## DC circuit calculations

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## Question 1

In a series circuit, certain general principles may be stated with regard to quantities of voltage, current, resistance, and power. Complete these sentences, each one describing a fundamental principle of series circuits:
"In a series circuit, voltage . . ."
"In a series circuit, current . . ."
"In a series circuit, resistance . . ."
"In a series circuit, power . . ."
For each of these rules, explain $w h y$ it is true.
file i01140

## Question 2

Explain, step by step, how to calculate the amount of current $(I)$ that will go through each resistor in this series circuit, and also the current $(I)$ supplied by the DC voltage source:

file i01236

Question 3
Determine the amount of voltage dropped by each resistor in this circuit, if each resistor has a color code of Brn, Blk, Red, Gld (assume perfectly precise resistance values - $0 \%$ error):


Also, determine the following information about this circuit:

- Current through each resistor
- Power dissipated by each resistor
- Ratio of each resistor's voltage drop to battery voltage $\left(\frac{E_{R}}{E_{b a t}}\right)$
- Ratio of each resistor's resistance to the total circuit resistance $\left(\frac{R}{R_{t o t a l}}\right)$ file i01181

Question 4
Calculate the output voltages of these two voltage divider circuits $\left(V_{A}\right.$ and $\left.V_{B}\right)$ :


Now, calculate the voltage between points $\mathbf{A}$ (red lead) and $\mathbf{B}$ (black lead) $\left(V_{A B}\right)$. file i01238

Question 5
Calculate both the maximum and the minimum amount of voltage obtainable from this potentiometer circuit (as measured between the wiper and ground):

file i01131
Question 6
Suppose that an electric heater, which is nothing more than a large resistor, dissipates 500 watts of power when directly connected to a 110 volt source:


Now suppose that exact same heater is connected to one end of a long two-wire cable, which is then connected to the same 110 volt source. Assuming that each conductor within the cable has an end-to-end resistance of 3 ohms, how much power will the heater dissipate?

file i01139

Question 7
Suppose an analog voltmeter has a range of 0 to 10 volts, and an internal resistance of exactly $100 \mathrm{k} \Omega$ :


Show how a single resistor could be connected to this voltmeter to extend its range to 0 to 50 volts. Calculate the resistance of this "range" resistor, as well as its necessary power dissipation rating.
file i01138

## Question 8

Determine the voltages registered by a voltmeter between the following points in this circuit. Be sure to note whether the voltmeter's indication will be a positive value or a negative value in each case:

$V_{A}=$ $\qquad$ (red lead on A, black lead on ground)
$V_{B}=$ $\qquad$ (red lead on B, black lead on ground)
$V_{C}=$ $\qquad$ (red lead on $\mathbf{C}$, black lead on ground)
$V_{D}=$ $\qquad$ (red lead on $\mathbf{D}$, black lead on ground)
$V_{A C}=$ $\qquad$ (red lead on A, black lead on $\mathbf{C}$ )
$V_{D B}=$ $\qquad$ (red lead on $\mathbf{D}$, black lead on $\mathbf{B}$ )
$V_{B A}=$ $\qquad$ (red lead on B, black lead on $\mathbf{A}$ )
$V_{B C}=$ $\qquad$ (red lead on $\mathbf{B}$, black lead on $\mathbf{C}$ )
$V_{C D}=$ $\qquad$ (red lead on $\mathbf{C}$, black lead on $\mathbf{D}$ ) file i02520

Question 9
Calculate the amount of voltage between test points TP1 and TP3, and also the amount of voltage between test points TP2 and TP4:

$V_{T P 1-T P 3}=\quad V_{T P 2-T P 4}=$
file i01157
Question 10
In a parallel circuit, certain general principles may be stated with regard to quantities of voltage, current, resistance, and power. Complete these sentences, each one describing a fundamental principle of parallel circuits:
"In a parallel circuit, voltage . . ."
"In a parallel circuit, current . . ."
"In a parallel circuit, resistance . . ."
"In a parallel circuit, power . . ."
For each of these rules, explain why it is true.
file i01150
Question 11
Use Kirchhoff's Current Law to calculate the magnitude and direction of the current through resistor $R_{4}$ in this resistor network:


Note: all current arrows point in the direction of conventional flow!
file i01161

