Modular Electronics Learning (ModEL) project

*r SPICE ckt
v1 1 0 dc 12
v2 2 1 dc 15
i1 2 3 4700
i2 3 0 7100
dc v1 12 15 1
.print dc v(2,3)
.print dc i(v2)
.end

Multimeters

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Chapter 1

Introduction

Devices designed to provide accurate measurements of voltage, current, resistance, and other electrical quantities are called meters. Meters designed to perform more than one type of electrical measurement are called multi-function meters, or simply multimeters. In contrast to analog meters which use moving parts to express the magnitude of the measured quantity, a digital meter represents its measurement by means of a numerical display, typically a liquid-crystal display or LCD. Digital multimeters, often referred to by the acronym DMM, is perhaps the most common type of electrical test instrument in use today. Many different manufacturers produce these instruments, with a wide range of features and capabilities. This learning module will reference multiple DMM models, but will not focus on any particular brand or model. Only those features most commonly provided by DMMs will be explored. Likewise, all project and experiment ideas suggested in this learning module may be performed using any modern DMM model.

Important concepts related to electrical meters and their proper use include analog versus digital representation, the definition of voltage, the definition of current, the definition of resistance, the relationship of voltage polarity and current direction to meter indication, insertion resistance, Ohm’s Law, Joule’s Law, parallel versus series connections, polarized devices, testing an ohmmeter, meter range, analog scale reading, AC versus DC, transient events, meter resolution, electromagnetism, and overcurrent protection.

Here are some good questions to ask of yourself while studying this subject:

• How might an experiment be designed and conducted to explore the properties of series electric circuits? What hypothesis (i.e. prediction) might you pose for that experiment, and what result(s) would either support or disprove that hypothesis?

• How might an experiment be designed and conducted to explore the properties of parallel electric circuits? What hypothesis (i.e. prediction) might you pose for that experiment, and what result(s) would either support or disprove that hypothesis?

• How do analog and digital measuring instruments compare to each other?

• How exactly are voltage and current conceptually different from each other? Note that many students new to the study of electricity confuse these two concepts!
• What does “polarity” mean for a voltage?
• How much energy should a meter extract from the circuit being tested?
• What does it mean if a digital meter registers a negative value?
• Which electrical quantity(ies) is/are always measured between two points?
• Which electrical quantity(ies) is/are measurable at a single point?
• How are “clamp-on” ammeters able to sense current without making contact with the conductors?
• Why must be carefully connect voltmeters to circuits differently than we connect ammeters?
• What is *insertion resistance* and why is it important?
• What constitutes a *series* electrical connection?
• What constitutes a *parallel* electrical connection?
• What is a *polarized* electrical device?
• In what way(s) does an ohmmeter differ from a voltmeter or ammeter?
• Why must all sources of energy be disconnected from a circuit when using an ohmmeter to measure resistance?
• Which meter type poses a greater level of hazard when connecting to a circuit, and why?
• What are the challenges associated with correctly interpreting an analog meter display?
• Why do some meters have user-selectable *ranges*?
• When might you use some of the special features of a multimeter (e.g. min/max)?
2.1 Analog versus digital meters

A meter is an electrical test instrument designed to provide accurate measurement of some quantity such as voltage or current. A multimeter is a meter built with multiple functions, able to measure more than one type of electrical quantity.

Analog multimeters (also known as Volt-Ohm-Milliammeters, or VOMs) use a mechanical pointer to indicate the magnitude of the measured quantity, that pointer moved against the restraining force of a small spring by the magnetic attraction of a current-carrying wire coil. The measured circuit quantity (e.g. voltage, current) causes a small current to pass through this coil, which in turn causes the meter’s pointer (also called a needle) to deflect and point to numerical values printed on a scale. Digital multimeters (DMMs) use an electronic circuit to sense the measured quantity and represent its magnitude as a digital number value which is then scaled and displayed in numerical form for the user to see.
Hand-held models of these two types of meters are shown below for example, a Fluke model 87-III DMM on the left and a Simpson model 260 VOM on the right, both measuring a 4 Volt signal:

An analog multimeter may be switched from one measurement mode to another by means of a rotary selector switch which connects the two external test lead wires (one red, one black) to the analog meter indicator through different internal resistive networks. Each resistor network serves to “range” the multimeter so that full deflection on the meter’s face represents a different quantity of voltage, current, or resistance. Analog multimeters may be equipped with different jacks into which the test lead wires may plug, either for ranging purposes and/or for functional changes (e.g. voltage versus current).

A digital multimeter may be switched from one measurement mode to another by means of a similar selector switch (and/or a series of pushbutton switches), as well as multiple test lead jacks. There is no standard layout for multimeters, with each model being somewhat different. Some digital multimeters even have menus through which the user must navigate to select desired modes and/or features.

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1 The VOM is set to the 10 Volt range, and so the proper scale to read on the meter’s face is the one that spans 0 to 10.
2.1. ANALOG VERSUS DIGITAL METERS

Analog multimeters have a much older legacy than digital multimeters. As evidence of this, the following photograph (courtesy of NASA sometime during the 1960’s) shows an electronics technician and engineer using a Simpson model 260 analog multimeter to take measurements on an experimental ion-thrust engine intended for space probe propulsion:

Interestingly, the Simpson Electric Company still manufactures this same analog multimeter at the time of this writing (2022), and for good reason: it is an extremely versatile, accurate, and rugged instrument for its class. Digital multimeters generally enjoy superior accuracy, ruggedness, and features, but analog multimeters still excel for indicating brief pulses and subtle increases and decreases in signal strength\(^2\) of voltage or current, as well as measuring high-frequency\(^3\) AC voltage or current.

\(^2\)It is much easier for a human being to discern the transient motion of a pointer across a scale, as well as gradual increases and decreases over time, than it is to interpret periodically-updating digits.

\(^3\)Most digital multimeters “cut off” an AC frequencies within the human audio range (i.e. less than 20 kHz), but a good-quality analog multimeter is generally able to reliably measure AC voltage or current at frequencies well above human hearing with negligible error. According to the Simpson model 260-8 user manual, the frequency response in the 10 Volt AC measurement range is “flat” until approximately 80 kHz. Even at 300 kHz, the relative measurement error is no worse than (negative) one percent!
The heart of any analog meter is called its \textit{movement}: the mechanism by which the electrical quantity causes a mechanical indicator to move in response. Most analog meters use a design of movement called a \textit{permanent-magnet moving-coil (PMMC)} mechanism, where a small coil of wire pivots against the restraining force of a spring within a constant magnetic field provided by a permanent magnet. As electric current passes through that coil, it generates a magnetic field that reacts against the field created by the permanent magnet, causing the coil to rotate slightly on its axis and thereby move the pointer.

A PMMC movement with scale detached appears in this next photograph:

The laminated sheet-steel body of this movement transfers the magnetic flux from the poles of a permanent magnet (hidden from view in this photograph) to either side of a gap in which resides the moving coil. This particular coil, like most PMMC coils, is made of extremely fine-gauge copper wire, and so has the characteristic color of copper. A spiral spring (hidden from view) orients the default position of the pointer to the angle seen in the photograph. A pair of fine-gauge wires connects the moving coil to a pair of terminals on the back-side of this movement (also hidden from view) connecting either directly or indirectly to the circuit under test. Current passing through this coil in the proper direction will cause it to rotate clockwise against the magnetic flux of the sheet-steel frame, swinging the pointer clockwise as well.
2.2 Voltage, current, and resistance

In order to properly understand multimeter use, we must properly understand what it is these instruments measure. All multimeters measure (at a minimum) the following three electrical parameters, with most modern digital multimeters having the capability to measure far more:

- Voltage
- Current
- Resistance

Voltage ($V$) is defined as a difference in electrical potential, “electric potential” in turn defined as the amount of potential energy invested in an electric charge carrier. The unit of the Volt ($V$) is equal to one Joule of potential energy per Coulomb$^4$ of electric charge. A good way to conceptualize voltage is to think of it in terms of how much energy an electric charge would either gain or lose if moved from one location to another, analogous to the amount of gravitational potential energy a mass would either gain or lose if moved from one altitude to another. However we define it, an essential characteristic of voltage is that it is always relative between two points.

Current ($I$) is defined as the rate of flow of electric charge carriers through a conductive material. The unit of the Ampere ($A$) is equal to one Coulomb of electric charge passing by per second of time. Current is analogous to the flow of a gas or liquid through a pipe, the fluid molecules analogous to mobile charge carriers and the pipe analogous to a conductive wire. Unlike voltage, current can actually be specified at a single location, and in fact may be measured as such by detecting the surrounding magnetic field created by the moving charge carriers.

Resistance ($R$) is defined as the amount of voltage between two points resulting from the passage of an electric current between those points. It is defined mathematically as the quotient of voltage to current – Ohm’s Law, $R = \frac{V}{I}$. Its unit of measurement, the Ohm ($\Omega$), is equal to one Volt of voltage “drop” per Ampere of current. The measurement of resistance is similar to the measurement of voltage in that it is a quantity relative between two points.

Subsequent sections of this Tutorial will demonstrate how voltage, current, and resistance may be measured in a simple battery-resistor circuit using both analog and digital multimeters.

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$^4$One Coulomb is defined as a quantity of $6.2415 \times 10^{18}$ single electric charges (i.e. single protons or electrons).
2.3 Series versus parallel connections

Other concepts necessary for understanding multimeter use include the distinction between what are called **series** versus **parallel** connections between multiple components. These two different topologies (shapes) of circuits determine which components are guaranteed to share the same amount of electric current and which components are guaranteed to share the same amount of voltage.

When electrical components are connected together such that they form a chain providing only one path for current, they are said to be connected in **series** with each other:

- Components connected in series with each other must share the same amount of current at any given time, because the electric charge carriers have only one path to travel. Since charge carriers are conserved (i.e. cannot be created or destroyed), they must move along this single path at the same rate, just like the mass flow rate of water in a river is the same at any point along any unbranching section of it because mass is also conserved.

If we view a meter as a component, then connecting a meter in series with another component guarantees the meter will sense the same amount of current that passes through that component. Thus, **we always connect ammeters in series with the component whose current we wish to measure**.
2.3. SERIES VERSUS PARALLEL CONNECTIONS

When electrical components are connected together such that they span the same two sets of conductors, we say they are connected in parallel with each other:

![Diagram of parallel-connected components]

Points directly connected together by negligible resistance are electrically common to one another, and the absence of resistance between those points ensures charge carriers don’t lose any energy traveling between. Thus, electrically common points must be equipotential.

This equipotentiality explains the behavior of parallel-connected components. Referencing the above diagram, if charge carriers at points A through D all exist at the same potential energy level, and charge carriers at points E through H likewise all exist at the same potential energy level, then the difference of potential between any point A-D and any point E-H (e.g. from A to E, from D to H, from B to G, etc.) must be the same. Therefore voltage across every component in a parallel network is the same.

Viewing a meter as a component, if we connect a meter in parallel with another component it guarantees the meter will sense the same amount of voltage as that other component. Thus, we always connect voltmeters in parallel with the component whose voltage we wish to measure.
2.4 Measuring voltage

Here we see a VOM configured as a voltmeter, used to measure voltage across resistor $R_3$ in a three-resistor circuit:

First, note how the meter’s test leads touch the resistor’s terminals, placing the meter in parallel with the resistor. A “parallel” network is defined as one having exactly two sets of electrically common points, with all components connected between those them. Touching the red test lead to the top of $R_3$ makes the “+” jack of the VOM electrically common to the top of $R_3$, while touching the black test lead to the bottom of $R_3$ make the “COMMON −” jack of the meter electrically common to the bottom of $R_3$. Parallel connections ensure components share the same voltage, and with any voltage measurement our goal is for the meter to experience the exact same voltage as the component whose voltage we are interested in measuring.

Note also how we must respect the polarity (+, −) of the measured voltage when connecting our meter to any direct-current (DC) circuit. The terminal of the resistor we expect to be at a greater potential (+) is the one we touch with the red probe, while the black probe touches the terminal at lower potential (−). Correct polarity is very important when using a VOM to measure voltage because this is necessary to drive the meter’s pointer up the scale (clockwise rotation). Connecting the voltmeter backwards would drive the pointer in the other direction, forcing it against the left-hand stop. The particular VOM shown in this illustration is modeled after a Simpson 260, which has a polarity-reversing switch intended to reverse the roles of red and black test leads in case of

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5This is commonly referred to as pegging the pointer, because the mechanical stops on an analog meter movement usually consist of small metal pegs.
accidental “backwards” connection. Normally one simply reverses the placement of the two test leads upon discovering a backwards connection, but the polarity-reversing switch is useful whenever the test leads are clamped in place (e.g. when secured by terminal blocks for semi-permanent connection to the circuit).

An illustration showing the effect of connecting a VOM “backwards” appears below:

The purpose of any test instrument is to merely measure and not to influence whatever’s being measured, and for an electrical meter this means extracting as little energy as possible from the circuit. For a voltmeter this means drawing as little current away from the circuit as possible, and this necessitates the voltmeter having a very high resistance between its test leads. For a good-quality VOM this insertion resistance will be tens or hundreds of thousands of Ohms depending on the voltage-measuring range selected. DMMs configured as voltmeters generally have insertion resistance values in the tens of millions of Ohms for even better performance. An ideal voltmeter has infinite insertion resistance\(^6\) (i.e. an ideal voltmeter behaves as an electrical open).

\(^6\)Interestingly, there is such a thing as a voltmeter that dissipates zero energy in steady-state conditions, and that is the electrostatic voltmeter which operates by sensing the invisible electric field existing between two conductors having a voltage between them. Unfortunately, these instruments are only practical for high voltages, usually in the kilo-Volt range, and so are all but unusable in most circumstances.
Using a DMM to measure $R_3$’s voltage is not much different from using the VOM. We must select the proper function on the meter’s switch, ensure the test plugs are inserted into the correct jacks on the meter’s face, and once again connect the meter in parallel with the component:

Since we are intending to measure voltage in a DC circuit, we must choose the “V” function with the two parallel lines (one solid, one dashed). The wavy-curve symbol above the other “V” represents alternating-current (AC) voltage measurement.

As mentioned previously, DMMs typically exhibit far greater insertion resistance as voltmeters than VOMs, and this results in less energy being extracted from the circuit under test. This allows the circuit to function nearer to its un-measured state when the meter is connected to it, resulting in more realistic measurements. For many electric circuits such as power systems this distinction is irrelevant because either multimeter type dissipates a trivial amount of power compared to the circuit’s normal operating load. However, for sensitive electronic circuits where the power levels are much smaller it is often best to use a DMM rather than a VOM to measure voltage$^7$.

DMMs are also easier for novices to use because their displays require no interpretation. A VOM’s pointer usually does not fall exactly on one of the scale’s division-marks, and so one must read the division markings carefully to interpret the numerical value represented by the pointer’s position. Digital displays require no skill to read, being simply a decimal number.

$^7$An interesting exception to this rule is when the VOM in question is a Vacuum-Tube VoltMeter or VTVM. These instruments used electromagnetic meter movements just like VOMs, but incorporated an electronic amplifier circuit to effectively isolate the meter movement’s energy demand from the circuit under test.
2.4. **MEASURING VOLTAGE**

If we happen to connect the DMM’s test leads backwards to $R_3$, the only difference we will notice is that the digital display will be preceded by a negative sign:

Unlike most VOMs where the indicating pointer’s “zero” position is biased toward one side of the scale, a DMM’s display knows no such limits. Correct-polarity measurements generate positively-signed results and backward-polarity measurements negatively-signed results. Most users of multimeters consider this to be an advantage, not having to pay attention to correct polarity when connecting a meter to a circuit.
2.5 Measuring current

Current, unlike voltage, actually does have meaning at any single point in an electric circuit. With a magnetic clamp-on ammeter we may infer how much current is passing through the wire by sensing the strength of the magnetic field encircling the wire at that point, magnetic field strength being directly proportional to current. A photograph of a Wavetek “Meterman” model clamp-on ammeter appears below, the jaws of the meter’s clamp mechanism being held open by depressing a lever with my thumb:

![Magnetometer](image)

However, for any electric current less than a few Amperes the magnetic field produced by the moving charge carriers is weaker than that of the Earth’s natural magnetic field\(^8\), and therefore accurate measurements of current based on measuring magnetism are impractical for such circuits. For most electronic circuit work, a direct-connection meter such as a VOM or DMM is far superior to a magnetic clamp-on instrument for measuring current.

