over many decades. Linux not only provided me with a powerful computing platform, but its open design served to inspire my life’s work of creating open-source educational resources.

Bram Moolenaar’s Vim text editor

Writing code for any code-based computer application requires a text editor, which may be thought of as a word processor strictly limited to outputting plain-ASCII text files. Many good text editors exist, and one’s choice of text editor seems to be a deeply personal matter within the programming world. I prefer Vim because it operates very similarly to vi which is ubiquitous on Unix/Linux operating systems, and because it may be entirely operated via keyboard (i.e. no mouse required) which makes it fast to use.
Donald Knuth’s \TeX\ typesetting system

Developed in the late 1970’s and early 1980’s by computer scientist extraordinaire Donald Knuth to typeset his multi-volume magnum opus *The Art of Computer Programming*, this software allows the production of formatted text for screen-viewing or paper printing, all by writing plain-text code to describe how the formatted text is supposed to appear. \TeX\ is not just a markup language for documents, but it is also a Turing-complete programming language in and of itself, allowing useful algorithms to be created to control the production of documents. Simply put, \TeX\ is a programmer’s approach to word processing. Since \TeX\ is controlled by code written in a plain-text file, this means anyone may read that plain-text file to see exactly how the document was created. This openness afforded by the code-based nature of \TeX\ makes it relatively easy to learn how other people have created their own \TeX\ documents. By contrast, examining a beautiful document created in a conventional WYSIWYG word processor such as Microsoft Word suggests nothing to the reader about how that document was created, or what the user might do to create something similar. As Mr. Knuth himself once quipped, conventional word processing applications should be called WYSIAYG (What You See Is All You Get).

Leslie Lamport’s \LaTeX\ extensions to \TeX\

Like all true programming languages, \TeX\ is inherently extensible. So, years after the release of \TeX\ to the public, Leslie Lamport decided to create a massive extension allowing easier compilation of book-length documents. The result was \LaTeX\, which is the markup language used to create all ModEL module documents. You could say that \TeX\ is to \LaTeX\ as C is to C++. This means it is permissible to use any and all \TeX\ commands within \LaTeX\ source code, and it all still works. Some of the features offered by \LaTeX\ that would be challenging to implement in \TeX\ include automatic index and table-of-content creation.

Tim Edwards’ \Xcircuit\ drafting program

This wonderful program is what I use to create all the schematic diagrams and illustrations (but not photographic images or mathematical plots) throughout the ModEL project. It natively outputs PostScript format which is a true vector graphic format (this is why the images do not pixellate when you zoom in for a closer view), and it is so simple to use that I have never had to read the manual! Object libraries are easy to create for \Xcircuit, being plain-text files using PostScript programming conventions. Over the years I have collected a large set of object libraries useful for drawing electrical and electronic schematics, pictorial diagrams, and other technical illustrations.
Gimp graphic image manipulation program

Essentially an open-source clone of Adobe’s PhotoShop, I use Gimp to resize, crop, and convert file formats for all of the photographic images appearing in the ModEL modules. Although Gimp does offer its own scripting language (called Script-Fu), I have never had occasion to use it. Thus, my utilization of Gimp to merely crop, resize, and convert graphic images is akin to using a sword to slice bread.

SPICE circuit simulation program

SPICE is to circuit analysis as TeX is to document creation: it is a form of markup language designed to describe a certain object to be processed in plain-ASCII text. When the plain-text “source file” is compiled by the software, it outputs the final result. More modern circuit analysis tools certainly exist, but I prefer SPICE for the following reasons: it is free, it is fast, it is reliable, and it is a fantastic tool for teaching students of electricity and electronics how to write simple code. I happen to use rather old versions of SPICE, version 2g6 being my “go to” application when I only require text-based output. NGSPICE (version 26), which is based on Berkeley SPICE version 3f5, is used when I require graphical output for such things as time-domain waveforms and Bode plots. In all SPICE example netlists I strive to use coding conventions compatible with all SPICE versions.

Andrew D. Hwang’s ePiX mathematical visualization programming library

This amazing project is a C++ library you may link to any C/C++ code for the purpose of generating PostScript graphic images of mathematical functions. As a completely free and open-source project, it does all the plotting I would otherwise use a Computer Algebra System (CAS) such as Mathematica or Maple to do. It should be said that ePiX is not a Computer Algebra System like Mathematica or Maple, but merely a mathematical visualization tool. In other words, it won’t determine integrals for you (you’ll have to implement that in your own C/C++ code!), but it can graph the results, and it does so beautifully. What I really admire about ePiX is that it is a C++ programming library, which means it builds on the existing power and toolset available with that programming language. Mr. Hwang could have probably developed his own stand-alone application for mathematical plotting, but by creating a C++ library to do the same thing he accomplished something much greater.
Another open-source tool for mathematical visualization is gnuplot. Interestingly, this tool is not part of Richard Stallman’s GNU project, its name being a coincidence. For this reason the authors prefer “gnu” not be capitalized at all to avoid confusion. This is a much “lighter-weight” alternative to a spreadsheet for plotting tabular data, and the fact that it easily outputs directly to an X11 console or a file in a number of different graphical formats (including PostScript) is very helpful. I typically set my gnuplot output format to default (X11 on my Linux PC) for quick viewing while I’m developing a visualization, then switch to PostScript file export once the visual is ready to include in the document(s) I’m writing. As with my use of Gimp to do rudimentary image editing, my use of gnuplot only scratches the surface of its capabilities, but the important points are that it’s free and that it works well.

Python programming language

Both Python and C++ find extensive use in these modules as instructional aids and exercises, but I’m listing Python here as a tool for myself because I use it almost daily as a calculator. If you open a Python interpreter console and type from math import * you can type mathematical expressions and have it return results just as you would on a hand calculator. Complex-number (i.e. phasor) arithmetic is similarly supported if you include the complex-math library (from cmath import *). Examples of this are shown in the Programming References chapter (if included) in each module. Of course, being a fully-featured programming language, Python also supports conditionals, loops, and other structures useful for calculation of quantities. Also, running in a console environment where all entries and returned values show as text in a chronologically-ordered list makes it easy to copy-and-paste those calculations to document exactly how they were performed.
Appendix D

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Appendix E

References


Mileaf, Harry, Electricity One-Seven, revised second edition, Hayden Book Company, 1996.
Appendix F

Version history

This is a list showing all significant additions, corrections, and other edits made to this learning module. Each entry is referenced by calendar date in reverse chronological order (newest version first), which appears on the front cover of every learning module for easy reference. Any contributors to this open-source document are listed here as well.

27 October 2021 – explicitly added a reference to inrush current in the Tutorial.

25 October 2021 – reversed the magnetic polarity on the first two graphical examples in the Tutorial (image_4202 and image_4203) to make them all consistent with each other.

8 May 2021 – commented out or deleted empty chapters.

21 October 2020 – minor additions to the Introduction chapter, and made a small typo correction in the Tutorial.

5 October 2020 – significantly edited the Introduction chapter to make it more suitable as a pre-study guide and to provide cues useful to instructors leading “inverted” teaching sessions.

23-24 July 2020 – wrote more content for the Tutorial chapter.

22 July 2020 – document first created.
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