Question 12
Explain, step by step, how to calculate the amount of current $(I)$ that will go through each resistor in this parallel circuit, and also the current $(I)$ supplied by the DC voltage source:

file i01237
Question 13
Calculate the total amount of current that the battery must supply to this parallel circuit:


Now, using Ohm's Law, calculate total resistance ( $R_{\text {total }}$ ) from total (source) voltage $V_{\text {total }}$ and total (source) current $I_{\text {total }}$.
file i01149

## Question 14

Complete the table of values for this circuit:

file i01148

Question 15
Complete the table of values for this circuit:


|  | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | $\mathrm{R}_{4}$ | Total |
| :--- | :---: | :---: | :---: | :---: | :---: |
| V |  |  |  |  |  |
| I |  |  |  |  |  |
| R |  | $1 \mathrm{k} \Omega$ | $2.2 \mathrm{k} \Omega$ | $6.8 \mathrm{k} \Omega$ | $470 \Omega$ |
|  |  |  |  |  |  |
| P |  |  |  |  |  |
|  |  |  |  |  |  |

$\underline{\text { file } \mathrm{i} 01146}$
Question 16
The circuit shown here is commonly referred to as a current divider. Calculate the voltage dropped across each resistor, the current drawn by each resistor, and the total amount of electrical resistance "seen" by the 9 -volt battery:


- Current through the $2 \mathrm{k} \Omega$ resistor $=$
- Current through the $3 \mathrm{k} \Omega$ resistor $=$
- Current through the $5 \mathrm{k} \Omega$ resistor $=$
- Voltage across each resistor $=$
- $R_{\text {total }}=$
file i01147


## Question 17

Examine these two variable-resistance (rheostat) networks, each one with a large-range potentiometer and a small-range potentiometer:


For each network, determine which pot is the coarse adjustment and which pot is the fine adjustment for total network resistance, and explain your reasoning.

## Suggestions for Socratic discussion

- A good problem-solving technique is to perform a "thought experiment" on the given system. Here, determine the effect on total network resistance while each potentiometer (one at a time) is adjusted through its entire range while the other potentiometer is left in its mid-position.
file i03144

Identify which of these components are connected directly in series with each other, and which are connected directly in parallel with each other:

Figure 1


Figure 4


Figure 2


Figure 5


Figure 3


Figure 6


Assume that the open wire ends are connection points to a power source. file i01163

Question 19
Identify which of these components are connected directly in series with each other, and which are connected directly in parallel with each other:

Figure 1


Figure 4


Figure 2


Figure 5


Figure 3


Figure 6


Assume that the open wire ends are connection points to a power source. In circuits where ground symbols appear, consider ground as the other side of the power source.
file i01164

Calculate the resistance between points $\mathbf{A}$ and $\mathbf{B}\left(R_{A B}\right)$ for the following resistor networks:

Figure 1


Figure 2


Figure 5


Figure 3


Figure 6

file i01165
Question 21
Use Kirchhoff's Voltage Law to calculate the magnitude and polarity of the voltage across resistors $R_{2}$ and $R_{4}$ in this resistor network:

file i01156

Question 22
Imagine you are using a digital voltmeter to measure voltages between pairs of points in a circuit, following the sequence of steps shown in the following diagrams:

## Step 1



## Step 3



Step 2


Step 4


How much voltage would be registered by the voltmeter in each of the steps? Be sure to include the sign of the DC voltage measured (note the coloring of the voltmeter leads, with the red lead always on the first point denoted in the subscript: $V_{B A}=$ red lead on "B" and black lead on "A"):

- $V_{B A}=$
- $V_{D B}=$
- $V_{F D}=$
- $V_{A F}=$

What is the algebraic sum of these voltages?
file i01158

## Question 23

Calculate the amount of voltage dropped across resistor $R_{2}$ :


Also, note the direction of current through it and the polarity of the voltage drop across it. file i01166

Question 24
Complete the table of values for this circuit:

file i01169

Question 25
Suppose you were designing a circuit that required two LEDs for "power on" indication. The power supply voltage is 15 volts, and each LED is rated at 1.6 volts and 20 mA . Calculate the dropping resistor sizes and power ratings:


After doing this, a co-worker looks at your circuit and suggests a modification. Why not use a single dropping resistor for both LEDs, economizing the number of components necessary?