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\(^8\)A wire carrying a current of 3 Amperes produces a magnetic field of 60,000 nano-Teslas at one centimeter away from the wire. By contrast, the Earth’s magnetic field is approximately 53,000 nano-Teslas in strength.
2.5. MEASURING CURRENT

Below we see an illustration of a VOM being used as an ammeter to measure current through resistor $R_2$ in a circuit:

Whereas a voltmeter’s test leads must connect in parallel with the component whose voltage is to be measured, an ammeters test leads must connect in series with the component whose current is to be measured. These series/parallel relationships are fundamental to the measured quantity: parallel connection guarantees equal voltage, while series connection guarantees equal current. Therefore, in order to connect this VOM as an ammeter for resistor $R_2$, we needed to disconnect one of the wires on $R_2$ and place the ammeter within the circuit to complete that broken path. In other words, we connect an ammeter in such a way that current through the component of interest must flow through the meter.

This is problematic for multiple reasons. First and foremost, the need to alter the circuit’s wired connections in order to insert our ammeter may pose a safety hazard. A voltmeter may be connected to a “live” circuit with little risk, since the meter draws negligible current and the test probe handles are well-insulated to guard against accidental skin contact with the circuit. However, to alter a circuit’s normal wiring requires direct contact between you and the circuit, and so usually this means we must de-energize the circuit for safety.\footnote{When I teach laboratory classes I insist that students always de-energize a circuit prior to making bodily contact with it. Even on low-voltage, low-power circuits where the risk of electric shock and arc flash are nonexistent, it is well-worth building the good habit of never touching a live circuit with your skin. I have seen far too many cases where students develop a cavalier attitude because they become accustomed to touching their safe breadboarded circuits, and then one day they find themselves working on a circuit with dangerous levels of voltage and/or current without considering the safety risks! Human beings are creatures of habit, which is why good habits should be practiced at all times in a field where a simple mistake on the wrong circuit can spell the difference between life and death.}
Inserting an ammeter into a circuit is also problematic due to the risk of faulting that circuit when we remove the ammeter and re-connect the disconnected conductors. Should we happen to re-connect the wires poorly, or even connect one to a different location than before, we will have unintentionally altered the circuit. This sort of circuit alteration cannot happen when taking a voltage measurement requiring no disconnecting of conductors. For these reasons, when doing routine work or diagnostic troubleshooting on circuits, we generally prefer to avoid current measurements where possible and try to get the information we need from voltage measurements instead.

As mentioned previously, the purpose of any test instrument is to measure and not to influence the circuit being tested. For an electrical meter this means extracting as little energy as possible from the circuit under test, and for ammeters this means dropping as little voltage as possible so that charge carriers passing through lose negligible energy. Therefore, ammeters must exhibit very low resistance between their test leads, ideally zero\(^{10}\) (i.e. an ideal ammeter behaves as an electrical short).

In direct-current (DC) circuits, polarity matters for ammeters just as it does for voltmeters. Note how in order to drive the VOM's pointer up-scale (to the right), we had to connect it such that current\(^{11}\) entered the red test lead and exited the black test lead. If we swap red and black leads, the VOM’s pointer will “peg” down-scale as it did when we applied reverse polarity in voltage-measuring mode:

\(^{10}\)Magnetic clamp-on ammeters approach this ideal, since they operate by sensing the magnetic field surrounding the wire. Unfortunately, the low sensitivity of magnetic clamp-on ammeters makes them unsuitable for use in low-power circuits where we most care about insertion resistance.

\(^{11}\)We are assuming the use of “conventional” flow notation rather than “electron” flow notation unless otherwise specified.
Measuring current with a DMM configured to be an ammeter usually requires we plug the red test lead into a different jack on the meter’s face, as shown below:

If you look closely at the labels near the DMM current jacks, you will see that the meter has fuses built-in to protect against overcurrent. In this case, the fuse has a 400 mA rating, and will “blow” open in the event more than that much current passes through. This is an important safety feature for any ammeter, given the meter’s low insertion resistance. If someone were to leave the meter in its current-measuring mode and then forgetfully connect it in parallel with a voltage source to measure voltage, the meter will present a short-circuit to that source. Depending on how much electrical resistance is contained inside the source, the fault current through the mis-connected ammeter may be very high indeed. Without overcurrent protection, this could damage the meter and perhaps even endanger the person holding the meter! Overcurrent protection is not necessary for voltmeters, because voltmeters have high insertion resistance by design, and so self-limit current to a negligibly safe value.

A safety feature of some DMMs is an audio warning beeper that sounds whenever a test plug is inserted into one of the current-measuring jacks and the selector switch is set to measure voltage. When people forget to switch the DMM from current-measuring mode to voltage-measuring mode, it is usually the red test lead plug they forget to move into the correct jack. If someone leaves the plug inserted in the current-measuring jack and moves the selector switch to a voltage-measuring position, the meter beeps until the error is corrected.
Reversing polarity merely causes the DMM to display a negative current value:

2.6 Measuring resistance

Electrical resistance is any form of energy dissipation – usually in the form of heat – resulting from the movement of charge carriers from one location to another. The mechanism of energy loss usually takes the form of collisions between the mobile charge carriers and stationary atoms within the conductive material. Both VOMs and DMMs are capable of resistance measurement, and they do so by applying their own current to the device under test using a battery internal to the meter as the energy source. This means the device whose resistance is to be measured must be completely de-energized before testing its resistance with a meter! If any other electrical source is forcing current through the device, that current will interfere with the meter’s own current, and the result (at best) will be meaningless measurements.

A good precautionary step to take prior to measuring the resistance of any component you suspect may be energized is to first configure the multimeter for voltage measurement, and use it to verify the complete and total absence of voltage across that component.
This next illustration shows a VOM measuring the resistance of resistor $R_1$:

Notice how two wires needed to be disconnected in order to successfully measure $R_1$’s resistance in this circuit: we needed to disconnect one of the wires going to the battery (either one), and we also had to disconnect one of the wires that formerly connected $R_1$ and $R_2$ in parallel with each other (either one). If we consider the multimeter to be an electrical source in its resistance-measuring mode, we need to ensure that current exiting one test probe and entering the other only flows through the component of interest and through no others. In this case, you can see that between the red and black test probes, the one and only path for current is through $R_1$. If the battery had remained connected, its current would have interfered with the multimeter’s and yielded a meaningless result. If $R_2$ had remained connected in parallel with $R_1$, the multimeter’s test current would have passed through both $R_1$ and $R_2$ as a parallel network and given a measurement equal to that parallel equivalence, and not of $R_1$’s resistance alone.
The requirement of electrically isolating a path through just the component of interest is fundamental to resistance measurement regardless of the type of multimeter used. Therefore, a DMM would need to be connected to \( R_1 \) in a similar manner, and for the exact same reasons, as a VOM. The next illustration shows an alternative disconnection scheme for isolating \( R_1 \), with either scheme suitable for either VOM or DMM:

Meter polarity is irrelevant when measuring resistance of devices such as resistors, which present the same amount of energy dissipation for currents moving in either direction. Polarized devices such as diodes, though, will register differently depending on which way the meter’s red and black test leads connect to the device’s terminals. One should never obtain a negative resistance measurement from a DMM, nor experience the pointer on a VOM “peg” down-scale, when measuring resistance. If this ever happens, it is a sure sign that the component is being energized by some other source!
2.6. MEASURING RESISTANCE

A good self-test to perform with a DMM prior to measuring resistance – and essential for a VOM prior to taking any resistance measurement – is to touch the two test probes directly together before contacting the circuit. The meter should register very nearly zero, and in fact the only resistance it should register in this “shorted” condition is the resistance of the test leads and plugs themselves, which should be a small fraction of an Ohm. All VOMs have a knob or other adjustment provided to “zero” the resistance-measuring function prior to use on a real component:

VOM resistance scales are read in reverse direction compared to voltage and current: for $V$ or $I$ zero is found on the left-hand end of the scale, but for $R$ zero is found at the far right. The reason for this is that VOM meter movements are essentially sensitive ammeters, and so pointer deflection in the clockwise direction is always the result of current passing through the meter movement’s fine wire coil. When configured as an ammeter, the VOM’s movement current is usually some precise fraction of the measured value. When configured as a voltmeter, current through the VOM’s meter movement is the inevitable flow of charge carriers necessary for the meter to function, and this too increases with increasing measured voltage. When configured as an ohmmeter, it is less resistance that results in more current through the movement given the meter’s internal battery voltage (Ohm’s Law, $I = \frac{V}{R}$), and so minimum resistance drives the pointer toward the right-hand end of the scale while maximum resistance (an “open” condition) results in the pointer remaining at its resting position at the far-left end of the scale.
2.7 Ranges and scales

When we examine the face of a VOM (in this case a Simpson model 260), we see multiple scales printed on a white background, the pointer showing us the measured value depending on which scale and function the VOM is configured for:

![Image of a VOM face]

In this photograph we see the red-colored pointer at the far-left end of all the scales, registering zero for any voltage or current function, and infinite for resistance. If we examine the selector switch on the VOM’s face we will notice that every voltage and current function has a maximum value associated with it, and that this maximum value corresponds to the significant figures\(^{12}\) of the right-most numerical value on at least one scale:

![Image of a VOM selector switch]

\(^{12}\)Note, for example, how the 250 V, 50 V, and 10 V switch positions relate to the 250, 50, and 10 DC scales, respectively. However, there is no “100” scale for the 100 MA switch position, nor is there a “500” scale for the 500 MA switch position. In such cases the user is expected to interpret whichever scale has the same significant (i.e. non-zero) digits as the correct scale. For example, when the switch is set to any range ending in “500”, you must read along the “50” scale and mentally multiply the indicated scale value by ten. Likewise, for any range ending in “1”, you must read along the “10” scale and mentally divide the indicated scale value by ten.
For example, consider the following photograph taken of this same VOM while measuring an electrical signal:

![Image of a multimeter]

Our interpretation of the pointer’s position depends entirely on this meter’s range. The following list provides different range settings for this meter along with the corresponding interpretation of the pointer’s position. Note how all DC measurements are read on the black-colored scales, while AC measurements use the red-colored scales:

- 1 Volt DC range = 0.35 V DC, as read on the black 0-10 scale
- 2.5 Volt AC range = 0.95 V AC, as read on the dedicated lower red 0-2.5 Volt AC scale
- 50 Volt DC range = 17.5 V DC, as read on the black 0-50 scale
- 250 Volt AC range = 87.5 V AC, as read on the upper red 0-250 scale
- 10 milliAmpere DC range = 3.5 mA DC, as read on the black 0-10 scale
- 500 milliAmpere AC range = 181 mA AC, as read on the upper red 0-50 scale
- R × 1 Ohms range = 22 Ω, as read on the top black scale
- R × 100 Ohms range = 2.2 kΩ, as read on the top black scale

Having multiple ranges for a VOM makes sense because the scale-and-pointer display mechanism has limited resolution. A small range (e.g. 0 to 1 Volt or 0 to 1 mA for a full sweep of the pointer) would be useless measuring larger quantities, but a large range (e.g. 0 to 1000 Volts) would be equally useless for measuring modest quantities because the pointer would not move enough to be able to accurately discern the value. Clearly, to obtain good readability from a mechanical meter movement with limited sweep we need the ability to “shift gears” by switching to different measurement ranges.

13This too, is a helpful analogy for understanding the dilemma. Automobiles must have transmissions providing different gear ratios to match the internal combustion engine’s limited speed range with the various road speeds required for driving. Bicycles must provide different chain-and-sprocket ratios for the same reason, to match desired road speed with optimum pedaling speed (cadence). Selecting different measurement ranges on a multimeter is analogous to “shifting gears” in an automobile or bicycle.
Interestingly, the exact same principle applies to digital multimeters as well as analog. The "analog-to-digital converter" circuit inside of a DMM converting the measured voltage or current signal into a numerical value also has limited resolution, just as an analog meter movement has limited range of pointer motion. In order to be able to measure both small and large quantities with a DMM, it must have multiple range settings to appropriately match the signal strength to the converter circuit's capabilities.

Low-end DMMs have selector switches just like VOMs to choose the best range for the measurement task at hand. Higher-quality DMMs, though, provide a feature called *auto-ranging* where the meter chooses its own range to suit the signal magnitude, much like an automobile with an automatic transmission selects the best gear ratio to match the engine's speed with the car's road speed. Even then, auto-ranging DMMs provide the user with the ability to manually set the range, as it may be troublesome to wait for the meter to select the appropriate range while the measured signal fluctuates.

When a DMM's range switches, you will notice the decimal point shift positions on the meter's display. For example, on a three-digit DMM display you may see no decimal point on the highest range (XXX), and a decimal point position that shifts to the left with each step down in range (e.g. XX.X, followed by X.X).

If a DMM is "over-ranged" by a signal exceeding its range limits, it generally displays "OL" which is the digital equivalent of an analog meter's pointer "pegging" fully upscale. When using a manually-ranged multimeter, whether DMM or VOM, it is best to begin with the meter's range set for the highest value when first connecting the test leads to the circuit, to help avoid the possibility of damage if the signal is stronger than anticipated. If this initial range value proves too large, you can always "downshift" the meter to a lower range until a good-resolution measurement appears.

### 2.8 Other measurements

Modern DMMs provide many measurement capabilities beyond voltage, current, and resistance. These include some of the following, limited only by the manufacturer's abilities and meter pricing:

- Semiconductor junction forward voltage drop ($V_f$, measured in Volts)
- AC voltage or current frequency ($f$, measured in Hertz)
- Conductance ($G$, measured in Siemens)
- Pulse duty cycle (%)
- Capacitance ($C$, measured in Farads)

The best resource for learning how to use all the “extra” measurement functions available on a DMM is the user’s manual for that meter. These are generally well-written and highly valuable.

### 2.9 Useful features

In addition to being able to measure multiple parameters in circuits, multimeters often provide additional features useful on some or all of the measurement functions. These features vary widely from model to model, but some of the more common features are listed here in subsections.
2.9. USEFUL FEATURES

2.9.1 Discriminating AC from DC measurements

Most digital multimeters discriminate well between AC and DC quantities. That is to say, when configured for DC measurement they tend to ignore any “ripple” or other time-variations in the signal and present just the DC average value of that signal. Conversely, when configured for AC measurement they filter out any DC “bias” and show only the time-varying or “rippling” portion of the signal. This is a very useful feature when measuring mixed DC+AC signals, either voltage or current: you may switch the DMM between its DC and AC measuring modes to see how much DC and AC are present in that signal.

VOMs do not naturally discriminate at all on the basis of AC versus DC because electromagnetic meter movements naturally respond to any applied electrical stimulus: DC causes the pointer to move in one direction while AC causes the pointer to wiggle back and forth. If a mixed DC+AC signal is measured by a VOM in its DC mode, the pointer’s average position will equal the DC value while the AC portion of the signal attempts to oscillate the pointer back and forth. For low frequencies this oscillation is visible, and at high frequencies it is not. However, even at low frequencies the pointer usually cannot keep up with the AC signal’s frequency, and so the peak-to-peak oscillation you see in the pointer’s tip does not represent the full peak-to-peak span of the signal.

When a VOM is set to measure AC, the signal gets routed through a rectifying network to convert AC into DC so that the movement will only drive the pointer in one direction. This doesn’t help much for a mixed DC+AC signal because the meter’s calibration usually differs slightly between AC and DC owing to the voltage drops of the rectifying network. The AC portion of the mixed AC+DC signal will drive the pointer as it should, but the DC portion’s effect on the pointer will be out of calibration.