Re-calculate the dropping resistor ratings (resistance and power) for the new design. file i01170

Question 26
Calculate the current through the zener diode for the given values of input (source) voltage in this circuit:


- $V_{\text {source }}=25 \mathrm{~V} ; I_{\text {zener }}=$
- $V_{\text {source }}=20 \mathrm{~V} ; I_{\text {zener }}=$
- $V_{\text {source }}=15 \mathrm{~V} ; I_{\text {zener }}=$
- $V_{\text {source }}=10 \mathrm{~V} ; I_{\text {zener }}=$
- $V_{\text {source }}=5 \mathrm{~V} ; I_{\text {zener }}=$

Do you see any relationship between source voltage and zener diode current? If so, explain what that relationship is.
file i00757
Question 27
Complete the table of values for this circuit:

file i01167

Question 28
Complete the table of values for this circuit:


| $\mathrm{R}_{1}$ |  | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | $\mathrm{R}_{4}$ | $\mathrm{R}_{5}$ | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V |  |  |  |  |  |  |
| I |  |  |  |  |  |  |
| R | $220 \Omega$ | $130 \Omega$ | $470 \Omega$ | $100 \Omega$ | $270 \Omega$ |  |
| P |  |  |  |  |  |  |

file i01176
Question 29
Complete the table of values for this circuit:

file 101177

Question 30
Calculate the amount of voltage between points $\mathbf{A}$ and $\mathbf{B}$ in this circuit. You must sketch polarity marks $(+,-)$ on the schematic diagram to show the polarity of $V_{A B}$, as well as show all of your mathematical work!

file i02527

Question 31
Complete the table of values for this circuit:


| $\mathrm{R}_{1}$ |  | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | $\mathrm{R}_{4}$ | $\mathrm{R}_{5}$ | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V |  |  |  |  |  |  |
| I |  |  |  |  |  |  |
| R | $2 \mathrm{k} \Omega$ | $1 \mathrm{k} \Omega$ | $3.3 \mathrm{k} \Omega$ | $4.7 \mathrm{k} \Omega$ | $4.7 \mathrm{k} \Omega$ |  |
| P |  |  |  |  |  |  |

file i01179

Question 32
When the $5 \mathrm{k} \Omega$ potentiometer in this circuit is set to its $0 \%, 25 \%, 50 \%, 75 \%$, and $100 \%$ positions, the following output voltages are obtained (measured with respect to ground, of course):


- At $0 \%$ setting, $V_{\text {out }}=0 \mathrm{~V}$
- At $25 \%$ setting, $V_{\text {out }}=2.5 \mathrm{~V}$
- At $50 \%$ setting, $V_{\text {out }}=5 \mathrm{~V}$
- At $75 \%$ setting, $V_{\text {out }}=7.5 \mathrm{~V}$
- At $100 \%$ setting, $V_{\text {out }}=10 \mathrm{~V}$

Calculate what the output voltages will be if a $1 \mathrm{k} \Omega$ load resistor is connected between the " $V_{\text {out }}$ " terminal and ground:


- At $0 \%$ setting, $V_{\text {out }}=$
- At $25 \%$ setting, $V_{\text {out }}=$
- At $50 \%$ setting, $V_{\text {out }}=$
- At $75 \%$ setting, $V_{\text {out }}=$
- At $100 \%$ setting, $V_{\text {out }}=$ file i01132

Question 33
Determine the voltages (with respect to ground) at points $\mathbf{A}$ and $\mathbf{B}$ in this circuit under four different conditions: both loads off, load 1 on (only), load 2 on (only), and both loads on:


| Voltage | Both loads off | Load 1 on (only) | Load 2 on (only) | Both loads on |
| :---: | :---: | :---: | :---: | :---: |
| $V_{A}$ |  |  |  |  |
| $V_{B}$ |  |  |  |  |

file i01133
Question 34
One of the resistors in this voltage divider circuit is failed open. Based on the voltage readings shown at each load, determine which one it is:

file i01134

Question 35
One of the resistors in this voltage divider circuit is failed open. Based on the voltage readings shown at each load, determine which one it is:

file i01135
Question 36
One of the resistors in this voltage divider circuit is failed (either open or shorted). Based on the voltage readings shown at each load, determine which one and what type of failure it is:

file i01136

Question 37
Old vacuum-tube based electronic circuits often required several different voltage levels for proper operation. An easy way to obtain these different power supply voltages was to take a single, high-voltage power supply circuit and "divide" the total voltage into smaller divisions.