Some higher-end VOMs do provide an AC-only voltage measurement feature in the form of an Output jack. This is an alternate jack position for the red test lead plug, connecting the red test lead to the rest of the meter’s internal circuitry through a capacitor which blocks the DC portion of the signal so that the meter only registers the AC portion. To use this, you simply configure the VOM to measure AC voltage at the appropriate range and move the red plug from its regular position to the Output jack. This jack is called “Output” because it was designed for use when measuring the signal output by an audio-frequency amplifier circuit, the meter’s internal capacitor sized to pose negligible impedance to the signal compared to the rest of the meter’s insertion resistance in the AC mode.

2.9.2 Min/Max mode

A feature common to many DMMs is Minimum/Maximum capture. This feature, useful in all measurement modes, retains a record of the highest and lowest signal values sensed after the Min/Max feature is engaged. Some meters also provide a mathematical average of the signal values over time since the Min/Max feature’s engagement.

Min/Max mode is extremely useful when you must leave the multimeter unattended while working at some other location. It is also useful for capturing transient events too quick to show on the meter’s display, though the time resolution of Min/Max does have limits. An example of using Min/Max mode in this capacity is the measurement of motor inrush current during the start-up of an electric motor.
2.9.3 Relative mode

This DMM feature is analogous to the “tare” function on a weigh-scale, where the sensed weight of an empty container sitting on the scale bed may be “zeroed out” to make the scale register only the weight of the contents placed into the container rather than the combined weight of the container and contents. A DMM equipped with this feature will “re-set” its display to zero in any measurement mode upon pressing the “Relative” button.

One common application of a DMM’s “Relative” mode is compensating for test lead resistance prior to making a low-resistance measurement. After configuring the DMM to measure resistance, you touch the two test probes together to create a “shorted” condition and press “Relative” to make the meter register zero in this state. This way, any test lead resistance will be canceled, so that when the test probes contact the device in question the meter only registers that device’s resistance.

Interestingly, VOMs already have this feature built-in as an essential part of their resistance-measuring functionality. Due to the fact that VOMs use an internal battery with unstable voltage to perform resistance measurement, self-calibration of the VOM’s resistance scale is necessary with every use. However, this zero-adjust VOM feature only works for resistance measurement, while the “Relative” feature on a DMM works on any function (e.g. voltage, current, resistance, frequency, etc.).

2.9.4 Hold mode

Another common DMM feature is the “Hold” mode, where a button exists for the purpose of “freezing” a displayed value even when the actual signal value changes.

Some specialized analog meters provided a mechanical equivalent to this in the form of a finger-operated “clutch” that would secure the movement’s pointer in its last position. For example, an analog clamp-on ammeter may be equipped with such a clutch so that the unit may be positioned awkwardly to sense current through the wire, the pointer’s position secured by the clutch mechanism with the pointer still out of view, and then when the unit returns to an easily-viewed position it is possible to read the pointer’s position.

2.9.5 High resolution mode

The measurement resolution of a DMM may be extended by exploiting a fundamental principle of data acquisition, which is that additional resolution may be gained from a measurement by successive oversampling of a signal over longer periods of time. The idea is quite simple: by taking successive samples of a signal and computing the mathematical average of those samples, it is possible to discern signal values lying between the resolution intervals permitted by the sampling circuitry. For example, if you monitored a digital voltmeter display over four successive samples and saw that it read 5.87 Volts, 5.88 Volts, 5.87 Volts, and 5.88 Volts, you could average these to obtain 5.875 Volts (half-way in between 5.87 and 5.88) because two of the samples read 5.87 while the other two read 5.88. The real voltage must be between those two values, and the fact the meter spent half its time on one value and half on the other is good evidence\(^\text{14}\) that the true value lies at or very close to the middle. A DMM with high-resolution mode does this oversampling and averaging for you.

\(^\text{14}\)This is not strictly true for all forms of analog-digital conversion, but for the most common types used in precision measurement it is.
2.9. USEFUL FEATURES

When switched into high-resolution mode, the DMM’s update speed will become noticeably slower, and you will generally see an additional digit appear on the meter’s display.

No such feature exists for analog multimeters (VOMs), because the theoretical resolution of any analog device is infinite. Unlike a digital system where all values are represented by discrete steps, an analog system is inherently continuous. All the resolution you will ever need is already there in the analog system’s indication, if only you have eyes good enough to see it!

Some precision analog meters employ magnifying lenses to permit closer viewing of the pointer’s position along the scale. This, of course, requires a scale with ever-finer divisions marking the numerical values along it. Another feature of high-precision analog meter movements is a mirrored scale where a reflective mirror strip is laid parallel to the scale arcs, allowing the user to orient the meter (or their head) so that the pointer’s reflection aligns with the pointer itself to ensure no parallax error\(^\text{15}\).

In the photograph shown below you can see how the pointer’s reflection in the mirrored arc does not align with the pointer itself, indicating to the user that their eye is out of alignment with the meter’s face:

![Photograph of an analog meter with a mirrored scale](image)

Interestingly, a very old analog meter technology called a mirror galvanometer substituted a mirror and a beam of light for the pointer and scale of the usual electromagnetic meter movement. The concept of a mirror galvanometer was to shine a beam of light at the meter movement’s mirror, with the reflected beam acting as a massless pointer of arbitrary length. With this device, resolution was limited only by the dimensions of the darkened room used to show the light beam’s angle on a far wall!

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\(^{15}\)Parallax error is the error resulting from looking at a pointer from an angle, and seeing its position (falsely) at some other point along the scale due to the inevitable gap between the pointer tip and the scale face.
Chapter 3

Derivations and Technical References

This chapter is where you will find mathematical derivations too detailed to include in the tutorial, and/or tables and other technical reference material.
CHAPTER 3. DERIVATIONS AND TECHNICAL REFERENCES

3.1 Helpful “tricks” using a digital multimeter (DMM)

The digital multimeter (DMM) is quite possibly the most useful tool in the electronic technician’s collection\(^1\). This one piece of test equipment, properly wielded, yields valuable insight into the status and operation of many electrical and electronic systems. Not only is a good-quality multimeter capable of precisely indicating electrical voltage, current, and resistance, but it is also useful for more advanced tests. The subject of this section is how to use a digital multimeter for some of these advanced tests\(^2\).

For all these tests, I suggest the use of a top-quality field multimeter. I am personally a great fan of Fluke brand meters, having used this particular brand for nearly my whole professional career. The ability of these multimeters to accurately measure true RMS amplitude, discriminate between AC and DC signals, measure AC signals over a wide frequency range, and survive abuse both mechanical and electrical, is outstanding.

3.1.1 Recording unattended measurements

Many modern multimeters have a feature that records the highest and lowest measurements sensed during the duration of a test. On Fluke brand multimeters, this is called the Min/Max function. This feature is extremely useful when diagnosing intermittent problems, where the relevant voltages or currents indicating or causing the problem are not persistent, but rather come and go. Many times I have used this feature to monitor a signal with an intermittent “glitch,” while I attended to other tasks.

The most basic high-low capture function on a multimeter only tells you what the highest and lowest measured readings were during the test interval (and that only within the meter’s scan time – it is possible for a very brief transient signal to go undetected by the meter if its duration is less than the meter’s scan time). More advanced multimeters actually log the time when an event occurs, which is obviously a more useful feature. If your tool budget can support a digital multimeter with “logging” capability, spend the extra money and take the time to learn how this feature works!

\(^1\) As a child, I often watched episodes of the American science-fiction television show Star Trek, in which the characters made frequent use of a diagnostic tool called a tricorder. Week after week the protagonists of this show would avoid trouble and solve problems using this nifty device. The sonic screwdriver was a similar tool in the British science-fiction television show Doctor Who. Little did I realize while growing up that my career would make just as frequent use of another diagnostic tool: the electrical multimeter.

\(^2\) I honestly considered naming this section “Stupid Multimeter Tricks,” but changed my mind when I realized how confusing this could be for some of my readers not familiar with colloquial American English.
3.1. HELPFUL “TRICKS” USING A DIGITAL MULTIMETER (DMM)

3.1.2 Avoiding “phantom” voltage readings

My first “trick” is not a feature of a high-quality DMM so much as it is a solution to a common problem caused by the use of a high-quality DMM. Most digital multimeters exhibit very high input impedance in their voltage-measuring modes. This is commendable, as an ideal voltmeter should have infinite input impedance (so as to not “load” the voltage signal it measures). However, in industrial applications, this high input impedance may cause the meter to register the presence of voltage where none should rightfully appear.

Consider the case of testing for the absence of AC voltage on an isolated power conductor that happens to lie near other (energized) AC power conductors within a long run of conduit:

With the power switch feeding wire 5 in the open state, there should be no AC voltage measured between wire 5 and neutral (L2), yet the voltmeter registers slightly over 10 volts AC. This “phantom voltage” is due to capacitive coupling between wire 5 and wire 8 (still energized) throughout the length of their mutual paths within the conduit.

Such phantom voltages may be very misleading if the technician encounters them while troubleshooting a faulty electrical system. Phantom voltages give the impression of connection (or at least high-resistance connection) where no continuity actually exists. The example shown, where the phantom voltage is 10.3 volts compared to the source voltage value of 120 volts, is actually quite modest. With increased stray capacitance between the conductors (longer wire runs in close proximity, and/or more than one energized “neighboring” wire), phantom voltage magnitude begins
to approach that of the source voltage$^3$.

The equivalent circuit is shown here, with the DMM modeled as a 10 MΩ resistance:

An analog voltmeter would never have registered 10.3 volts under the same conditions, due to its substantially lower input impedance. Thus, “phantom voltage” readings are a product of modern test equipment more than anything else.

$^3$I have personally measured “phantom” voltages in excess of 100 volts AC, in systems where the source voltage was 120 volts AC.
The obvious solution to this problem is to use a different voltmeter – one with a much lesser input impedance. But what is a technician to do if their only voltmeter is a high-impedance DMM? Connect a modest resistance in parallel with the meter input terminals, of course! Fluke happens to market just this type of accessory\(^4\), the SV225 “Stray Voltage Adapter” for the purpose of eliminating stray voltage readings on a high-impedance DMM:

With the voltmeter’s input impedance artificially decreased by the application of this accessory, the capacitive coupling is insufficient to produce any substantial voltage dropped across the voltmeter’s input terminals, thus eliminating. The technician may now proceed to test for the presence of AC control signal (or power) voltages with confidence.

\(^4\)Before there was such an accessory available, I used a 20 kΩ high-power resistor network connected in parallel with my DMM’s input terminals, which I fabricated myself. It was ugly and cumbersome, but it worked well. When I made this, I took great care in selecting resistors with power ratings high enough that accidental contact with a truly “live” AC power source (up to 600 volts) would not cause damage to them. A pre-manufactured device such as the Fluke SV225, however, is a much better option.
3.1.3 Non-contact AC voltage detection

While the last multimeter “trick” was the elimination of a parasitic effect, this trick is the exploitation of that same effect: “phantom voltage” readings obtained through capacitive coupling of a high-impedance voltmeter to a conductor energized with AC voltage (with respect to ground). You may use a high-impedance AC voltmeter to perform qualitative measurements of ground-referenced AC power voltage by setting the meter to the most sensitive AC range possible, grounding one test lead, and simply touching the other test lead to the insulation of the conductor under test. The presence of voltage (usually in the range of millivolts AC) upon close proximity to the energized conductor will indicate the energization of that conductor.

This trick is useful for determining whether or not particular AC power or control wires are energized in a location where the only access you have to those wires is their insulating sheaths. An example of where you might encounter this situation is where you have removed the cover from a conduit elbow or other fitting to gain access to a wire bundle, and you find those wires labeled for easy identification, but the wires do not terminate to any exposed metal terminals for you to contact with your multimeter’s probe tips. In this case, you may firmly connect one probe to the metal conduit fitting body, while individually touching the other probe tip to the desired conductors (one at a time), watching the meter’s indication in AC millivolts.

Several significant caveats limit the utility of this “trick:”

- The impossibility of quantitative measurement
- The potential for “false negative” readings (failure to detect a voltage that is present)
- The potential for “false positive” readings (detection of a “phantom voltage” from an adjacent conductor)
- The exclusive applicability to AC voltages of significant magnitude (≥ 100 VAC)

Being a qualitative test only, the millivoltage indication displayed by the high-impedance voltmeter tells you nothing about the actual magnitude of AC voltage between the conductor and ground. Although the meter’s input impedance is quite constant, the parasitic capacitance formed by the surface area of the test probe tip and the thickness (and dielectric constant) of the conductor insulation is quite variable. However, in conditions where the validity of the measurement may be established (e.g. cases where you can touch the probe tip to a conductor known to be energized in order to establish a “baseline” millivoltage signal), the technique is useful for quickly checking the energization status of conductors where ohmic (metal-to-metal) contact is impossible.

For the same reason of wildly variable parasitic capacitance, this technique should never be used to establish the de-energization of a conductor for safety purposes. The only time you should trust a voltmeter’s non-indication of line voltage is when that same meter is validated against a known source of similar voltage in close proximity, and when the test is performed with direct metal-to-metal (probe tip to wire) contact. A non-indicating voltmeter may indicate the absence of dangerous voltage, or it may indicate an insensitive meter.
3.1. HELPFUL “TRICKS” USING A DIGITAL MULTIMETER (DMM)

3.1.4 Detecting AC power harmonics

The presence of harmonic voltages\(^5\) in an AC power system may cause many elusive problems. Power-quality instruments exist for the purpose of measuring harmonic content in a power system, but a surprisingly good qualitative check for harmonics may be performed using a multimeter with a frequency-measuring function.

Setting a multimeter to read AC voltage (or AC current, if that is the quantity of interest) and then activating the “frequency” measurement function should produce a measurement of exactly 60.0 Hz in a properly functioning power system (50.0 Hz in Europe and some other parts of the world). The only way the meter should ever read anything significantly different from the base frequency is if there is significant harmonic content in the circuit. For example, if you set your multimeter to read frequency of AC voltage, then obtained a measurement of 60 Hz that intermittently jumped up to some higher value (say 78 Hz) and then back down to 60 Hz, it would suggest your meter was detecting harmonic voltages of sufficient amplitude to make it difficult for your meter to “lock on” to the fundamental frequency.

It is very important to note that this is a crude test of power system harmonics, and that measurements of “solid” base frequency do not guarantee the absence of harmonics. Certainly, if your multimeter produces unstable readings when set to measure frequency, it suggests the presence of strong harmonics in the circuit. However, the absence of such instability does not necessarily mean the circuit is free of harmonics. In other words, a stable reading for frequency is inconclusive: the circuit might be harmonic-free, or the harmonics may be weak enough that your multimeter ignores them and only displays the fundamental circuit frequency.

\(^5\)These are AC voltages having frequencies that are integer-multiples of the fundamental powerline frequency. In the United States, where 60 Hz is standard, harmonic frequencies would be whole-number multiples of 60: 120 Hz, 180 Hz, 240 Hz, 300 Hz, etc.
3.1.5 Identifying noise in DC signal paths

An aggravating source of trouble in analog electronic circuits is the presence of AC “noise” voltage superimposed on DC signals. Such “noise” is immediately evident when the signal is displayed on an oscilloscope screen, but how many technicians carry a portable oscilloscope with them for troubleshooting?

A high-quality multimeter exhibiting good discrimination between AC and DC voltage measurement is very useful as a qualitative noise-detection instrument. Setting the multimeter to read AC voltage, and connecting it to a signal source where pure (unchanging) DC voltage is expected, should yield a reading of nearly zero millivolts. If noise is superimposed on this DC signal, it will reveal itself as an AC voltage, which your meter will display.