These voltage divider circuits also made provision for a small amount of "wasted" current through the divider called a bleeder current, designed to discharge the high voltage output of the power supply quickly when it was turned off.

Design a high-voltage divider to provide the following loads with their necessary voltages, plus a "bleeder" current of 5 mA (the amount of current going through resistor R4):

file i01137
Question 38
Calculate the necessary value of $R$ to create a voltage drop of 4 volts between test points $\mathbf{A}$ and $\mathbf{B}$ :

file i01272

Answers

## Answer 1

"In a series circuit, voltage drops add to equal the total."
This is an expression of Kirchhoff's Voltage Law (KVL), whereby the algebraic sum of all voltages in any loop must be equal to zero.
"In a series circuit, current is equal through all components."
This is true because a series circuit by definition has only one path for current to travel. Since charge carriers must move in unison or not at all (a consequence of the Conservation of Charge, whereby electric charges cannot be created or destroyed), the current measured at any one point in a series circuit must be the same as the current measured at any other point in that same circuit, at any given time.
"In a series circuit, resistances add to equal the total."
Each resistance in a series circuit acts to oppose electric current. When resistances are connected in series, their oppositions combine to form a greater total opposition because then same current must travel through every resistance.
"In a series circuit, power dissipations add to equal the total."
This is an expression of the Conservation of Energy, which states energy cannot be created or destroyed. Anywhere power is dissipated in any load of a circuit, that power must be accounted for back at the source, no matter how those loads might be connected to each other.

Answer 2
First we need to identify all the relevant principles for series circuits:

- The algebraic sum of all voltages in the circuit will be equal to zero (Kirchhoff's Voltage Law)
- Current is common throughout a series circuit, because there is only one path for current in the entire circuit
- Resistances add in series

We know the voltage of the source and the resistance of the three loads. However, we cannot simply apply Ohm's Law at this point because the source voltage is not impressed entirely on any one of the loads rather the source voltage will be split up proportionately amongst the three loads in accordance with KVL. It is important to always apply Ohm's Law in context: $V=I R$ is true only if $V, I$, and $R$ apply to the same component or set of components. Here, the 36 volts of the source applies to all three resistors, not to any one resistor.

However, we may apply the principle of resistances adding in series to arrive at a total resistance value for the circuit, which we may then apply to total voltage to find total current. Adding up the three resistors' values, we get a total resistance of $R_{\text {total }}=1500+10000+4700=16200$ ohms. Total circuit current is then calculated as follows:

$$
I=\frac{V}{R}=\frac{36 \mathrm{~V}}{16200 \Omega}=2.222 \mathrm{~mA}
$$

It is helpful to annotate all calculated values on the circuit schematic for easy reference. The reason this is helpful is because it applies a context to the calculated value. Here we will sketch arrows (in the direction of conventional flow) to document the 2.222 mA circuit current, based on the relationship between voltage and current for sources (i.e. current exits the positive pole of a source because the source is driving that current):


Since this is a series circuit, we know that this value of current ( 2.222 milliamps) will be common through all components. Now that we know the current through each resistor and the resistance of each resistor, we may apply Ohm's Law to each resistor individually as such:

$$
\begin{gathered}
V_{R 1}=I R_{1}=(2.222 \mathrm{~mA})(1500 \Omega)=3.333 \mathrm{~V} \\
V_{R 2}=I R_{2}=(2.222 \mathrm{~mA})(10000 \Omega)=22.222 \mathrm{~V} \\
V_{R 3}=I R_{3}=(2.222 \mathrm{~mA})(4700 \Omega)=10.444 \mathrm{~V}
\end{gathered}
$$

Once again it is recommended to annotate the circuit schematic with these calculated values, for the sake of keeping all calculations in context. The polarity $(+,-)$ of each voltage is important to note as well, and we know this by the relationship between voltage and current for loads (i.e. the positive pole of a load is the one where conventional flow enters, because the voltage dropped by a load is opposing current):


As a final check of our work, we may sum these three resistors' voltage drops to ensure they do indeed add up to equal the source voltage in accordance with KVL:

$$
3.333 \mathrm{~V}+22.222 \mathrm{~V}+10.444 \mathrm{~V}=36 \mathrm{~V}
$$

Answer 3
Voltage across each resistor $=1.5 \mathrm{~V}$

Current through each resistor $=1.5 \mathrm{~mA}$
Power dissipated by each resistor $=2.25 \mathrm{~mW}$
Voltage ratio $=\frac{1}{3}$
Resistance ratio $=\frac{1}{3}$
Answer 4
$V_{A}=+65.28 \mathrm{~V}$
$V_{B}=+23.26 \mathrm{~V}$
$V_{A B}=+42.02 \mathrm{~V}($ point $\mathbf{A}$ being positive relative to point $\mathbf{B})$
Answer 5

$$
\begin{aligned}
& V_{\max }=3.85 \mathrm{volts} \\
& V_{\min }=0.35 \mathrm{volts}
\end{aligned}
$$

[^0]Answer 7
The basic problem here is how to make the voltmeter see 10 volts while it's being connected to a source with a value of 50 volts. This will require a series resistor to drop the extra 40 volts:


A power dissipation rating of $\frac{1}{8}$ watt would be more than sufficient for this application.
Answer 8
$V_{A}=+30$ volts (red lead on $\mathbf{A}$, black lead on ground)
$V_{B}=+3$ volts (red lead on $\mathbf{B}$, black lead on ground)
$V_{C}=+9$ volts $($ red lead on $\mathbf{C}$, black lead on ground)
$V_{D}=-15$ volts (red lead on $\mathbf{D}$, black lead on ground)
$V_{A C}=+21$ volts $($ red lead on $\mathbf{A}$, black lead on $\mathbf{C})$
$V_{D B}=-18$ volts $($ red lead on $\mathbf{D}$, black lead on $\mathbf{B})$
$V_{B A}=\underline{-27 \text { volts }(\text { red lead on } \mathbf{B}, \text { black lead on } \mathbf{A}) ~}$
$V_{B C}=\underline{-6 \text { volts }(\text { red lead on } \mathbf{B} \text {, black lead on } \mathbf{C}) ~}$
$V_{C D}=+24$ volts $($ red lead on $\mathbf{C}$, black lead on $\mathbf{D})$
Answer 9
$V_{T P 1-T P 3}=15.83$ volts $\quad V_{T P 2-T P 4}=22.22$ volts

Answer 10
"In a parallel circuit, voltage is equal across all components."
This is true because a parallel circuit by definition is one where the constituent components all share the same two equipotential points.
"In a parallel circuit, currents add to equal the total."
This is an expression of Kirchhoff's Current Law (KCL), whereby the algebraic sum of all currents entering and exiting a node must be equal to zero.
"In a parallel circuit, resistances diminish to equal the total."
Each resistance in a parallel circuit provides another path for electric current. When resistances are connected in parallel, their combined total paths provide less opposition than any single path because the current is able to split up and proportionately follow these alternative paths.
"In a parallel circuit, power dissipations add to equal the total."
This is an expression of the Conservation of Energy, which states energy cannot be created or destroyed. Anywhere power is dissipated in any load of a circuit, that power must be accounted for back at the source, no matter how those loads might be connected to each other.

## Answer 11



## Note: all current arrows point in the direction of conventional flow!

## Answer 12

First we need to identify all the relevant principles for series circuits:

- The algebraic sum of all currents at a node will be equal to zero (Kirchhoff's Current Law)
- Voltage is common throughout a parallel circuit, because every component shares the same two equipotential points
- Resistances diminish in parallel

Following from the rule that voltage is common throughout a parallel circuit, we may conclude that each of the three resistors sees 36 volts from the source. Thus, we may immediately apply Ohm's Law to calculate current through each of the resistors, knowing the voltage across each resistor and the resistance of each resistor:

$$
\begin{aligned}
I_{R 1} & =\frac{V}{R_{1}}=\frac{36 \mathrm{~V}}{1500 \Omega}=24 \mathrm{~mA} \\
I_{R 2} & =\frac{V}{R_{2}}=\frac{36 \mathrm{~V}}{10000 \Omega}=3.6 \mathrm{~mA} \\
I_{R 3} & =\frac{V}{R_{3}}=\frac{36 \mathrm{~V}}{4700 \Omega}=7.660 \mathrm{~mA}
\end{aligned}
$$