Not only is the AC voltage capability of a high-quality (discriminating) multimeter useful in detecting the presence of “noise” voltage superimposed on analog DC signals, it may also give clues as to the source of the noise. By activating the frequency-measuring function of the multimeter while measuring AC voltage (or AC millivoltage), you will be able to track the frequency of the noise to see its value and stability.

Once on a job I was diagnosing a problem in an analog power control system, where the control device was acting strangely. Suspecting that noise on the measurement signal line might be causing the problem, I set my Fluke multimeter to measure AC volts, and read a noise voltage of several tenths of a volt (superimposed on a DC signal a few volts in magnitude). This told me the noise was indeed a significant problem. Pressing the “Hz” button on my multimeter, I measured a noise frequency of 360 Hz, which happens to be the “ripple” frequency of a six-pulse (three-phase) AC-to-DC rectifier operating on a base frequency of 60 Hz. This told me where the likely source of the noise was, which led me to the physical location of the problem (a bad shield on a cable run near the rectified power output wiring).
3.1. HELPFUL “TRICKS” USING A DIGITAL MULTIMETER (DMM)

3.1.6 Generating test signals

Modern digital multimeters are fantastically capable measurement tools, but did you know they are also capable of generating simple test signals? Although this is not the design purpose of the resistance and diode-check functions of a multimeter, the meter does output a low DC voltage in each of these settings.

This is useful when qualitatively testing certain measurement instruments such as data acquisition modules and other meters designed to input a low-voltage or low-current DC signal. By setting a multimeter to either the resistance ($\Omega$) or diode check function and then connecting the test leads to the input terminals of the signal-sensing device, that device’s response may be noted.

Of course, this is a qualitative test only, since multimeters are not designed to output any precise amount of voltage in either the resistance or diode-check modes. However, for testing the basic response of a process indicator, recorder, controller, data acquisition channel, DCS input, or any other DC-signal-receiving devices, it is convenient and useful. In every multimeter I have ever tried this with, the diode-check function outputs more voltage than the resistance measurement function\(^6\). This gives you two levels of “test signal” generation: a low level (resistance) and a high level (diode check). If you are interested in using your multimeter to generate test voltages, I recommend you take the time to connect your multimeter to a high-impedance voltmeter (such as another digital multimeter set to measure DC volts) and note just how much voltage your meter outputs in each mode. Knowing this will allow you to perform tests that are more quantitative than qualitative.

\(^6\)There is a design reason for this. Most digital multimeters are designed to be used on semiconductor circuits, where the minimum “turn-on” voltage of a silicon PN junction is approximately 500 to 700 millivolts. The diode-check function must output more than that, in order to force a PN junction into forward conduction. However, it is useful to be able to check ohmic resistance in a circuit without activating any PN junctions, and so the resistance measurement function typically uses test voltages less than 500 millivolts.
3.1.7 Using the meter as a temporary jumper

Often in the course of diagnosing problems in electrical and electronic systems, there is a need to temporarily connect two or more points in a circuit together to force a response. This is called “jumpering,” and the wires used to make these temporary connections are called jumper wires.

More than once I have found myself in a position where I needed to make a temporary “jumper” connection between two points in a circuit, but I did not have any wires with me to make that connection. In such cases, I learned that I could use my multimeter test leads while plugged into the current-sensing jacks of the meter. Most digital multimeters have a separate jack for the red test lead, internally connected to a low-resistance shunt leading to the common (black) test lead jack. With the red test lead plugged into this jack, the two test leads are effectively common to one another, and act as a single length of wire.

![Diagram of multimeter test leads](image)

These test lead probes are now electrically common!

Touching the meter’s test leads to two points in a circuit will now “jumper” those two points together, any current flowing through the shunt resistance of the multimeter. If desired, the meter may be turned on to monitor how much current goes through the “jumper” if this is diagnostically relevant.

An additional benefit to using a multimeter in the current-measuring mode as a test jumper is that this setting is usually current-protected by a fuse inside the meter. Applying jumper wires to a live circuit may harbor some danger if significant potential and current-sourcing capability exist between those two points: the moment a jumper wire bridges those points, a dangerous current may develop within the wire. Using the multimeter in this manner gives you a fused jumper wire: an added degree of safety in your diagnostic procedure.
3.2 Decibels

One of the mathematical tools popularly used to gauge increases and decreases of electrical power is the common logarithm, expressed as a measurement unit called the decibel. The basic idea of decibels is to express a ratio of two electrical power quantities in logarithmic terms. Every time you see the unit of “decibel” you can think: this is an expression of how much greater (or how much smaller) one power is to another. The only question is which two powers are being compared.

Electronic amplifiers are a type of electrical system where comparisons of power are useful. Students of electronics learn to compare the output power of an amplifier against the input power as a unitless ratio, called a gain. Take for example an electronic amplifier with a signal input of 40 milliWatts and a signal output of 18.4 Watts:

![Amplifier Diagram](image)

\[
\text{DC power supply} \to \text{Amplifier} \to \text{Signal} \quad \begin{array}{c}
P_{\text{in}} = 40 \text{ mW} \\
P_{\text{out}} = 18.4 \text{ W}
\end{array}
\]

\[
\text{Gain} = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{18.4 \text{ W}}{40 \text{ mW}} = 460
\]

An alternative way to express the gain of this amplifier is to do so using the unit of the Bel, defined as the common logarithm of the gain ratio:

\[
\log \left( \frac{P_{\text{out}}}{P_{\text{in}}} \right) = \log \left( \frac{18.4 \text{ W}}{40 \text{ mW}} \right) = 2.66276 \text{ B}
\]

When you see an amplifier gain expressed in the unit of “Bel”, it’s really just a way of saying “The output signal coming from this amplifier is \(x\) powers of ten greater than the input signal.” An amplifier exhibiting a gain of 1 Bel outputs 10 times as much power as the input signal. An amplifier with a gain of 2 Bels boosts the input signal by a factor of 100. The amplifier shown above, with a gain of 2.66276 Bels, boosts the input signal 460-fold.

At some point in technological history it was decided that the “Bel” (B) was too large and cumbersome, and so it became common to express powers in fractions of a Bel instead: the deciBel (1 dB = \(\frac{1}{10}\) of a Bel). Therefore, this is the form of formula you will commonly see for expressing electrical signal power gains or losses:

\[
\text{dB} = 10 \log \left( \frac{P_{\text{out}}}{P_{\text{in}}} \right)
\]

The gain of our hypothetical electronic amplifier, therefore, would be more commonly expressed as 26.6276 dB rather than 2.66276 B, although either expression is technically valid\(^7\).

\(^7\)It is interesting to note that although the “Bel” is a metric unit, it is seldom if ever used without the metric prefix
An operation students often struggle with is converting a decibel figure back into a ratio, since the concept of logarithms seems to be universally perplexing. Here I will demonstrate how to algebraically manipulate the decibel formula to solve for the power ratio given a dB figure.

First, we will begin with the decibel formula as given, solving for a value in decibels given a power ratio:

\[ \text{dB} = 10 \log(\text{Ratio}) \]

If we wish to solve for the ratio, we must “undo” all the mathematical operations surrounding that variable. One way to determine how to do this is to reverse the order of operations we would follow if we knew the ratio and were solving for the dB value. After calculating the ratio, we would then take the logarithm of that value, and then multiply that logarithm by 10: start with the ratio, then take the logarithm, then multiply last. To un-do these operations and solve for the ratio, we must un-do each of these operations in reverse order. First, we must un-do the multiplication (by dividing by 10):

\[ \frac{\text{dB}}{10} = \frac{10 \log(\text{Ratio})}{10} \]
\[ \frac{\text{dB}}{10} = \log(\text{Ratio}) \]

Next, we must un-do the logarithm function by applying its mathematical inverse to both sides of the formula – making each expression a power of 10:

\[ 10^{\frac{\text{dB}}{10}} = 10^{\log(\text{Ratio})} \]
\[ 10^{\frac{\text{dB}}{10}} = \text{Ratio} \]

To test our algebra, we can take the previous decibel value for our hypothetical amplifier and see if this new formula yields the original gain ratio:

\[ \text{Ratio} = 10^{26.6276 \ \text{dB}} \]
\[ \text{Ratio} = 10^{2.66276} \ \text{B} \]
\[ \text{Ratio} = 460 \]

Sure enough, we arrive at the correct gain ratio of 460, starting with the decibel gain figure of 26.6276 dB.

“deci” \((\frac{1}{10})\). One could express powers in microbels, megabels, or any other metric prefix desired, but it is never done in industry: only the decibel is used.
3.2. **DECIBELS**

We may also use decibels to express power *losses* in addition to power *gains*. There are many practical applications of this in signaling systems, both electronic and optical. One such application is **filtering**, where a “filter” circuit screens out certain components of the signal while letting others pass through (e.g. the bass or treble control for an audio system). Another application is **attenuation**, where the entirety of a signal is reduced in magnitude (e.g. the volume control for an audio system).

We will explore yet another application of signal power reduction as a case study for decibels: **cable loss**. Cables designed to convey signals over long distances are not perfect conduits of energy, as some of the signal’s energy is inevitably lost along the way. This is true for different types of signals, electrical and optical being two popular examples. In the following illustration we see a signal cable losing power along its length\(^8\), such that the power out is less than the power in:

\[
\text{Signal} \ P_{\text{in}} \quad \text{Cable} \quad \text{Signal} \ P_{\text{out}}
\]

\[
\frac{P_{\text{out}}}{P_{\text{in}}} = \frac{37 \text{ mW}}{40 \text{ mW}} = 0.925
\]

\[
10 \log \left( \frac{P_{\text{out}}}{P_{\text{in}}} \right) = 10 \log \left( \frac{37 \text{ mW}}{40 \text{ mW}} \right) = -0.3386 \text{ dB}
\]

Contrasting this result against the previous result (with the amplifier) we see a very important property of decibel figures: any power *gain* is expressed as a *positive* decibel value, while any power *loss* is expressed as a *negative* decibel value. Any component outputting the exact same power as it takes in will exhibit a “gain” value of 0 dB (equivalent to a gain *ratio* of 1).

Remember that Bels and decibels are nothing more than logarithmic expressions of “greater than” and “less than”. Positive values represent powers that are *greater* while negative values represent powers that are *lesser*. Zero Bel or decibel values represent *no change* (neither gain nor loss) in power.

A couple of simple decibel values are useful to remember for approximations, where you need to quickly estimate decibel values from power ratios (or vice-versa). Each addition or subtraction of 10 dB exactly represents a 10-fold multiplication or division of power ratio: e.g. +20 dB represents a power ratio gain of \(10 \times 10 = 100\), whereas −30 dB represents a power ratio reduction of \(\frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} = \frac{1}{1000}\). Each addition or subtraction of 3 dB approximately represents a 2-fold multiplication or division or power ratio: e.g. +6 dB is approximately equal to a power ratio gain of \(2 \times 2 = 4\), whereas −12 dB is approximately equal to a power ratio reduction of \(\frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{8}\). We may combine ± 10 dB and ± 3 dB increments to come up with ratios that are products of 10 and 2: e.g. +26 dB is approximately equal to a power ratio gain of \(10 \times 10 \times 2 \times 2 = 400\).

---

\(^8\)For high-frequency signals such as those used in radio communications, the dominant mode of energy dissipation is **dielectric heating**, where the AC electric field between the cable conductors excites the molecules of the conductor insulation. This energy loss manifests as heat, which explains why there is less signal energy present at the load end of the cable than is input at the source end of the cable. For DC and low-frequency AC circuits the dominant mode of energy dissipation is cable conductor resistance, which is typically very small.
Observe what happens if we combine a “gain” component with a “loss” component and calculate the overall power out versus power in:

\[
\text{DC power supply} \quad \text{Signal } P_{\text{in}} \quad 40 \text{ mW} \quad \rightarrow \quad \text{Amplifier} \quad \rightarrow \quad \text{Cable} \quad \rightarrow \quad \text{Signal } P_{\text{out}} \quad 17.02 \text{ W}
\]

Gain = 460 (ratio)  
Gain = 26.6276 dB  
Loss = 0.925 (ratio)  
Loss = -0.3386 dB

The overall gain of this amplifier and cable system expressed as a ratio is equal to the product of the individual component gain/loss ratios. That is, the gain ratio of the amplifier multiplied by the loss ratio of the cable yields the overall power ratio for the system:

\[
\text{Overall gain} = \frac{17.02 \text{ W}}{40 \text{ mW}} = (460)(0.925) = 425.5
\]

The overall gain may be alternatively expressed as a decibel figure, in which case it is equal to the sum of the individual component decibel values. That is, the decibel gain of the amplifier added to the decibel loss of the cable yields the overall decibel figure for the system:

\[
\text{Overall gain} = 10 \log \left( \frac{17.02 \text{ W}}{40 \text{ mW}} \right) = 26.6276 \text{ dB} + (-0.3386 \text{ dB}) = 26.2890 \text{ dB}
\]

It is often useful to be able to estimate decibel values from power ratios and vice-versa. If we take the gain ratio of this amplifier and cable system (425.5) and round it down to 400, we may easily express this gain ratio as an expanded product of 10 and 2:

\[
425.5 \approx 400 = (10) \times (10) \times (2) \times (2)
\]

Knowing that every 10-fold multiplication of power ratio is an addition of +10 dB, and that every 2-fold multiplication of power is an addition of +3 dB, we may express the expanded product as a sum of decibel values:

\[
(10) \times (10) \times (2) \times (2) = (10 \text{ dB}) + (10 \text{ dB}) + (3 \text{ dB}) + (3 \text{ dB}) = 26 \text{ dB}
\]

Therefore, our power ratio of 425.5 is approximately equal to +26 decibels.
3.2. DECIBELS

Decibels always represent comparisons of power, but that comparison need not always be $P_{out}/P_{in}$ for a system component. We may also use decibels to express an amount of power compared to some standard reference. If, for example, we wished to express the input power to our hypothetical amplifier (40 milliWatts) using decibels, we could do so by comparing 40 mW against a standard “reference” power of exactly 1 milliWatt. The resulting decibel figure would be written as “dBm” in honor of the 1 milliWatt reference:

$$P_{in} = 10 \log \left( \frac{40 \text{ mW}}{1 \text{ mW}} \right) = 16.0206 \text{ dBm}$$

The unit of “dBm” literally means the amount of dB “greater than” 1 milliWatt. In this case, our input signal of 40 milliWatts is 16.0206 dB greater than a standard reference power of exactly 1 milliWatt. The output power of that amplifier (18.4 Watts) may be expressed in dBm as well:

$$P_{out} = 10 \log \left( \frac{18.4 \text{ W}}{1 \text{ mW}} \right) = 42.6482 \text{ dBm}$$

A signal power of 18.4 Watts is 42.6482 dB greater than a standard reference power of exactly 1 milliWatt, and so it has a decibel value of 42.6482 dBm.

![Signal Flow Diagram](DC_power_supply.png)

Notice how the output and input powers expressed in dBm relate to the power gain of the amplifier. Taking the input power and simply adding the amplifier’s gain factor yields the amplifier’s output power in dBm:

$$P_{in}(\text{dB}) + P_{gain}(\text{dB}) = P_{out}(\text{dB})$$

$$16.0206 \text{ dBm} + 26.6276 \text{ dB} = 42.6482 \text{ dBm}$$

An electronic signal that begins 16.0206 dB greater than 1 milliWatt, when boosted by an amplifier gain of 26.6276 dB, will become 42.6482 dB greater than the original reference power of 1 milliWatt.
We may alternatively express all powers in this hypothetical amplifier in reference to a 1-Watt standard power, with the resulting power expressed in units of “dBW” (decibels greater than 1 Watt):

\[ P_{\text{in}} = 10 \log \left( \frac{40 \text{ mW}}{1 \text{ W}} \right) = -13.9794 \text{ dBW} \]

\[ P_{\text{out}} = 10 \log \left( \frac{18.4 \text{ W}}{1 \text{ W}} \right) = 12.6482 \text{ dBW} \]

Note how the input power of 40 milliWatts equates to a negative dBW figure because 40 milliWatts is less than the 1 Watt reference, and how the output power of 18.4 Watts equates to a positive dBW figure because 18.4 Watts is more than the 1 Watt reference. A positive dB figure means “more than” while a negative dB figure means “less than.”