It is helpful to annotate all calculated values on the circuit schematic for easy reference. The reason this is helpful is because it applies a context to the calculated value. Here we will sketch arrows (in the direction of conventional flow) to document all three resistor currents, based on the relationship between voltage and current for loads (i.e. current enters the positive pole of a load because the load is opposing that current):


From here we may apply KCL to calculate current values at the each node, knowing that every milliamp leaving a node must be matched by a milliamp of current entering the node. Current entering the upperright node, therefore, will be the sum of the two currents exiting that node. The same thing happens at the lower-right node, where two currents entering that node merge to form a larger current exiting:

$$
I=3.6 \mathrm{~mA}+7.660 \mathrm{~mA}=11.260 \mathrm{~mA}
$$

Once again we will document this calculated value on the circuit schematic to maintain its context:


Applying KCL to the upper-left and lower-left nodes, and annotating the schematic once again:

$$
I=24 \mathrm{~mA}+11.260 \mathrm{~mA}=35.260 \mathrm{~mA}
$$



With the arrows showing this 35.260 mA current, we can see it passes straight out of (and back in to) the 36 volt source, which means this is our total current value for the parallel circuit.

Answer 13

$$
\begin{aligned}
& I_{t o t a l}=40.0 \mathrm{~mA} \\
& R_{\text {total }}=250 \Omega
\end{aligned}
$$

Answer 14

|  | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | Total |
| :---: | :---: | :---: | :---: |
| V | 30 V | 30 V | 30 V |
| I | 3 mA | 9.09 mA | 12.09 mA |
| R | $10 \mathrm{k} \Omega$ | $3.3 \mathrm{k} \Omega$ | $2.481 \mathrm{k} \Omega$ |
| P | 90 mW | 272.7 mW | 362.7 mW |
|  |  |  |  |



|  |  | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | $\mathrm{R}_{4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Total |  |  |  |  |  |
| V | 4 V | 4 V | 4 V | 4 V | 4 V |
| I | 4 mA | 1.82 mA | $588.2 \mu \mathrm{~A}$ | 8.51 mA | 14.92 mA |
| R | $1 \mathrm{k} \Omega$ | $2.2 \mathrm{k} \Omega$ | $6.8 \mathrm{k} \Omega$ | $470 \Omega$ | $268.1 \Omega$ |
| P | 16 mW | 7.27 mW | 2.35 mW | 34.0 mW | 59.67 mW |
|  |  |  |  |  |  |

## Answer 16

- Current through the $2 \mathrm{k} \Omega$ resistor $=4.5 \mathrm{~mA}$
- Current through the $3 \mathrm{k} \Omega$ resistor $=3 \mathrm{~mA}$
- Current through the $5 \mathrm{k} \Omega$ resistor $=1.8 \mathrm{~mA}$
- Voltage across each resistor $=9$ volts
- $R_{\text {total }}=967.74 \Omega$


## Answer 17

## Series network

100k $=$ Coarse adjustment $; 5 \mathrm{k}=$ Fine adjustment

## Parallel network

$5 \mathrm{k}=$ Coarse adjustment ; 100k $=$ Fine adjustment
General principles to keep in mind here are that series resistances $a d d$ while parallel resistances diminish. The total resistance of a series network is always greater than any of its constituent resistances, and so the largest resistance in a series network tends to dominate. The total resistance of a parallel network is always less than any of its constituent resistances, and so the least resistance in a parallel network tends to dominate.

Answer 18
Figure 1:
R2 in parallel with R3.
Figure 2:
R1 in series with R2.
Figure 3:
R2 in series with R3.

Figure 4:
R1 in series with R2; R3 in series with R4.
Figure 5:
R1 in parallel with R3; R2 in parallel with R4.
Figure 6:
R1 in series with R2.
Answer 19
Figure 1:
R1 in series with SW1.
Figure 2:
R1 in series with R2; R3 in parallel with R4.
Figure 3:
R1 parallel with R2.
Figure 4:
R1 parallel with R2.
Figure 5:
L1 in series with C1.
Figure 6:
R3 in parallel with R4.