Note also how the output and input powers expressed in dBW still relate to the power gain of the amplifier by simple addition, just as they did when previously expressed in units of dBm. Taking the input power in units of dBW and simply adding the amplifier’s gain factor yields the amplifier’s output power in dBW:

\[ P_{\text{in}}(\text{dB}) + P_{\text{gain}}(\text{dB}) = P_{\text{out}}(\text{dB}) \]

\[-13.9794 \text{ dBW} + 26.6276 \text{ dB} = 12.6482 \text{ dBW} \]

An electronic signal that begins 13.9794 dB less than 1 Watt, when boosted by an amplifier gain of 26.6276 dB, will become 12.6482 dB greater than the original reference power of 1 Watt.
This is one of the major benefits of using decibels to express powers: we may very easily calculate power gains and losses by summing a string of dB figures, each dB figure representing the power gain or power loss of a different system component. Normally, any compounding of ratios involves multiplication and/or division of those ratios, but with decibels we may simply add and subtract. One of the interesting mathematical properties of logarithms is that they “transform” one type of problem into a simpler type: in this case, a problem of multiplying ratios into a (simpler) problem of adding decibel figures.

For example, we may express the power dissipated along a cable in terms of decibels per foot; the longer the cable, of course, the more power will be lost this way, all other factors being equal. For example, a radio-frequency signal cable having a loss figure of \(-0.15\) decibels per foot at a signal frequency of 2.4 GHz will suffer \(-15\) dB over 100 feet, and \(-150\) dB over 1000 feet. To illustrate how decibels may be used to calculate power delivered to a load in such a system, accounting for various gains and losses along the way using decibel figures:

\[
\begin{align*}
\text{Power output} &= 21.8 \text{ dBm} \\
\text{Cable loss} &= -0.17 \text{ dB/ft} \\
\text{Length} &= 6 \text{ feet} \\
\text{Gain} &= 45 \text{ dB} \\
\text{Power delivered to the load} &= 62.38 \text{ dBm}
\end{align*}
\]

\[
\begin{align*}
21.8 \text{ dBm} + (-0.17 \text{ dB/ft})(6 \text{ ft}) + 45 \text{ dB} + (-0.17 \text{ dB/ft})(20 \text{ ft}) \\
= 21.8 \text{ dBm} - 1.02 \text{ dB} + 45 \text{ dB} - 3.4 \text{ dB} \\
= 62.38 \text{ dBm}
\end{align*}
\]

A similar application of decibels is found in multi-stage amplifier circuits, where one stage amplifies a signal to be fed into a successive stage to be amplified more. The power gains of these stages, each expressed as a ratio, multiply to make the over-all amplifier’s power gain (ratio). The power gains of those same stages, each expressed as a decibel figure, add to make the over-all amplifier’s power gain (dB):

\[\text{Stage 1} \times \text{Stage 2} \times \text{Stage 3}\]

In fact, logarithms are one of the simplest examples of a transform function, converting one type of mathematical problem into another type. Other examples of mathematical transform functions used in engineering include the Fourier transform (converting a time-domain function into a frequency-domain function) and the Laplace transform (converting a differential equation into an algebraic equation).
Another common application of decibels is to express ratios of voltage and/or current rather than power. However, since the unit of the Bel has been defined as an expression of a power ratio, we cannot simply substitute $V$ or $I$ for $P$ in any of the formulæ we’ve seen so far.

Suppose an amplifier has a voltage gain of 2 (i.e. $V_{out}$ is twice as large as $V_{in}$), and we would like to express this gain in decibels. Since decibels are intended to express power gain and not voltage gain, we must figure out how much power gain is equivalent to a voltage gain of two. Obviously, voltage and power are fundamentally different quantities, but if we imagine ourselves connecting a fixed load resistance to the input signal, and then to the output signal, we will realize that load’s power dissipation will be more than double when energized by a voltage twice as large. Joule’s Law is helpful to determine the exact ratio of power dissipation:

$$P = \frac{V^2}{R}$$

Doubling voltage for any given load resistance results in power \textit{quadrupling} because power is proportional to the square of the voltage applied to a fixed resistance. Using this as the basis for applying decibels to a voltage ratio. Knowing that Joule’s Law also declares power is proportional to the square of the current applied to a fixed resistance ($P = I^2R$) means this same mathematical relationship will apply to current gains and reductions as well as voltage gains and reductions:

$$\text{dB} = 10 \log \left( \frac{P_{out}}{P_{in}} \right) = 10 \log \left( \frac{V_{out}}{V_{in}} \right)^2 = 10 \log \left( \frac{I_{out}}{I_{in}} \right)^2$$

An algebraic identity of logarithms is that the logarithm of any quantity raised to a power is equal to that power multiplied by the logarithm of the quantity. Expressed in general terms:

$$\log x^y = y \log x$$

Therefore, we may simplify the decibel formula for voltage gain by removing the “2” power and making it a multiplier:

$$10 \log \left( \frac{V_{out}}{V_{in}} \right)^2 = (2)(10) \log \left( \frac{V_{out}}{V_{in}} \right) = 20 \log \left( \frac{V_{out}}{V_{in}} \right)$$

$$10 \log \left( \frac{I_{out}}{I_{in}} \right)^2 = (2)(10) \log \left( \frac{I_{out}}{I_{in}} \right) = 20 \log \left( \frac{I_{out}}{I_{in}} \right)$$

Thus, we may use decibels to express voltage or current ratios if we simply substitute 20 instead of 10 as the multiplier.
3.2. DECIBELS

We can see the practicality of using decibels to represent something other than electrical power by examining this analog meter face, belonging to a Simpson model 260 VOM (Volt-Ohm-Milliammeter). Note the bottom scale on this meter’s face, calibrated in decibels (DB):

Pay attention to the note on decibels written in the lower-left corner of the meter face, where 0 dB is defined as 0.001 Watt dissipated by 600 Ohms. The fact that 0 dB is defined as 1 milliWatt means it should (properly) be labeled dBm rather than dB\(^1\). A load resistance value is necessary as part of this definition for dB because this meter cannot measure power directly but must infer signal power from measurements of AC voltage. Without a specific load resistance, there is no clear relation between voltage and power. 600 Ohms is an old telecommunications standard for audio-frequency AC signals, and continues to be used today for voltage-based decibel measurements of audio-frequency AC signals.

The meter as shown is connected to nothing at all, and so registers 0 Volts AC. This, of course, corresponds to zero power, and it has no corresponding decibel value because the logarithm of zero is mathematically undefined\(^2\). Practically, it means \(-\infty\) dB, which is why the needle at the 0 Volt position “falls off” the left-hand end of the dB scale.

Close inspection of the dB scale on this meter face reveals another interesting property of decibels, and that is the nonlinear nature of the dB scale. This contrasts starkly against all the voltage and current scales on this meter face which are linear. This nonlinearity is a fundamental property of decibels because it is based on the logarithm function which is nonlinear.

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\(^1\)Such mis-labeling is not that uncommon in the profession, the expectation being that the technician or engineer working with the instrument ought to be familiar enough with the concept of decibels to know when dB really means dBm, or dBW, etc.

\(^2\)Your electronic calculator will complain if you attempt to take the logarithm of zero!
Now, we will explore what is necessary to make this meter register 0 dBm (i.e. 1 milliWatt) with an applied AC voltage. 1 milliWatt of power dissipated by 600 Ohms is equivalent to:

\[ V = \sqrt{PR} = \sqrt{(0.001)(600)} = 0.7746 \text{ Volts} \]

Setting the VOM to the 2.5 V AC range and applying just enough AC voltage to bring the needle to the 0 dB mark allows us to verify that this is indeed equivalent to just under 0.8 Volts (read on the 2.5 VAC scale):

In the lower-right corner of the meter face we see some notes regarding correction values for decibel measurements when using different AC voltage ranges. The dB scale is read directly when the meter is set on the 2.5 VAC range. When set on the 10 VAC range (i.e. a range four times as great), the meter’s needle will experience a deflection one-fourth as much as when set to the 2.5 VAC range, and therefore it will point to a lesser (or even negative) value on the dB scale. Converting a voltage ratio of 0.25 into a decibel figure shows us how much less the needle will register on the dB scale when the voltage range is quadrupled:

\[ 20 \log \left( \frac{2.5}{10} \right) = -12.04 \text{ dB} \]

Therefore, when using the 10 VAC range instead of the 2.5 VAC range, one must add 12 dB to the reading. Likewise, we may prove each of the printed correction factors for the alternative voltage-measurement ranges listed (50 Volt AC range and 250 Volt AC range):

\[ 20 \log \left( \frac{2.5}{50} \right) = -26.02 \text{ dB} \]

\[ 20 \log \left( \frac{2.5}{250} \right) = -40.0 \text{ dB} \]
Chapter 4

Questions

This learning module, along with all others in the ModEL collection, is designed to be used in an inverted instructional environment where students independently read the tutorials and attempt to answer questions on their own prior to the instructor’s interaction with them. In place of lecture, the instructor engages with students in Socratic-style dialogue, probing and challenging their understanding of the subject matter through inquiry.

Answers are not provided for questions within this chapter, and this is by design. Solved problems may be found in the Tutorial and Derivation chapters, instead. The goal here is independence, and this requires students to be challenged in ways where others cannot think for them. Remember that you always have the tools of experimentation and computer simulation (e.g. SPICE) to explore concepts!

The following lists contain ideas for Socratic-style questions and challenges. Upon inspection, one will notice a strong theme of metacognition within these statements: they are designed to foster a regular habit of examining one’s own thoughts as a means toward clearer thinking. As such these sample questions are useful both for instructor-led discussions as well as for self-study.

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1 Technical reading is an essential academic skill for any technical practitioner to possess for the simple reason that the most comprehensive, accurate, and useful information to be found for developing technical competence is in textual form. Technical careers in general are characterized by the need for continuous learning to remain current with standards and technology, and therefore any technical practitioner who cannot read well is handicapped in their professional development. An excellent resource for educators on improving students’ reading prowess through intentional effort and strategy is the book Reading For Understanding – How Reading Apprenticeship Improves Disciplinary Learning in Secondary and College Classrooms by Ruth Schoenbach, Cynthia Greenleaf, and Lynn Murphy.

2 Lecture is popular as a teaching method because it is easy to implement: any reasonably articulate subject matter expert can talk to students, even with little preparation. However, it is also quite problematic. A good lecture always makes complicated concepts seem easier than they are, which is bad for students because it instills a false sense of confidence in their own understanding; reading and re-articulation requires more cognitive effort and serves to verify comprehension. A culture of teaching-by-lecture fosters a debilitating dependence upon direct personal instruction, whereas the challenges of modern life demand independent and critical thought made possible only by gathering information and perspectives from afar. Information presented in a lecture is ephemeral, easily lost to failures of memory and dictation; text is forever, and may be referenced at any time.
CHAPTER 4. QUESTIONS

General challenges following tutorial reading

- **Summarize** as much of the text as you can in one paragraph of your own words. A helpful strategy is to explain ideas as you would for an intelligent child: as simple as you can without compromising too much accuracy.

- **Simplify** a particular section of the text, for example a paragraph or even a single sentence, so as to capture the same fundamental idea in fewer words.

- Where did the text make the most sense to you? What was it about the text’s presentation that made it clear?

- Identify where it might be easy for someone to misunderstand the text, and explain why you think it could be confusing.

- Identify any **new concept(s)** presented in the text, and explain in your own words.

- Identify any **familiar concept(s)** such as physical laws or principles applied or referenced in the text.

- Devise a **proof of concept** experiment demonstrating an important principle, physical law, or technical innovation represented in the text.

- Devise an experiment to **disprove** a plausible misconception.

- Did the text reveal any **misconceptions** you might have harbored? If so, describe the misconception(s) and the reason(s) why you now know them to be incorrect.

- Describe any useful **problem-solving strategies** applied in the text.

- Devise a question of your own to challenge a reader’s comprehension of the text.
General follow-up challenges for assigned problems

- Identify where any fundamental laws or principles apply to the solution of this problem, especially before applying any mathematical techniques.
- Devise a thought experiment to explore the characteristics of the problem scenario, applying known laws and principles to mentally model its behavior.
- Describe in detail your own strategy for solving this problem. How did you identify and organized the given information? Did you sketch any diagrams to help frame the problem?
- Is there more than one way to solve this problem? Which method seems best to you?
- Show the work you did in solving this problem, even if the solution is incomplete or incorrect.
- What would you say was the most challenging part of this problem, and why was it so?
- Was any important information missing from the problem which you had to research or recall?
- Was there any extraneous information presented within this problem? If so, what was it and why did it not matter?
- Examine someone else’s solution to identify where they applied fundamental laws or principles.
- Simplify the problem from its given form and show how to solve this simpler version of it. Examples include eliminating certain variables or conditions, altering values to simpler (usually whole) numbers, applying a limiting case (i.e. altering a variable to some extreme or ultimate value).
- For quantitative problems, identify the real-world meaning of all intermediate calculations: their units of measurement, where they fit into the scenario at hand. Annotate any diagrams or illustrations with these calculated values.
- For quantitative problems, try approaching it qualitatively instead, thinking in terms of “increase” and “decrease” rather than definite values.
- For qualitative problems, try approaching it quantitatively instead, proposing simple numerical values for the variables.
- Were there any assumptions you made while solving this problem? Would your solution change if one of those assumptions were altered?
- Identify where it would be easy for someone to go astray in attempting to solve this problem.
- Formulate your own problem based on what you learned solving this one.

General follow-up challenges for experiments or projects

- In what way(s) was this experiment or project easy to complete?
- Identify some of the challenges you faced in completing this experiment or project.
• Show how thorough documentation assisted in the completion of this experiment or project.

• Which fundamental laws or principles are key to this system’s function?

• Identify any way(s) in which one might obtain false or otherwise misleading measurements from test equipment in this system.

• What will happen if (component X) fails (open/shorted/etc.)?

• What would have to occur to make this system unsafe?
4.1 Conceptual reasoning

These questions are designed to stimulate your analytic and synthetic thinking. In a Socratic discussion with your instructor, the goal is for these questions to prompt an extended dialogue where assumptions are revealed, conclusions are tested, and understanding is sharpened. Your instructor may also pose additional questions based on those assigned, in order to further probe and refine your conceptual understanding.

Questions that follow are presented to challenge and probe your understanding of various concepts presented in the tutorial. These questions are intended to serve as a guide for the Socratic dialogue between yourself and the instructor. Your instructor’s task is to ensure you have a sound grasp of these concepts, and the questions contained in this document are merely a means to this end. Your instructor may, at his or her discretion, alter or substitute questions for the benefit of tailoring the discussion to each student’s needs. The only absolute requirement is that each student is challenged and assessed at a level equal to or greater than that represented by the documented questions.

It is far more important that you convey your reasoning than it is to simply convey a correct answer. For this reason, you should refrain from researching other information sources to answer questions. What matters here is that you are doing the thinking. If the answer is incorrect, your instructor will work with you to correct it through proper reasoning. A correct answer without an adequate explanation of how you derived that answer is unacceptable, as it does not aid the learning or assessment process.

You will note a conspicuous lack of answers given for these conceptual questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. The best way by far is to debate the answers with fellow students and also with the instructor during the Socratic dialogue sessions intended to be used with these learning modules. Reasoning through challenging questions with other people is an excellent tool for developing strong reasoning skills.

Another means of checking your conceptual answers, where applicable, is to use circuit simulation software to explore the effects of changes made to circuits. For example, if one of these conceptual questions challenges you to predict the effects of altering some component parameter in a circuit, you may check the validity of your work by simulating that same parameter change within software and seeing if the results agree.

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3Analytical thinking involves the “disassembly” of an idea into its constituent parts, analogous to dissection. Synthetic thinking involves the “assembly” of a new idea comprised of multiple concepts, analogous to construction. Both activities are high-level cognitive skills, extremely important for effective problem-solving, necessitating frequent challenge and regular practice to fully develop.
4.1.1 Reading outline and reflections

“Reading maketh a full man; conference a ready man; and writing an exact man” – Francis Bacon

Francis Bacon’s advice is a blueprint for effective education: reading provides the learner with knowledge, writing focuses the learner’s thoughts, and critical dialogue equips the learner to confidently communicate and apply their learning. Independent acquisition and application of knowledge is a powerful skill, well worth the effort to cultivate. To this end, students should read these educational resources closely, write their own outline and reflections on the reading, and discuss in detail their findings with classmates and instructor(s). You should be able to do all of the following after reading any instructional text:

√ Briefly OUTLINE THE TEXT, as though you were writing a detailed Table of Contents. Feel free to rearrange the order if it makes more sense that way. Prepare to articulate these points in detail and to answer questions from your classmates and instructor. Outlining is a good self-test of thorough reading because you cannot outline what you have not read or do not comprehend.

√ Demonstrate ACTIVE READING STRATEGIES, including verbalizing your impressions as you read, simplifying long passages to convey the same ideas using fewer words, annotating text and illustrations with your own interpretations, working through mathematical examples shown in the text, cross-referencing passages with relevant illustrations and/or other passages, identifying problem-solving strategies applied by the author, etc. Technical reading is a special case of problem-solving, and so these strategies work precisely because they help solve any problem: paying attention to your own thoughts (metacognition), eliminating unnecessary complexities, identifying what makes sense, paying close attention to details, drawing connections between separated facts, and noting the successful strategies of others.

√ Identify IMPORTANT THEMES, especially GENERAL LAWS and PRINCIPLES, expounded in the text and express them in the simplest of terms as though you were teaching an intelligent child. This emphasizes connections between related topics and develops your ability to communicate complex ideas to anyone.

√ Form YOUR OWN QUESTIONS based on the reading, and then pose them to your instructor and classmates for their consideration. Anticipate both correct and incorrect answers, the incorrect answer(s) assuming one or more plausible misconceptions. This helps you view the subject from different perspectives to grasp it more fully.

√ Devise EXPERIMENTS to test claims presented in the reading, or to disprove misconceptions. Predict possible outcomes of these experiments, and evaluate their meanings: what result(s) would confirm, and what would constitute disproof? Running mental simulations and evaluating results is essential to scientific and diagnostic reasoning.

√ Specifically identify any points you found CONFUSING. The reason for doing this is to help diagnose misconceptions and overcome barriers to learning.
4.1.2 Foundational concepts

Correct analysis and diagnosis of electric circuits begins with a proper understanding of some basic concepts. The following is a list of some important concepts referenced in this module’s full tutorial. Define each of them in your own words, and be prepared to illustrate each of these concepts with a description of a practical example and/or a live demonstration.

- Energy
- Voltage
- Current
- Resistance
- Volt (unit of measurement)
- Ampere (unit of measurement)
- Ohm (unit of measurement)
- Ohm’s Law
- Series connection
- Parallel connection
- Resistor
- Joule’s Law
Insertion resistance

Open

Short

Polarity

Magnetic field

Electromagnetism

Fuse

Polarized device

Significant figure

Range
4.1.3 Choosing a voltmeter range

Suppose I were about to measure an unknown voltage with a manual-range voltmeter. This particular voltmeter has several different voltage measurement ranges to choose from:

- 500 Volts
- 250 Volts
- 100 Volts
- 50 Volts
- 25 Volts
- 10 Volts
- 5 Volts

What range would be best to begin with, when first measuring this unknown voltage with the meter? Explain your answer.

Challenges

- When measuring current, is the range selection process fundamentally similar or different? Why?
4.1.4 Applying foundational concepts to multimeter usage

Identify which foundational concept(s) apply to each of the declarations shown below regarding the following circuit. If a declaration is true, then identify it as such and note which concept supports that declaration; if a declaration is false, then identify it as such and note which concept is violated by that declaration:

- Connect voltmeter to points B and F to measure voltage of resistor $R_1$
- Connect ammeter between points D and K to measure current through $R_6$
- Break wire at point E and connect ammeter between the broken wire ends to measure current through $R_5$
- Connect ammeter between points F and H to measure current through source $V_2$
- If $R_5$ fails open, current measured through $V_2$ using an ammeter will become zero

Here is a list of foundational concepts for your reference: Conservation of Energy, Conservation of Electric Charge, behavior of sources vs. loads, effects of open faults, effect of shorted faults, properties of series networks, properties of parallel networks, meter insertion resistance. More than one of these concepts may apply to a declaration, and some concepts may not apply to any listed declaration at all. Also, feel free to include foundational concepts not listed here.

Lastly, define the following terms and apply them to any locations in this circuit you may choose:
4.1. CONCEPTUAL REASONING

- Voltage
- Current
- Resistance
- Power

Challenges

- Which components are guaranteed to share the exact same amount of voltage due to how they connect together in the circuit?
- Which components are guaranteed to share the exact same amount of current due to how they connect together in the circuit?
4.1.5 Testing multimeters with an ohmmeter

If we were to connect a multimeter (configured to measure voltage) directly to another multimeter (configured to read resistance), what would you expect to see the ohmmeter register for resistance between its test leads?

If we were to connect a multimeter (configured to measure current) directly to another multimeter (configured to read resistance), what would you expect to see the ohmmeter register for resistance between its test leads?

Challenges
• What should the probe-to-probe resistance of a voltmeter *ideally* be? Why?
• What should the probe-to-probe resistance of an ammeter *ideally* be? Why?
4.1.6 Phantom voltage measurements

A technician uses a digital multimeter to check for the presence of dangerous voltage between conductor #3 and Earth ground prior to touching that conductor. This safety check is done as a matter of precaution, even though the technician has reason to believe that conductor is electrically distinct (i.e. not electrically common to any other conductors) and should not be “live”. To this technician’s surprise, he measures 43 Volts AC between conductor #3 and ground!

Puzzled, this technician consults another technician to ask how it is possible to measure a possibly dangerous voltage level between a conductor and ground when the conductor in question is not connected to anything else. “Oh,” says the other technician, “That’s probably just a phantom voltage. Don’t worry about it!”

Explain this phenomenon. Exactly how is the AC voltmeter registering a voltage on what should be a “dead” wire?

Should you be concerned about the safety hazard of so-called “phantom voltages”? Why or why not?

Some voltmeters made for general electrical use (rather than precision electronic use) are specially built to have less input impedance than typical: tens of kiloOhms instead of megaOhms. This design helps minimize “phantom” voltage measurements. Explain how a voltmeter with less input impedance (also known as insertion resistance) than usual is less liable to be “fooled” when taking measurements on an unattached conductor such as this.
4.1. CONCEPTUAL REASONING

Challenges

- Are “phantom” voltages strictly an AC phenomenon, or may they manifest in DC circuits as well?

- Identify some parameters of the multi-conductor cable which could be modified (e.g. length, wire gauge, insulation thickness, etc.) to exacerbate the “phantom” voltages effect.
CHAPTER 4. QUESTIONS

4.2 Quantitative reasoning

These questions are designed to stimulate your computational thinking. In a Socratic discussion with your instructor, the goal is for these questions to reveal your mathematical approach(es) to problem-solving so that good technique and sound reasoning may be reinforced. Your instructor may also pose additional questions based on those assigned, in order to observe your problem-solving firsthand.

Mental arithmetic and estimations are strongly encouraged for all calculations, because without these abilities you will be unable to readily detect errors caused by calculator misuse (e.g. keystroke errors).

You will note a conspicuous lack of answers given for these quantitative questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. My advice is to use circuit simulation software such as SPICE to check the correctness of quantitative answers. Refer to those learning modules within this collection focusing on SPICE to see worked examples which you may use directly as practice problems for your own study, and/or as templates you may modify to run your own analyses and generate your own practice problems.

Completely worked example problems found in the Tutorial may also serve as "test cases" for gaining proficiency in the use of circuit simulation software, and then once that proficiency is gained you will never need to rely on an answer key!

---

4In other words, set up the circuit simulation software to analyze the same circuit examples found in the Tutorial. If the simulated results match the answers shown in the Tutorial, it confirms the simulation has properly run. If the simulated results disagree with the Tutorial’s answers, something has been set up incorrectly in the simulation software. Using every Tutorial as practice in this way will quickly develop proficiency in the use of circuit simulation software.

5This approach is perfectly in keeping with the instructional philosophy of these learning modules: teaching students to be self-sufficient thinkers. Answer keys can be useful, but it is even more useful to your long-term success to have a set of tools on hand for checking your own work, because once you have left school and are on your own, there will no longer be “answer keys” available for the problems you will have to solve.
4.2. QUANTITATIVE REASONING

4.2.1 Miscellaneous physical constants

Note: constants shown in bold type are exact, not approximations. Values inside of parentheses show one standard deviation (σ) of uncertainty in the final digits: for example, Avogadro’s number given as 6.02214179(30) × 10²³ means the center value (6.02214179 × 10²³) plus or minus 0.00000030 × 10²³.

Avogadro’s number (Nₐ) = 6.02214179(30) × 10²³ per mole (mol⁻¹)

Boltzmann’s constant (k) = 1.3806504(24) × 10⁻²³ Joules per Kelvin (J/K)

Electronic charge (e) = 1.602176487(40) × 10⁻¹⁹ Coulomb (C)

Faraday constant (F) = 9.64853399(24) × 10⁴ Coulombs per mole (C/mol)

Magnetic permeability of free space (µ₀) = 1.25663706212(19) × 10⁻⁶ Henrys per meter (H/m)

Electric permittivity of free space (ε₀) = 8.8541878128(13) × 10⁻¹² Farads per meter (F/m)

Characteristic impedance of free space (Z₀) = 376.730313668(57) Ohms (Ω)

Gravitational constant (G) = 6.67428(67) × 10⁻¹¹ cubic meters per kilogram-seconds squared (m³/kg-s²)

Molar gas constant (R) = 8.314472(15) Joules per mole-Kelvin (J/mol-K) = 0.08205746(14) liters-atmospheres per mole-Kelvin

Planck constant (h) = 6.62606896(33) × 10⁻³⁴ joule-seconds (J-s)

Stefan-Boltzmann constant (σ) = 5.670400(40) × 10⁻⁸ Watts per square meter-Kelvin⁴ (W/m²-K⁴)

Speed of light in a vacuum (c) = 299792458 meters per second (m/s) = 186282.4 miles per second (mi/s)

Note: All constants taken from NIST data “Fundamental Physical Constants – Extensive Listing”, from http://physics.nist.gov/ constants, National Institute of Standards and Technology (NIST), 2006; with the exception of the permeability of free space which was taken from NIST’s 2018 CODATA recommended values database.
4.2.2 Introduction to spreadsheets

A powerful computational tool you are encouraged to use in your work is a spreadsheet. Available on most personal computers (e.g. Microsoft Excel), spreadsheet software performs numerical calculations based on number values and formulae entered into cells of a grid. This grid is typically arranged as lettered columns and numbered rows, with each cell of the grid identified by its column/row coordinates (e.g. cell B3, cell A8). Each cell may contain a string of text, a number value, or a mathematical formula. The spreadsheet automatically updates the results of all mathematical formulae whenever the entered number values are changed. This means it is possible to set up a spreadsheet to perform a series of calculations on entered data, and those calculations will be re-done by the computer any time the data points are edited in any way.

For example, the following spreadsheet calculates average speed based on entered values of distance traveled and time elapsed:

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th>B</th>
<th>C</th>
<th>D</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Distance traveled</td>
<td>46.9</td>
<td>Kilometers</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>Time elapsed</td>
<td>1.18</td>
<td>Hours</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>Average speed</td>
<td>= B1 / B2</td>
<td>km/h</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Text labels contained in cells A1 through A3 and cells C1 through C3 exist solely for readability and are not involved in any calculations. Cell B1 contains a sample distance value while cell B2 contains a sample time value. The formula for computing speed is contained in cell B3. Note how this formula begins with an “equals” symbol (=), references the values for distance and speed by lettered column and numbered row coordinates (B1 and B2), and uses a forward slash symbol for division (/). The coordinates B1 and B2 function as variables\(^6\) would in an algebraic formula.

When this spreadsheet is executed, the numerical value 39.74576 will appear in cell B3 rather than the formula = B1 / B2, because 39.74576 is the computed speed value given 46.9 kilometers traveled over a period of 1.18 hours. If a different numerical value for distance is entered into cell B1 or a different value for time is entered into cell B2, cell B3’s value will automatically update. All you need to do is set up the given values and any formulae into the spreadsheet, and the computer will do all the calculations for you.

Cell B3 may be referenced by other formulae in the spreadsheet if desired, since it is a variable just like the given values contained in B1 and B2. This means it is possible to set up an entire chain of calculations, one dependent on the result of another, in order to arrive at a final value. The arrangement of the given data and formulae need not follow any pattern on the grid, which means you may place them anywhere.

\(^6\)Spreadsheets may also provide means to attach text labels to cells for use as variable names (Microsoft Excel simply calls these labels “names”), but for simple spreadsheets such as those shown here it’s usually easier just to use the standard coordinate naming for each cell.
Common arithmetic operations available for your use in a spreadsheet include the following:

- Addition (+)
- Subtraction (-)
- Multiplication (*)
- Division (/)
- Powers (^)
- Square roots (sqrt())
- Logarithms (ln(), log10())

Parentheses may be used to ensure proper order of operations within a complex formula. Consider this example of a spreadsheet implementing the quadratic formula, used to solve for roots of a polynomial expression in the form of $ax^2 + bx + c$:

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th>B</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>x_1 = (-B4 + sqrt((B4^2) - (4<em>B3</em>B5))) / (2*B3)</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>x_2 = (-B4 - sqrt((B4^2) - (4<em>B3</em>B5))) / (2*B3)</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>a = 9</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>b = 5</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>c = -2</td>
<td></td>
</tr>
</tbody>
</table>

This example is configured to compute roots of the polynomial $9x^2 + 5x - 2$ because the values of 9, 5, and −2 have been inserted into cells B3, B4, and B5, respectively. Once this spreadsheet has been built, though, it may be used to calculate the roots of any second-degree polynomial expression simply by entering the new $a$, $b$, and $c$ coefficients into cells B3 through B5. The numerical values appearing in cells B1 and B2 will be automatically updated by the computer immediately following any changes made to the coefficients.

---

7 Modern spreadsheet software offers a bewildering array of mathematical functions you may use in your computations. I recommend you consult the documentation for your particular spreadsheet for information on operations other than those listed here.

8 Spreadsheet programs, like text-based programming languages, are designed to follow standard order of operations by default. However, my personal preference is to use parentheses even where strictly unnecessary just to make it clear to any other person viewing the formula what the intended order of operations is.

9 Reviewing some algebra here, a root is a value for $x$ that yields an overall value of zero for the polynomial. For this polynomial ($9x^2 + 5x - 2$) the two roots happen to be $x = 0.269381$ and $x = -0.82494$, with these values displayed in cells B1 and B2, respectively upon execution of the spreadsheet.
Alternatively, one could break up the long quadratic formula into smaller pieces like this:

\[
y = \sqrt{b^2 - 4ac} \quad z = 2a
\]

\[
x = \frac{-b \pm y}{z}
\]

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th>B</th>
<th>C</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>x_1</td>
<td>((-B4 + C1) / C2)</td>
<td>(\sqrt{(B4^2) - (4<em>B3</em>B5)})</td>
</tr>
<tr>
<td>2</td>
<td>x_2</td>
<td>((-B4 - C1) / C2)</td>
<td>(2*B3)</td>
</tr>
<tr>
<td>3</td>
<td>a</td>
<td>9</td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>b</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>c</td>
<td>-2</td>
<td></td>
</tr>
</tbody>
</table>

Note how the square-root term \((y)\) is calculated in cell \(C1\), and the denominator term \((z)\) in cell \(C2\). This makes the two final formulae (in cells \(B1\) and \(B2\)) simpler to interpret. The positioning of all these cells on the grid is completely arbitrary\(^{10}\) – all that matters is that they properly reference each other in the formulae.