Answer 20
Figure 1:

$$
R_{A B}=500 \Omega
$$

Figure 2:

$$
R_{A B}=750 \Omega
$$

Figure 3:

$$
R_{A B}=1.511 \mathrm{k} \Omega
$$

Figure 4:

$$
R_{A B}=940 \Omega
$$

Figure 5:
$R_{A B}=880 \Omega$
Figure 6:
$R_{A B}=80.54 \Omega$
Answer 21


Answer 22

- $V_{B A}=+10.8$ volts
- $V_{D B}=+25.2$ volts
- $V_{F D}=-12.0$ volts
- $V_{A F}=-24.0$ volts


## Answer 23

$V_{R 2}=12.11$ volts, positive on top and negative on bottom. If you follow conventional flow notation, this means current goes down through resistor $R_{2}$. The actual flow of electrons through $R_{2}$, however, is up.

|  |  | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ |
| :---: | :---: | :---: | :---: | :---: |
| Total |  |  |  |  |
| V | 12.6 V | 2.4 V | 2.4 V | 15 V |
| I | $700 \mu \mathrm{~A}$ | $263.7 \mu \mathrm{~A}$ | $436.3 \mu \mathrm{~A}$ | $700 \mu \mathrm{~A}$ |
| R | $18 \mathrm{k} \Omega$ | $9.1 \mathrm{k} \Omega$ | $5.5 \mathrm{k} \Omega$ | $21.43 \mathrm{k} \Omega$ |
| P | 8.82 mW | $632.8 \mu \mathrm{~W}$ | 1.05 mW | 10.5 mW |
|  |  |  |  |  |

Answer 25
With two resistors: $R_{1}=R_{2}=670 \Omega$, rated for at least 0.268 watts $(1 / 2$ watt would be a practical rating).

With one resistor: $R_{1}=335 \Omega$, rated for at least 0.536 watts ( 1 watt would be a practical rating).

## Answer 26

As the source voltage decreases, zener diode current also decreases:

- $V_{\text {source }}=25 \mathrm{~V} ; I_{\text {zener }}=41.49 \mathrm{~mA}$
- $V_{\text {source }}=20 \mathrm{~V} ; I_{\text {zener }}=30.85 \mathrm{~mA}$
- $V_{\text {source }}=15 \mathrm{~V} ; I_{\text {zener }}=20.21 \mathrm{~mA}$
- $V_{\text {source }}=10 \mathrm{~V} ; I_{\text {zener }}=9.58 \mathrm{~mA}$
- $V_{\text {source }}=5 \mathrm{~V} ; I_{\text {zener }}=0 \mathrm{~mA}$

It should be noted that the calculated answers shown here will not precisely match a real zener diode circuit, due to the fact that zener diodes tend to gradually taper off in current as the applied voltage nears the zener voltage rating rather than current sharply dropping to zero as a simpler model would predict.

Answer 27

|  | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | Total |
| :---: | :---: | :---: | :---: | :---: |
| V | 1.778 V | 1.778 V | 10.22 V | 12 V |
| I | 8.079 mA | 13.67 mA | 21.75 mA | 21.75 mA |
| R | $220 \Omega$ | $130 \Omega$ | $470 \Omega$ | $551.7 \Omega$ |
| P | 14.36 mW | 24.30 mW | 222.3 mW | 261.0 mW |
|  |  |  |  |  |

Answer 28

|  | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | $\mathrm{R}_{4}$ | $\mathrm{R}_{5}$ | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3.978 V | 2.351 V | 6.328 V | 3.155 V | 8.517 V | 18 V |
| I | 18.08 mA | 18.08 mA | 13.46 mA | 31.55 mA | 31.55 mA | 31.55 mA |
| R | $220 \Omega$ | $130 \Omega$ | $470 \Omega$ | $100 \Omega$ | $270 \Omega$ | $570.6 \Omega$ |
| P | 21.92 mW | 42.50 mW | 85.21 mW | 99.51 mW | 268.7 mW | 567.8 mW |
|  |  | 71.92 |  |  |  |  |


|  | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | $\mathrm{R}_{4}$ | Total |
| :---: | :---: | :---: | :---: | :---: | :---: |
| V | 4.714 V | 6.286 V | 1.179 V | 3.536 V | 11 V |
| I | 4.714 mA | 12.57 mA | 7.857 mA | 7.857 mA | 12.57 mA |
| R | $1 \mathrm{k} \Omega$ | $500 \Omega$ | $150 \Omega$ | $450 \Omega$ | $875 \Omega$ |
| P | 22.22 mW | 79.02 mW | 9.26 mW | 27.78 mW | 138.3 mW |
|  |  |  |  |  |  |