Spreadsheets are particularly useful for situations where the same set of calculations representing a circuit or other system must be repeated for different initial conditions. The power of a spreadsheet is that it automates what would otherwise be a tedious set of calculations. One specific application of this is to simulate the effects of various components within a circuit failing with abnormal values (e.g. a shorted resistor simulated by making its value nearly zero; an open resistor simulated by making its value extremely large). Another application is analyzing the behavior of a circuit design given new components that are out of specification, and/or aging components experiencing drift over time.

\(^{10}\)My personal preference is to locate all the “given” data in the upper-left cells of the spreadsheet grid (each data point flanked by a sensible name in the cell to the left and units of measurement in the cell to the right as illustrated in the first distance/time spreadsheet example), sometimes coloring them in order to clearly distinguish which cells contain entered data versus which cells contain computed results from formulae. I like to place all formulae in cells below the given data, and try to arrange them in logical order so that anyone examining my spreadsheet will be able to figure out how I constructed a solution. This is a general principle I believe all computer programmers should follow: document and arrange your code to make it easy for other people to learn from it.
4.2.3 Split DC voltage source measurements

Many types of electronic circuits use what is called a *split* or a *dual* power supply:

![Electronic circuit diagram]

Determine what a digital voltmeter would indicate if connected between the following points:

- Red lead on “A”, black lead on ground
- Red lead on “B”, black lead on ground
- Red lead on “A”, black lead on “B”
- Red lead on “B”, black lead on “A”

**Challenges**

- What would an analog voltmeter (VOM) indicate if connected in the same manner?
4.2.4 VOM measurement interpretation

Determine the quantity measured by this VOM, given the pointer’s position shown below, and the various range settings below that:

- Range = 100 Volts DC
- Range = 50 $\mu$A AC
- Range = Ohms $\times$ 10,000

Suppose a 5.25 Ampere current passes through a 1.6 Ohm resistor, and this meter is used to measure the resistor’s voltage drop. Assuming the meter is set to the 10 Volt DC range, where would its pointer indicate on the scale?

Suppose a 6 V source were connected to a 10 k$\Omega$ resistor, and this meter used to measure the resistor’s current while set to its 1 mA DC current range. Where would the meter’s pointer indicate along its scale?

**Challenges**

- Identify potential points of confusion for anyone interpreting the pointer’s position.
4.2.5 De-sensitizing an analog meter movement

The D’Arsonval meter movements used to build analog multimeters are extremely sensitive, usually requiring a milliAmpere or less of current through their moving coils to drive the pointer full-scale. If we were to connect one of these sensitive meter movements directly to a substantial electrical source such as a battery, the result would likely be destruction of the mechanism due to overcurrent and mechanical over-stress.

Determine what other component(s) must be connected to the following meter movement to limit the current through its coil, so that connecting the circuit to a 6-Volt battery results in the meter’s pointer moving exactly to the full-scale position. This will turn the meter movement into an analog voltmeter with a range of 0-6 Volts:

\[ \text{F.S.} = 1 \text{ mA} \quad R_{\text{coil}} = 400 \Omega \]

Challenges

- Modify this meter circuit to give it multiple voltage-measurement ranges.
4.2.6 Multi-range analog voltmeter circuit

Calculate the necessary resistance values to give this multi-range voltmeter the ranges indicated by the selector switch positions:

F.S. = 50 µA  
R_{coil} = 1 kΩ

2 V  50 V  100 V
10 V  25 V

- \( R_1 = \) 
- \( R_2 = \) 
- \( R_3 = \) 
- \( R_4 = \) 
- \( R_5 = \)

Challenges

- Calculate the Ohms-per-Volt sensitivity of this meter.
4.2.7  Another multi-range analog voltmeter circuit

Calculate the necessary resistance values to give this multi-range voltmeter the ranges indicated by the selector switch positions:

- $R_1 =$
- $R_2 =$
- $R_3 =$
- $R_4 =$
- $R_5 =$

**Challenges**

- Calculate the Ohms-per-Volt sensitivity of this meter.
- Which resistor should you calculate the value of first, and why?
4.2.8 Determining voltmeter range values

Determine the different range values of this multi-range voltmeter:

\[ F.S. = 50 \, \mu A \quad R_{col} = 750 \, \Omega \]

\[ R_1 = 199.25 \, k\Omega \]
\[ R_2 = 499.25 \, k\Omega \]
\[ R_3 = 999.25 \, k\Omega \]

All components on the printed circuit board are “surface-mount”, soldered onto the top surfaces of the copper traces. The switch (SW1) schematic diagram is shown to the immediate right of the circuit board, with resistor values shown below the circuit board.

Challenges

- Calculate the Ohms-per-Volt sensitivity of this meter.
- Modify this meter circuit to give it a 250 Volt range.
4.3 Diagnostic reasoning

These questions are designed to stimulate your deductive and inductive thinking, where you must apply general principles to specific scenarios (deductive) and also derive conclusions about the failed circuit from specific details (inductive). In a Socratic discussion with your instructor, the goal is for these questions to reinforce your recall and use of general circuit principles and also challenge your ability to integrate multiple symptoms into a sensible explanation of what’s wrong in a circuit. Your instructor may also pose additional questions based on those assigned, in order to further challenge and sharpen your diagnostic abilities.

As always, your goal is to fully explain your analysis of each problem. Simply obtaining a correct answer is not good enough – you must also demonstrate sound reasoning in order to successfully complete the assignment. Your instructor’s responsibility is to probe and challenge your understanding of the relevant principles and analytical processes in order to ensure you have a strong foundation upon which to build further understanding.

You will note a conspicuous lack of answers given for these diagnostic questions. Unlike standard textbooks where answers to every other question are given somewhere toward the back of the book, here in these learning modules students must rely on other means to check their work. The best way by far is to debate the answers with fellow students and also with the instructor during the Socratic dialogue sessions intended to be used with these learning modules. Reasoning through challenging questions with other people is an excellent tool for developing strong reasoning skills.

Another means of checking your diagnostic answers, where applicable, is to use circuit simulation software to explore the effects of faults placed in circuits. For example, if one of these diagnostic questions requires that you predict the effect of an open or a short in a circuit, you may check the validity of your work by simulating that same fault (substituting a very high resistance in place of that component for an open, and substituting a very low resistance for a short) within software and seeing if the results agree.
4.3.1 Voltage measurements in a switched circuit

Determine what these four multimeters (A, B, C, D) will register when connected to this circuit in the following positions (assume a battery voltage of 6 Volts):

- Meter A =
- Meter B =
- Meter C =
- Meter D =
Next, determine what the multimeters will register in the same circuit with the switch in the opposite state:

- Meter A =
- Meter B =
- Meter C =
- Meter D =

**Challenges**

- Explain how you could use one of these multimeters to measure the lamp’s current.
4.3.2 Voltage measurements by test points

A common convention when specifying DC voltage measurements is to use lettered subscripts denoting test points in a circuit that the meter’s leads will contact, the first test point being the meter’s red test lead and the second test point being the meter’s black test lead. Determine what this voltmeter will register when its test leads are connected to the following points in the circuit, being sure to specify whether the measured voltage will register as a positive or a negative quantity on the meter’s digital display:

For example, $V_{AB}$ denotes connecting the voltmeter’s red test lead to point A and its black test lead to point B.

- $V_{AB} =$
- $V_{EC} =$
- $V_{FB} =$
- $V_{CD} =$
- $V_{FA} =$
Now, do the same for the circuit with the switch in the open (off) position:

For example, $V_{AB}$ denotes connecting the voltmeter’s red test lead to point A and its black test lead to point B.

- $V_{AB} =$
- $V_{EC} =$
- $V_{FB} =$
- $V_{CD} =$
- $V_{FA} =$

**Challenges**

- Explain how you could configure the multimeter to measure the lamp’s current.
4.3.3 Malfunctioning multi-range analog voltmeter

What if this voltmeter suddenly stopped working when set in its middle range. The upper and lower ranges still function just fine, though. Identify the most likely source of the problem.

Challenges

- Explain how you could verify this fault without using another meter.
Appendix A

Problem-Solving Strategies

The ability to solve complex problems is arguably one of the most valuable skills one can possess, and this skill is particularly important in any science-based discipline.

- **Study principles, not procedures.** Don’t be satisfied with merely knowing how to compute solutions – learn *why* those solutions work.

- **Identify what it is you need to solve, identify all relevant data, identify all units of measurement, identify any general principles or formulae linking the given information to the solution, and then identify any “missing pieces” to a solution.** Annotate all diagrams with this data.

- **Sketch a diagram** to help visualize the problem. When building a real system, always devise a plan for that system and analyze its function before constructing it.

- **Follow the units of measurement and meaning of every calculation.** If you are ever performing mathematical calculations as part of a problem-solving procedure, and you find yourself unable to apply each and every intermediate result to some aspect of the problem, it means you don’t understand what you are doing. Properly done, every mathematical result should have practical meaning for the problem, and not just be an abstract number. You should be able to identify the proper units of measurement for each and every calculated result, and show where that result fits into the problem.

- **Perform “thought experiments”** to explore the effects of different conditions for theoretical problems. When troubleshooting real systems, perform *diagnostic tests* rather than visually inspecting for faults, the best diagnostic test being the one giving you the most information about the nature and/or location of the fault with the fewest steps.

- **Simplify the problem** until the solution becomes obvious, and then use that obvious case as a model to follow in solving the more complex version of the problem.

- **Check for exceptions** to see if your solution is incorrect or incomplete. A good solution will work for *all* known conditions and criteria. A good example of this is the process of testing scientific hypotheses: the task of a scientist is not to find support for a new idea, but rather to *challenge* that new idea to see if it holds up under a battery of tests. The philosophical
principle of *reductio ad absurdum* (i.e. disproving a general idea by finding a specific case where it fails) is useful here.

- **Work “backward”** from a hypothetical solution to a new set of given conditions.
- **Add quantities** to problems that are qualitative in nature, because sometimes a little math helps illuminate the scenario.
- **Sketch graphs** illustrating how variables relate to each other. These may be quantitative (i.e. with realistic number values) or qualitative (i.e. simply showing increases and decreases).
- **Treat quantitative problems as qualitative** in order to discern the relative magnitudes and/or directions of change of the relevant variables. For example, try determining what happens if a certain variable were to increase or decrease before attempting to precisely calculate quantities: how will each of the dependent variables respond, by increasing, decreasing, or remaining the same as before?
- **Consider limiting cases.** This works especially well for qualitative problems where you need to determine which direction a variable will change. Take the given condition and magnify that condition to an extreme degree as a way of simplifying the direction of the system’s response.
- **Check your work.** This means regularly testing your conclusions to see if they make sense. This does *not* mean repeating the same steps originally used to obtain the conclusion(s), but rather to use some other means to check validity. Simply repeating procedures often leads to *repeating the same errors* if any were made, which is why alternative paths are better.
Appendix B

Instructional philosophy

“The unexamined circuit is not worth energizing” – Socrates (if he had taught electricity)

These learning modules, although useful for self-study, were designed to be used in a formal learning environment where a subject-matter expert challenges students to digest the content and exercise their critical thinking abilities in the answering of questions and in the construction and testing of working circuits.

The following principles inform the instructional and assessment philosophies embodied in these learning modules:

• The first goal of education is to enhance clear and independent thought, in order that every student reach their fullest potential in a highly complex and inter-dependent world. Robust reasoning is always more important than particulars of any subject matter, because its application is universal.

• Literacy is fundamental to independent learning and thought because text continues to be the most efficient way to communicate complex ideas over space and time. Those who cannot read with ease are limited in their ability to acquire knowledge and perspective.

• Articulate communication is fundamental to work that is complex and interdisciplinary.

• Faulty assumptions and poor reasoning are best corrected through challenge, not presentation. The rhetorical technique of reductio ad absurdum (disproving an assertion by exposing an absurdity) works well to discipline student’s minds, not only to correct the problem at hand but also to learn how to detect and correct future errors.

• Important principles should be repeatedly explored and widely applied throughout a course of study, not only to reinforce their importance and help ensure their mastery, but also to showcase the interconnectedness and utility of knowledge.
These learning modules were expressly designed to be used in an “inverted” teaching environment\(^1\) where students first read the introductory and tutorial chapters on their own, then individually attempt to answer the questions and construct working circuits according to the experiment and project guidelines. The instructor never lectures, but instead meets regularly with each individual student to review their progress, answer questions, identify misconceptions, and challenge the student to new depths of understanding through further questionering. Regular meetings between instructor and student should resemble a Socratic\(^2\) dialogue, where questions serve as scalpels to dissect topics and expose assumptions. The student passes each module only after consistently demonstrating their ability to logically analyze and correctly apply all major concepts in each question or project/experiment. The instructor must be vigilant in probing each student’s understanding to ensure they are truly reasoning and not just memorizing. This is why “Challenge” points appear throughout, as prompts for students to think deeper about topics and as starting points for instructor queries. Sometimes these challenge points require additional knowledge that hasn’t been covered in the series to answer in full. This is okay, as the major purpose of the Challenges is to stimulate analysis and synthesis on the part of each student.

The instructor must possess enough mastery of the subject matter and awareness of students’ reasoning to generate their own follow-up questions to practically any student response. Even completely correct answers given by the student should be challenged by the instructor for the purpose of having students practice articulating their thoughts and defending their reasoning. Conceptual errors committed by the student should be exposed and corrected not by direct instruction, but rather by reducing the errors to an absurdity\(^3\) through well-chosen questions and thought experiments posed by the instructor. Becoming proficient at this style of instruction requires time and dedication, but the positive effects on critical thinking for both student and instructor are spectacular.

An inspection of these learning modules reveals certain unique characteristics. One of these is a bias toward thorough explanations in the tutorial chapters. Without a live instructor to explain concepts and applications to students, the text itself must fulfill this role. This philosophy results in lengthier explanations than what you might typically find in a textbook, each step of the reasoning process fully explained, including footnotes addressing common questions and concerns students raise while learning these concepts. Each tutorial seeks to not only explain each major concept in sufficient detail, but also to explain the logic of each concept and how each may be developed.

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\(^1\)In a traditional teaching environment, students first encounter new information via lecture from an expert, and then independently apply that information via homework. In an “inverted” course of study, students first encounter new information via homework, and then independently apply that information under the scrutiny of an expert. The expert’s role in lecture is to simply explain, but the expert’s role in an inverted session is to challenge, critique, and if necessary explain where gaps in understanding still exist.

\(^2\)Socrates is a figure in ancient Greek philosophy famous for his unflinching style of questioning. Although he authored no texts, he appears as a character in Plato’s many writings. The essence of Socratic philosophy is to leave no question unexamined and no point of view unchallenged. While purists may argue a topic such as electric circuits is too narrow for a true Socratic-style dialogue, I would argue that the essential thought processes involved with scientific reasoning on any topic are not far removed from the Socratic ideal, and that students of electricity and electronics would do very well to challenge assumptions, pose thought experiments, identify fallacies, and otherwise employ the arsenal of critical thinking skills modeled by Socrates.

\(^3\)This rhetorical technique is known by the Latin phrase *reductio ad absurdum*. The concept is to expose errors by counter-example, since only one solid counter-example is necessary to disprove a universal claim. As an example of this, consider the common misconception among beginning students of electricity that voltage cannot exist without current. One way to apply *reductio ad absurdum* to this statement is to ask how much current passes through a fully-charged battery connected to nothing (i.e. a clear example of voltage existing without current).
from “first principles”. Again, this reflects the goal of developing clear and independent thought in students’ minds, by showing how clear and logical thought was used to forge each concept. Students benefit from witnessing a model of clear thinking in action, and these tutorials strive to be just that.

Another characteristic of these learning modules is a lack of step-by-step instructions in the Project and Experiment chapters. Unlike many modern workbooks and laboratory guides where step-by-step instructions are prescribed for each experiment, these modules take the approach that students must learn to closely read the tutorials and apply their own reasoning to identify the appropriate experimental steps. Sometimes these steps are plainly declared in the text, just not as a set of enumerated points. At other times certain steps are implied, an example being assumed competence in test equipment use where the student should not need to be told again how to use their multimeter because that was thoroughly explained in previous lessons. In some circumstances no steps are given at all, leaving the entire procedure up to the student.

This lack of prescription is not a flaw, but rather a feature. Close reading and clear thinking are foundational principles of this learning series, and in keeping with this philosophy all activities are designed to require those behaviors. Some students may find the lack of prescription frustrating, because it demands more from them than what their previous educational experiences required. This frustration should be interpreted as an unfamiliarity with autonomous thinking, a problem which must be corrected if the student is ever to become a self-directed learner and effective problem-solver. Ultimately, the need for students to read closely and think clearly is more important both in the near-term and far-term than any specific facet of the subject matter at hand. If a student takes longer than expected to complete a module because they are forced to outline, digest, and reason on their own, so be it. The future gains enjoyed by developing this mental discipline will be well worth the additional effort and delay.

Another feature of these learning modules is that they do not treat topics in isolation. Rather, important concepts are introduced early in the series, and appear repeatedly as stepping-stones toward other concepts in subsequent modules. This helps to avoid the “compartmentalization” of knowledge, demonstrating the inter-connectedness of concepts and simultaneously reinforcing them. Each module is fairly complete in itself, reserving the beginning of its tutorial to a review of foundational concepts.

This methodology of assigning text-based modules to students for digestion and then using Socratic dialogue to assess progress and hone students’ thinking was developed over a period of several years by the author with his Electronics and Instrumentation students at the two-year college level. While decidedly unconventional and sometimes even unsettling for students accustomed to a more passive lecture environment, this instructional philosophy has proven its ability to convey conceptual mastery, foster careful analysis, and enhance employability so much better than lecture that the author refuses to ever teach by lecture again.

Problems which often go undiagnosed in a lecture environment are laid bare in this “inverted” format where students must articulate and logically defend their reasoning. This, too, may be unsettling for students accustomed to lecture sessions where the instructor cannot tell for sure who comprehends and who does not, and this vulnerability necessitates sensitivity on the part of the “inverted” session instructor in order that students never feel discouraged by having their errors exposed. Everyone makes mistakes from time to time, and learning is a lifelong process! Part of the instructor’s job is to build a culture of learning among the students where errors are not seen as shameful, but rather as opportunities for progress.
To this end, instructors managing courses based on these modules should adhere to the following principles:

- Student questions are always welcome and demand thorough, honest answers. The only type of question an instructor should refuse to answer is one the student should be able to easily answer on their own. Remember, the fundamental goal of education is for each student to learn to think clearly and independently. This requires hard work on the part of the student, which no instructor should ever circumvent. Anything done to bypass the student’s responsibility to do that hard work ultimately limits that student’s potential and thereby does real harm.

- It is not only permissible, but encouraged, to answer a student’s question by asking questions in return, these follow-up questions designed to guide the student to reach a correct answer through their own reasoning.

- All student answers demand to be challenged by the instructor and/or by other students. This includes both correct and incorrect answers – the goal is to practice the articulation and defense of one’s own reasoning.

- No reading assignment is deemed complete unless and until the student demonstrates their ability to accurately summarize the major points in their own terms. Recitation of the original text is unacceptable. This is why every module contains an “Outline and reflections” question as well as a “Foundational concepts” question in the Conceptual reasoning section, to prompt reflective reading.

- No assigned question is deemed answered unless and until the student demonstrates their ability to consistently and correctly apply the concepts to variations of that question. This is why module questions typically contain multiple “Challenges” suggesting different applications of the concept(s) as well as variations on the same theme(s). Instructors are encouraged to devise as many of their own “Challenges” as they are able, in order to have a multitude of ways ready to probe students’ understanding.

- No assigned experiment or project is deemed complete unless and until the student demonstrates the task in action. If this cannot be done “live” before the instructor, video-recordings showing the demonstration are acceptable. All relevant safety precautions must be followed, all test equipment must be used correctly, and the student must be able to properly explain all results. The student must also successfully answer all Challenges presented by the instructor for that experiment or project.
Students learning from these modules would do well to abide by the following principles:

- No text should be considered fully and adequately read unless and until you can express every idea in your own words, using your own examples.

- You should always articulate your thoughts as you read the text, noting points of agreement, confusion, and epiphanies. Feel free to print the text on paper and then write your notes in the margins. Alternatively, keep a journal for your own reflections as you read. This is truly a helpful tool when digesting complicated concepts.

- Never take the easy path of highlighting or underlining important text. Instead, summarize and/or comment on the text using your own words. This actively engages your mind, allowing you to more clearly perceive points of confusion or misunderstanding on your own.

- A very helpful strategy when learning new concepts is to place yourself in the role of a teacher, if only as a mental exercise. Either explain what you have recently learned to someone else, or at least imagine yourself explaining what you have learned to someone else. The simple act of having to articulate new knowledge and skill forces you to take on a different perspective, and will help reveal weaknesses in your understanding.

- Perform each and every mathematical calculation and thought experiment shown in the text on your own, referring back to the text to see that your results agree. This may seem trivial and unnecessary, but it is critically important to ensuring you actually understand what is presented, especially when the concepts at hand are complicated and easy to misunderstand. Apply this same strategy to become proficient in the use of circuit simulation software, checking to see if your simulated results agree with the results shown in the text.

- Above all, recognize that learning is hard work, and that a certain level of frustration is unavoidable. There are times when you will struggle to grasp some of these concepts, and that struggle is a natural thing. Take heart that it will yield with persistent and varied effort, and never give up!

Students interested in using these modules for self-study will also find them beneficial, although the onus of responsibility for thoroughly reading and answering questions will of course lie with that individual alone. If a qualified instructor is not available to challenge students, a workable alternative is for students to form study groups where they challenge one another.

To high standards of education,

Tony R. Kuphaldt

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4 As the old saying goes, “Insanity is trying the same thing over and over again, expecting different results.” If you find yourself stumped by something in the text, you should attempt a different approach. Alter the thought experiment, change the mathematical parameters, do whatever you can to see the problem in a slightly different light, and then the solution will often present itself more readily.

5 Avoid the temptation to simply share answers with study partners, as this is really counter-productive to learning. Always bear in mind that the answer to any question is far less important in the long run than the method(s) used to obtain that answer. The goal of education is to empower one’s life through the improvement of clear and independent thought, literacy, expression, and various practical skills.
Appendix C

Tools used

I am indebted to the developers of many open-source software applications in the creation of these learning modules. The following is a list of these applications with some commentary on each.

You will notice a theme common to many of these applications: a bias toward code. Although I am by no means an expert programmer in any computer language, I understand and appreciate the flexibility offered by code-based applications where the user (you) enters commands into a plain ASCII text file, which the software then reads and processes to create the final output. Code-based computer applications are by their very nature extensible, while WYSIWYG (What You See Is What You Get) applications are generally limited to whatever user interface the developer makes for you.

The GNU/Linux computer operating system

There is so much to be said about Linus Torvalds’ Linux and Richard Stallman’s GNU project. First, to credit just these two individuals is to fail to do justice to the mob of passionate volunteers who contributed to make this amazing software a reality. I first learned of Linux back in 1996, and have been using this operating system on my personal computers almost exclusively since then. It is free, it is completely configurable, and it permits the continued use of highly efficient Unix applications and scripting languages (e.g. shell scripts, Makefiles, sed, awk) developed over many decades. Linux not only provided me with a powerful computing platform, but its open design served to inspire my life’s work of creating open-source educational resources.

Bram Moolenaar’s Vim text editor

Writing code for any code-based computer application requires a text editor, which may be thought of as a word processor strictly limited to outputting plain-ASCII text files. Many good text editors exist, and one’s choice of text editor seems to be a deeply personal matter within the programming world. I prefer Vim because it operates very similarly to vi which is ubiquitous on Unix/Linux operating systems, and because it may be entirely operated via keyboard (i.e. no mouse required) which makes it fast to use.
Donald Knuth’s \TeX typesetting system

Developed in the late 1970’s and early 1980’s by computer scientist extraordinaire Donald Knuth to typeset his multi-volume magnum opus *The Art of Computer Programming*, this software allows the production of formatted text for screen-viewing or paper printing, all by writing plain-text code to describe how the formatted text is supposed to appear. \TeX is not just a markup language for documents, but it is also a Turing-complete programming language in and of itself, allowing useful algorithms to be created to control the production of documents. Simply put, \TeX *is a programmer’s approach to word processing.* Since \TeX is controlled by code written in a plain-text file, this means anyone may read that plain-text file to see exactly how the document was created. This openness afforded by the code-based nature of \TeX makes it relatively easy to learn how other people have created their own \TeX documents. By contrast, examining a beautiful document created in a conventional WYSIWYG word processor such as Microsoft Word suggests nothing to the reader about how that document was created, or what the user might do to create something similar. As Mr. Knuth himself once quipped, conventional word processing applications should be called WYSIAYG (What You See Is All You Get).

Leslie Lamport’s \LaTeX extensions to \TeX

Like all true programming languages, \TeX is inherently extensible. So, years after the release of \TeX to the public, Leslie Lamport decided to create a massive extension allowing easier compilation of book-length documents. The result was \LaTeX, which is the markup language used to create all ModEL module documents. You could say that \TeX is to \LaTeX as \C is to \C++. This means it is permissible to use any and all \TeX commands within \LaTeX source code, and it all still works. Some of the features offered by \LaTeX that would be challenging to implement in \TeX include automatic index and table-of-content creation.

Tim Edwards’ \Xcircuit drafting program

This wonderful program is what I use to create all the schematic diagrams and illustrations (but not photographic images or mathematical plots) throughout the ModEL project. It natively outputs PostScript format which is a true vector graphic format (this is why the images do not pixellate when you zoom in for a closer view), and it is so simple to use that I have never had to read the manual! Object libraries are easy to create for \Xcircuit, being plain-text files using PostScript programming conventions. Over the years I have collected a large set of object libraries useful for drawing electrical and electronic schematics, pictorial diagrams, and other technical illustrations.
**Gimp** graphic image manipulation program

Essentially an open-source clone of Adobe’s **PhotoShop**, I use **Gimp** to resize, crop, and convert file formats for all of the photographic images appearing in the ModEL modules. Although **Gimp** does offer its own scripting language (called **Script-Fu**), I have never had occasion to use it. Thus, my utilization of **Gimp** to merely crop, resize, and convert graphic images is akin to using a sword to slice bread.

**SPICE** circuit simulation program

**SPICE** is to circuit analysis as **\TeX** is to document creation: it is a form of markup language designed to describe a certain object to be processed in plain-ASCII text. When the plain-text “source file” is compiled by the software, it outputs the final result. More modern circuit analysis tools certainly exist, but I prefer **SPICE** for the following reasons: it is *free*, it is *fast*, it is *reliable*, and it is a fantastic tool for *teaching* students of electricity and electronics how to write simple code. I happen to use rather old versions of **SPICE**, version 2g6 being my “go to” application when I only require text-based output. **NGSPICE** (version 26), which is based on Berkeley **SPICE** version 3f5, is used when I require graphical output for such things as time-domain waveforms and Bode plots. In all **SPICE** example netlists I strive to use coding conventions compatible with all **SPICE** versions.

Andrew D. Hwang’s **ePiX** mathematical visualization programming library

This amazing project is a **C++** library you may link to any **C/C++** code for the purpose of generating PostScript graphic images of mathematical functions. As a completely free and open-source project, it does all the plotting I would otherwise use a Computer Algebra System (CAS) such as **Mathematica** or **Maple** to do. It should be said that **ePiX** is *not* a Computer Algebra System like **Mathematica** or **Maple**, but merely a mathematical *visualization* tool. In other words, it won’t determine integrals for you (you’ll have to implement that in your own **C/C++** code!), but it can graph the results, and it does so beautifully. What I really admire about **ePiX** is that it is a **C++** programming library, which means it builds on the existing power and toolset available with that programming language. Mr. Hwang could have probably developed his own stand-alone application for mathematical plotting, but by creating a **C++** library to do the same thing he accomplished something much greater.
Another open-source tool for mathematical visualization is gnuplot. Interestingly, this tool is not part of Richard Stallman’s GNU project, its name being a coincidence. For this reason the authors prefer “gnu” not be capitalized at all to avoid confusion. This is a much “lighter-weight” alternative to a spreadsheet for plotting tabular data, and the fact that it easily outputs directly to an X11 console or a file in a number of different graphical formats (including PostScript) is very helpful. I typically set my gnuplot output format to default (X11 on my Linux PC) for quick viewing while I’m developing a visualization, then switch to PostScript file export once the visual is ready to include in the document(s) I’m writing. As with my use of Gimp to do rudimentary image editing, my use of gnuplot only scratches the surface of its capabilities, but the important points are that it’s free and that it works well.

Both Python and C++ find extensive use in these modules as instructional aids and exercises, but I’m listing Python here as a tool for myself because I use it almost daily as a calculator. If you open a Python interpreter console and type from math import * you can type mathematical expressions and have it return results just as you would on a hand calculator. Complex-number (i.e. phasor) arithmetic is similarly supported if you include the complex-math library (from cmath import *). Examples of this are shown in the Programming References chapter (if included) in each module. Of course, being a fully-featured programming language, Python also supports conditionals, loops, and other structures useful for calculation of quantities. Also, running in a console environment where all entries and returned values show as text in a chronologically-ordered list makes it easy to copy-and-paste those calculations to document exactly how they were performed.
Appendix D

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Appendix E

References
Appendix F

Version history

This is a list showing all significant additions, corrections, and other edits made to this learning module. Each entry is referenced by calendar date in reverse chronological order (newest version first), which appears on the front cover of every learning module for easy reference. Any contributors to this open-source document are listed here as well.

27 November 2022 – placed questions at the top of the itemized list in the Introduction chapter prompting students to devise experiments related to the tutorial content.

30-31 August 2022 – added more parts to the “VOM measurement interpretation” Quantitative Reasoning question, and corrected several spelling errors throughout the document. Also made minor edits to the Tutorial.

21 March 2022 – added old NASA photograph showing a Simpson 260 VOM in use, as well as some explanatory text contrasting DMMs and VOMs.

1 September 2021 – minor additions to the Introduction chapter.

23 July 2021 – reduced the number of references to Ohm’s Law in the Tutorial, to make it more suitable for readers who have not yet studied Ohm’s Law.

18 July 2021 – added an “Applying foundational concepts...” question to the Conceptual Reasoning section of the Questions chapter.

9 June 2021 – minor updates to graphic images of DMMs.

17 May 2021 – added review section on series versus parallel networks.

28 January 2021 – added content to the Introduction chapter, as well as a new Diagnostic Question (“Voltage measurements by test points”).

12 September 2020 – added photograph of a D’Arsonval meter movement to the Tutorial.

24 August 2020 – significantly edited the Introduction chapter to make it more suitable as a
pre-study guide and to provide cues useful to instructors leading “inverted” teaching sessions.

25-27 May 2020 – added more content to the Tutorial chapter, and added questions.

10-11 April 2020 – added more content to the Tutorial chapter.

3 April 2020 – moved filename from mod_dmm.latex to mod_mm.latex and title from “Digital Multimeters” to simply “Multimeters”.

September 2018 – document first created.
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