Answer 30
$V_{\mathbf{A B}}=9.198$ volts, $\mathbf{A}$ positive and $\mathbf{B}$ negative.


The voltage between points A and B is the supply voltage ( 26 volts) minus the voltage drops across the 1 k and parallel subnetwork resistors. Alternatively, one could calculate $V_{A B}$ by adding the voltage drops of the 1 k and 270 ohm resistors.

The latter solution makes it easiest to see the polarity of $V_{A B}$ : noting how the voltage drops across the 1 k and 270 ohm resistors are additive, we see point A being the most positive and point B being the most negative.

Answer 31

|  | $\mathrm{R}_{1}$ | $\mathrm{R}_{2}$ | $\mathrm{R}_{3}$ | $\mathrm{R}_{4}$ | $\mathrm{R}_{5}$ | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V | 4.500 V | 676.6 mV | 2.233 V | 1.590 V | 1.590 V | 4.500 V |
| I | 2.250 mA | $676.7 \mu \mathrm{~A}$ | $676.7 \mu \mathrm{~A}$ | $338.3 \mu \mathrm{~A}$ | $338.3 \mu \mathrm{~A}$ | 2.927 mA |
| R | $2 \mathrm{k} \Omega$ | $1 \mathrm{k} \Omega$ | $3.3 \mathrm{k} \Omega$ | $4.7 \mathrm{k} \Omega$ | $4.7 \mathrm{k} \Omega$ | $1.538 \mathrm{k} \Omega$ |
| P | 10.12 mW | $457.9 \mu \mathrm{~W}$ | 1.511 mW | $538.0 \mu \mathrm{~W}$ | $538.0 \mu \mathrm{~W}$ | 13.17 mW |

- At $0 \%$ setting, $V_{\text {out }}=0 \mathrm{~V}$
- At $25 \%$ setting, $V_{\text {out }}=1.29 \mathrm{~V}$
- At $50 \%$ setting, $V_{\text {out }}=2.22 \mathrm{~V}$
- At $75 \%$ setting, $V_{\text {out }}=3.87 \mathrm{~V}$
- At $100 \%$ setting, $V_{\text {out }}=10 \mathrm{~V}$

Answer 33

| Voltage | Both loads off | Load 1 on (only) | Load 2 on (only) | Both loads on |
| :---: | :---: | :---: | :---: | :---: |
| $V_{A}$ | 26.4 volts | 26.3 volts | 22.4 volts | 22.3 volts |
| $V_{B}$ | 5 volts | 4.46 volts | 4.23 volts | 3.78 volts |

## Answer 34

Resistor R1 has failed open. This is evident because only load \#1 is receiving any power; the other two loads are completely "dead".

## Answer 35

Resistor R2 has failed open. We can tell this because load \#3 is receiving no power at all while load $\# 2$ is being over-powered.

## Answer 36

Resistor R1 has failed (partially) shorted. We can tell this because both loads $\# 2$ and $\# 3$ are being over-powered.

## Answer 37

The key to calculating all resistor values is to determine how much voltage each one must drop and how much current each one must carry. The current question may be answered by applying Kirchhoff's Current Law (KCL) to each of the nodes in the circuit, while the voltage question may be answered by calculating the voltage difference between each pair of supply lines to the tube circuit.

- $R_{1}=3.25 \mathrm{k} \Omega$
- $R_{2}=11 \mathrm{k} \Omega$
- $R_{3}=3.67 \mathrm{k} \Omega$
- $R_{4}=9 \mathrm{k} \Omega$


## Answer 38 <br> $R=2.667 \mathrm{k} \Omega$


[^0]:    Answer 6

    $$
    P=321.1 \text { watts }
    $$

